# Title

tobit postestimation — Postestimation tools for tobit

Postestimation commandspredictmarginsRemarks and examplesReferencesAlso see

# **Postestimation commands**

The following postestimation commands are available after tobit:

Command	Description
contrast	contrasts and ANOVA-style joint tests of estimates
estat ic	Akaike's and Schwarz's Bayesian information criteria (AIC and BIC)
estat summarize	summary statistics for the estimation sample
estat vce	variance-covariance matrix of the estimators (VCE)
estat (svy)	postestimation statistics for survey data
estimates	cataloging estimation results
*forecast	dynamic forecasts and simulations
*hausman	Hausman's specification test
lincom	point estimates, standard errors, testing, and inference for linear combinations of coefficients
linktest	link test for model specification
*lrtest	likelihood-ratio test
margins	marginal means, predictive margins, marginal effects, and average marginal effects
marginsplot	graph the results from margins (profile plots, interaction plots, etc.)
nlcom	point estimates, standard errors, testing, and inference for nonlinear combinations of coefficients
predict	predictions, residuals, influence statistics, and other diagnostic measures
predictnl	point estimates, standard errors, testing, and inference for generalized predictions
pwcompare	pairwise comparisons of estimates
suest	seemingly unrelated estimation
test	Wald tests of simple and composite linear hypotheses
testnl	Wald tests of nonlinear hypotheses

 $^{\ast}$  forecast, hausman, and lrtest are not appropriate with svy estimation results.

# predict

#### **Description for predict**

predict creates a new variable containing predictions such as linear predictions, standard errors, probabilities, and expected values.

#### Menu for predict

Statistics > Postestimation

### Syntax for predict

predict	[type] newvar [if] [in] [, statistic <u>nooff</u> set]				
predict	$[type] \{stub*   newvar_{reg} newvar_{sigma}\} [if] [in], scores$				
statistic	Description				
Main					
xb	linear prediction; the default				
stdp	standard error of the linear prediction				
stdf	standard error of the forecast				
pr( <i>a</i> , <i>b</i> )	$\Pr(a < y_j < b)$				
_ e(a,b)	$E(y_j   a < y_j < b)$				
$\underline{ys}tar(a,b)$	$E(y_j^*), y_j^* = \max\{a, \min(y_j, b)\}$				

These statistics are available both in and out of sample; type predict ... if e(sample) ... if wanted only for the estimation sample.

stdf is not allowed with svy estimation results.

where a and b may be numbers or variables; a missing  $(a \ge .)$  means  $-\infty$ , and b missing  $(b \ge .)$  means  $+\infty$ ; see [U] 12.2.1 Missing values.

### **Options for predict**

🛾 Main 🕽

xb, the default, calculates the linear prediction.

- stdp calculates the standard error of the prediction, which can be thought of as the standard error of the predicted expected value or mean for the observation's covariate pattern. The standard error of the prediction is also referred to as the standard error of the fitted value.
- stdf calculates the standard error of the forecast, which is the standard error of the point prediction
  for 1 observation. It is commonly referred to as the standard error of the future or forecast value.
  By construction, the standard errors produced by stdf are always larger than those produced by
  stdp; see Methods and formulas in [R] regress postestimation.

pr(a,b) calculates  $Pr(a < x_j b + u_j < b)$ , the probability that  $y_j | x_j$  would be observed in the interval (a, b).

*a* and *b* may be specified as numbers or variable names; *lb* and *ub* are variable names; pr(20,30) calculates  $Pr(20 < x_j b + u_j < 30)$ ; pr(*lb*,*ub*) calculates  $Pr(lb < x_j b + u_j < ub)$ ; and pr(20,*ub*) calculates  $Pr(20 < x_j b + u_j < ub)$ .

*a* missing  $(a \ge .)$  means  $-\infty$ ; pr(.,30) calculates  $Pr(-\infty < \mathbf{x}_j \mathbf{b} + u_j < 30)$ ; pr(*lb*,30) calculates  $Pr(-\infty < \mathbf{x}_j \mathbf{b} + u_j < 30)$  in observations for which  $lb \ge .$  and calculates  $Pr(lb < \mathbf{x}_j \mathbf{b} + u_j < 30)$  elsewhere.

*b* missing  $(b \ge .)$  means  $+\infty$ ; pr(20,.) calculates  $Pr(+\infty > \mathbf{x}_j\mathbf{b} + u_j > 20)$ ; pr(20,*ub*) calculates  $Pr(+\infty > \mathbf{x}_j\mathbf{b} + u_j > 20)$  in observations for which  $ub \ge .$  and calculates  $Pr(20 < \mathbf{x}_j\mathbf{b} + u_j < ub)$  elsewhere.

- e(a,b) calculates  $E(\mathbf{x}_j\mathbf{b} + u_j | a < \mathbf{x}_j\mathbf{b} + u_j < b)$ , the expected value of  $y_j|\mathbf{x}_j$  conditional on  $y_j|\mathbf{x}_j$  being in the interval (a,b), meaning that  $y_j|\mathbf{x}_j$  is truncated. a and b are specified as they are for pr().
- ystar(*a*,*b*) calculates  $E(y_j^*)$ , where  $y_j^* = a$  if  $\mathbf{x}_j \mathbf{b} + u_j \leq a$ ,  $y_j^* = b$  if  $\mathbf{x}_j \mathbf{b} + u_j \geq b$ , and  $y_j^* = \mathbf{x}_j \mathbf{b} + u_j$  otherwise, meaning that  $y_j^*$  is censored. *a* and *b* are specified as they are for pr().
- nooffset is relevant only if you specified offset(*varname*). It modifies the calculations made by predict so that they ignore the offset variable; the linear prediction is treated as  $\mathbf{x}_j \mathbf{b}$  rather than as  $\mathbf{x}_j \mathbf{b} + \text{offset}_j$ .

scores calculates equation-level score variables.

The first new variable will contain  $\partial \ln L / \partial (\mathbf{x}_i \boldsymbol{\beta})$ .

The second new variable will contain  $\partial \ln L / \partial \sigma$ .

# margins

### **Description for margins