formulas

teffects ipwra - Inverse-probability-weighted regression adjustment

Description	Quick start	Menu	Syntax
Options	Remarks and examples	Stored results	Methods and
Reference	Also see		

Description

Title

teffects ipwra estimates the average treatment effect (ATE), the average treatment effect on the treated (ATET), and the potential-outcome means (POMs) from observational data by inverse-probability-weighted regression adjustment (IPWRA). IPWRA estimators use weighted regression coefficients to compute averages of treatment-level predicted outcomes, where the weights are the estimated inverse probabilities of treatment. The contrasts of these averages estimate the treatment effects. IPWRA estimators have the double-robust property. teffects ipwra accepts a continuous, binary, count, fractional, or nonnegative outcome and allows a multivalued treatment.

See [TE] **teffects intro** or [TE] **teffects intro advanced** for more information about estimating treatment effects from observational data.

Quick start

```
ATE of binary treatment treat2 estimated by IPWRA using a linear model for outcome y1 on x1 and
      x2 and a logistic model for treat2 on x1 and w
         teffects ipwra (y1 x1 x2) (treat2 x1 w)
   As above, but estimate the ATET
         teffects ipwra (y1 x1 x2) (treat2 x1 w), atet
   Probit model for binary outcome y3
         teffects ipwra (y3 x1 x2, probit) (treat2 x1 w)
   As above, but use a heteroskedastic probit model for y3 and a probit model for treat2
         teffects ipwra (y3 x1 x2, hetprobit(x1 x2)) (treat2 x1 w, probit)
   As above, but use a fractional heteroskedastic probit model for y4 and a probit model for treat2
         teffects ipwra (y4 x1 x2, fhetprobit(x1 x2)) (treat2 x1 w, probit)
   ATE for each level of a three-valued treatment treat3
         teffects ipwra (y1 x1 x2) (treat3 x1 w)
   As above, and specify that treat3 = 3 is the control level using the value label "MyControl" for 3
         teffects ipwra (y1 x1 x2) (treat3 x1 w), control(MyControl)
Menu
```

Statistics > Treatment effects > Continuous outcomes > Regression adjustment with IPW

Statistics > Treatment effects > Binary outcomes > Regression adjustment with IPW

Statistics > Treatment effects > Count outcomes > Regression adjustment with IPW

Statistics > Treatment effects > Fractional outcomes > Regression adjustment with IPW

Statistics > Treatment effects > Nonnegative outcomes > Regression adjustment with IPW

Syntax

```
teffects ipwra (ovar onvarlist [, omodel noconstant])
  (tvar tmvarlist [, tmodel noconstant]) [if] [in] [weight]
  [, stat options]
```

ovar is a binary, count, continuous, fractional, or nonnegative outcome of interest. *omvarlist* specifies the covariates in the outcome model. *tvar* must contain integer values representing the treatment levels. *tmvarlist* specifies the covariates in the treatment-assignment model.

omodel	Description		
Model			
linear	linear outcome model; the default		
logit	logistic outcome model		
probit	probit outcome model		
hetprobit(<i>varlist</i>)	heteroskedastic probit outcome model		
poisson	exponential outcome model		
flogit	fractional logistic outcome model		
fprobit	fractional probit outcome model		
<pre>fhetprobit(varlist)</pre>	fractional heteroskedastic probit outcome model		

omodel specifies the model for the outcome variable.

tmodel	Description		
Model			
logit	logistic treatment model; the default		
probit	probit treatment model		
<pre>hetprobit(varlist)</pre>	heteroskedastic probit treatment model		

tmodel specifies the model for the treatment variable. For multivalued treatments, only logit is available and multinomial logit is used.

stat	Description
Stat	
ate	estimate average treatment effect in population; the default
atet	estimate average treatment effect on the treated
pomeans	estimate potential-outcome means

options	Description
SE/Robust vce(<i>vcetype</i>)	<i>vcetype</i> may be robust, bootstrap, or jackknife
	verype may be <u>robuse</u> , <u>bobe</u> strap, or <u>Jack</u> hille
Reporting	
<u>l</u> evel(#)	set confidence level; default is level(95)
aequations	display auxiliary-equation results
display_options	control columns and column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling
Maximization maximize_options	control the maximization process; seldom used
Advanced	
<pre>pstolerance(#)</pre>	set tolerance for overlap assumption
osample(<i>newvar</i>)	<i>newvar</i> identifies observations that violate the overlap assumption
<u> </u>	
<u>con</u> trol(# <i>label</i>)	specify the level of <i>tvar</i> that is the control
<u>tle</u> vel(# <i>label</i>)	specify the level of <i>tvar</i> that is the treatment
<u>coefl</u> egend	display legend instead of statistics

omvarlist and tmvarlist may contain factor variables; see [U] 11.4.3 Factor variables. bootstrap, by, jackknife, and statsby are allowed; see [U] 11.1.10 Prefix commands. Weights are not allowed with the bootstrap prefix; see [R] bootstrap. fweights, iweights, and pweights are allowed; see [U] 11.1.6 weight. coeflegend does not appear in the dialog box.

See [U] 20 Estimation and postestimation commands for more capabilities of estimation commands.

Options

Model

noconstant; see [R] estimation options.

Stat

stat is one of three statistics: ate, atet, or pomeans. ate is the default.

ate specifies that the average treatment effect be estimated.

atet specifies that the average treatment effect on the treated be estimated.

pomeans specifies that the potential-outcome means for each treatment level be estimated.

SE/Robust

vce(vcetype) specifies the type of standard error reported, which includes types that are robust to some kinds of misspecification (robust) and that use bootstrap or jackknife methods (bootstrap, jackknife); see [R] vce_option. Reporting

level(#); see [R] estimation options.

aequations specifies that the results for the outcome-model or the treatment-model parameters be displayed. By default, the results for these auxiliary parameters are not displayed.

display_options: noci, nopvalues, noomitted, vsquish, noemptycells, baselevels, allbaselevels, nofvlabel, fvwrap(#), fvwrapon(style), cformat(% fmt), pformat(% fmt), sformat(% fmt), and nolstretch; see [R] estimation options.

Maximization

maximize_options: <u>iter</u>ate(#), <u>[no]log</u>, and from(*init_specs*); see [R] **maximize**. These options are seldom used.

init_specs is one of

matname [, skip copy]
[, # ...], copy

Advanced

- pstolerance(#) specifies the tolerance used to check the overlap assumption. The default value is pstolerance(1e-5). teffects will exit with an error if an observation has an estimated propensity score smaller than that specified by pstolerance().
- osample(*newvar*) specifies that indicator variable *newvar* be created to identify observations that violate the overlap assumption.
- control(#|label) specifies the level of tvar that is the control. The default is the first treatment level. You may specify the numeric level # (a nonnegative integer) or the label associated with the numeric level. control() may not be specified with statistic pomeans. control() and tlevel() may not specify the same treatment level.
- tlevel(#|label) specifies the level of tvar that is the treatment for the statistic atet. The default
 is the second treatment level. You may specify the numeric level # (a nonnegative integer) or
 the label associated with the numeric level. tlevel() may only be specified with statistic atet.
 tlevel() and control() may not specify the same treatment level.

The following option is available with teffects ipwra but is not shown in the dialog box:

coeflegend; see [R] estimation options.

Remarks and examples

Remarks are presented under the following headings:

Overview Video example

Overview

IPWRA estimators use probability weights to obtain outcome-regression parameters that account for the missing-data problem arising from the fact that each subject is observed in only one of the potential outcomes. The adjusted outcome-regression parameters are used to compute averages of treatment-level predicted outcomes. The contrasts of these averages provide estimates of the treatment effects.

stata.com

IPWRA estimators use a model to predict treatment status, and they use another model to predict outcomes. Because IPWRA estimators have the double-robust property, only one of the two models must be correctly specified for the IPWRA estimator to be consistent.

IPWRA estimators use a three-step approach to estimating treatment effects:

- 1. They estimate the parameters of the treatment model and compute inverse-probability weights.
- 2. Using the estimated inverse-probability weights, they fit weighted regression models of the outcome for each treatment level and obtain the treatment-specific predicted outcomes for each subject.
- 3. They compute the means of the treatment-specific predicted outcomes. The contrasts of these averages provide the estimates of the ATEs. By restricting the computations of the means to the subset of treated subjects, we can obtain the ATETs.

These steps produce consistent estimates of the effect parameters because the treatment is assumed to be independent of the potential outcomes after conditioning on the covariates. The overlap assumption ensures that predicted inverse-probability weights do not get too large. The standard errors reported by teffects ipwra correct for the three-step process. See [TE] teffects intro or [TE] teffects intro advanced for more information about this estimator.

We will illustrate the use of teffects ipwra by using data from a study of the effect of a mother's smoking status during pregnancy (mbsmoke) on infant birthweight (bweight) as reported by Cattaneo (2010). This dataset also contains information about each mother's age (mage), education level (medu), marital status (mmarried), whether the first prenatal exam occurred in the first trimester (prenatal1), and whether this baby was the mother's first birth (fbaby).

Example 1: Estimating the ATE

We begin by using teffects ipwra to estimate the average treatment effect of smoking on birthweight. We will use a probit model to predict treatment status as a function of mmarried, mage, and fbaby; to maximize the predictive power of this model, we use factor-variable notation to incorporate quadratic effects of the mother's age, the only continuous covariate in our model. We will use linear regression (the default) to model birthweight, using prenatal1, mmarried, mage, and fbaby as explanatory variables. We type

. use http://www.stata-press.com/data/r14/cattaneo2 (Excerpt from Cattaneo (2010) Journal of Econometrics 155: 138-154)							
-	. teffects ipwra (bweight prenatal1 mmarried mage fbaby) > (mbsmoke mmarried c.mage##c.mage fbaby medu, probit)						
Iteration 0: Iteration 1:							
Estimator Outcome model	Treatment-effects estimation Number of obs = 4,642 Estimator : IPW regression adjustment Outcome model : linear Treatment model: probit				4,642		
bweight	Coef.	Robust Std. Err.	z	P> z	[95%	Conf.	Interval]
ATE mbsmoke (smoker vs nonsmoker)	-229.9671	26.62668	-8.64	0.000	-282.2	1544	-177.7798
POmean mbsmoke nonsmoker	3403.336	9.57126	355.58	0.000	3384	.576	3422.095

The average birthweight if all mothers were to smoke would be 230 grams less than the average of 3,403 grams that would occur if none of the mothers had smoked.

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By default, teffects ipwra displays the ATE and untreated POM. We can specify the pomeans option to display both the treated and untreated POMs, and we can use the aequations option to display the regression model coefficients used to predict the POMs as well as the coefficients from the model used to predict treatment.

Example 2: Displaying the POMs and equations

```
. use http://www.stata-press.com/data/r14/cattaneo2
(Excerpt from Cattaneo (2010) Journal of Econometrics 155: 138-154)
. teffects ipwra (bweight prenatal1 mmarried mage fbaby)
> (mbsmoke mmarried c.mage##c.mage fbaby medu, probit), pomeans aequations
Iteration 0:
              EE criterion = 9.885e-21
Iteration 1:
              EE criterion = 6.922e-26
Treatment-effects estimation
                                                Number of obs
                                                                         4,642
                                                                  =
              : IPW regression adjustment
Estimator
Outcome model : linear
Treatment model: probit
```

bweight	Coef.	Robust Std. Err.	Z	P> z	[95% Conf	. Interval]
POmeans						
mbsmoke						
nonsmoker	3403.336	9.57126	355.58	0.000	3384.576	3422.095
smoker	3173.369	24.86997	127.60	0.000	3124.624	3222.113
 OMEO						
prenatal1	67.98549	28.78428	2.36	0.018	11.56933	124.4017
mmarried	155.5893	26.46903	5.88	0.000	103.711	207.4677
mage	2.893051	2.134788	1.36	0.175	-1.291056	7.077158
fbaby	-71.9215	20.39317	-3.53	0.000	-111.8914	-31.95162
_cons	3194.808	55.04911	58.04	0.000	3086.913	3302.702
OME1						
prenatal1	34.76923	43.18534	0.81	0.421	-49.87248	119.4109
mmarried	124.0941	40.29775	3.08	0.002	45.11193	203.0762
mage	-5.068833	5.954425	-0.85	0.395	-16.73929	6.601626
fbaby	39.89692	56.82072	0.70	0.483	-71.46966	151.2635
_cons	3175.551	153.8312	20.64	0.000	2874.047	3477.054
TME1						
mmarried	6484821	.0554173	-11.70	0.000	757098	5398663
mage	.1744327	.0363718	4.80	0.000	.1031452	.2457202
c.mage#						
c.mage	0032559	.0006678	-4.88	0.000	0045647	0019471
fbaby	2175962	.0495604	-4.39	0.000	3147328	1204595
medu	0863631	.0100148	-8.62	0.000	1059917	0667345
_cons	-1.558255	.4639691	-3.36	0.001	-2.467618	6488926

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As is well known, the standard probit model assumes that the error terms in the latent-utility framework are homoskedastic; the model is not robust to departures from this assumption. An alternative is to use the heteroskedastic probit model, which explicitly models the error variance as a function of a set of variables.

Example 3: Heteroskedastic probit treatment model

Here we use the variables as before, but we use a heteroskedastic probit model to predict treatment status, modeling the heteroskedasticity as a quadratic function of the mother's age:

```
. teffects ipwra (bweight prenatal1 mmarried fbaby c.mage)
> (mbsmoke mmarried c.mage##c.mage fbaby medu, hetprobit(c.mage##c.mage)),
> aequations
Iteration 0: EE criterion = 4.443e-09
Iteration 1: EE criterion = 4.325e-18
Treatment-effects estimation Number of obs = 4,642
Estimator : IPW regression adjustment
Outcome model : linear
Treatment model: heteroskedastic probit
```

bweight	Coef.	Robust Std. Err.	Z	P> z	[95% Conf.	Interval]
ATE mbsmoke (smoker vs nonsmoker)	-229.6322	26.33452	-8.72	0.000	-281.2469	-178.0175
			0.72			
POmean mbsmoke nonsmoker	3403.74	9.545798	356.57	0.000	3385.03	3422.449
	5405.74	9.040790	330.57	0.000		
OMEO						
prenatal1	64.95125	28.62159	2.27	0.023	8.853958	121.0485
mmarried	154.2297	26.45867	5.83	0.000	102.3717	206.0878
fbaby	-71.61131	20.33774	-3.52	0.000	-111.4725	-31.75006
mage	3.010148	2.133812	1.41	0.158	-1.172047	7.192343
_cons	3195.355	55.05451	58.04	0.000	3087.45	3303.26
OME1						
prenatal1	38.55274	43.57024	0.88	0.376	-46.84336	123.9488
mmarried	126.3377	40.7398	3.10	0.002	46.48921	206.1863
fbaby	45.43547	56.4483	0.80	0.421	-65.20116	156.0721
mage	-6.069913	5.95251	-1.02	0.308	-17.73662	5.596792
_cons	3195.795	152.3979	20.97	0.000	2897.101	3494.49
 TME1						
mmarried	0295523	.0238951	-1.24	0.216	0763857	.0172812
mage	.0157893	.0105486	1.50	0.134	0048857	.0364643
c.mage#						
c.mage#	0002837	.0001901	-1.49	0.136	0006563	.0000888
c.mage	.0002037	.0001301	1.45	0.150	.0000303	.0000000
fbaby	0093306	.0080003	-1.17	0.244	025011	.0063497
medu	0036773	.0030317	-1.21	0.225	0096193	.0022647
_cons	1822201	.1180587	-1.54	0.123	4136109	.0491707
TME1_lnsigma						
mage	2211492	.0631504	-3.50	0.000	3449217	0973767
c.mage# c.mage	.0037613	.0012437	3.02	0.002	.0013236	.006199
	L					

The estimated ATE and base-level POM are essentially the same as those produced by the model that used a homoskedastic probit.

Video example

Treatment effects: Inverse-probability-weighted regression adjustment

Stored results

teffects ipwra stores the following in e():

Scalars	
e(N)	number of observations
e(nj)	number of observations for treatment level j
e(k_eq)	number of equations in e(b)
e(k_levels)	number of levels in treatment variable
e(treated)	level of treatment variable defined as treated
e(control)	level of treatment variable defined as control
e(converged)	1 if converged, 0 otherwise
Macros	
e(cmd)	teffects
e(cmdline)	command as typed
e(depvar)	name of outcome variable
e(tvar)	name of treatment variable
e(subcmd)	ipwra
e(tmodel)	logit, probit, or hetprobit
e(omodel)	linear, logit, probit, hetprobit, poisson, flogit, fprobit, or fhetprobit
e(stat)	statistic estimated, ate, atet, or pomeans
e(wtype)	weight type
e(wexp)	weight expression
e(title)	title in estimation output
e(tlevels)	levels of treatment variable
e(vce)	vcetype specified in vce()
e(vcetype)	title used to label Std. Err.
e(properties)	b V
e(estat_cmd)	program used to implement estat
e(predict)	program used to implement predict
e(marginsnotok)	predictions disallowed by margins
e(asbalanced)	factor variables fvset as asbalanced
e(asobserved)	factor variables fvset as asobserved
Matrices	
e(b)	coefficient vector
e(V)	variance-covariance matrix of the estimators
Functions	
e(sample)	marks estimation sample

Methods and formulas

teffects ipwra implements a smooth treatment-effects estimator. All smooth treatment-effects estimators are documented in *Methods and formulas* of [TE] teffects aipw.

Reference

Cattaneo, M. D. 2010. Efficient semiparametric estimation of multi-valued treatment effects under ignorability. Journal of Econometrics 155: 138–154.

Also see

- [TE] teffects postestimation Postestimation tools for teffects
- [TE] teffects Treatment-effects estimation for observational data
- [TE] teffects aipw Augmented inverse-probability weighting
- [U] 20 Estimation and postestimation commands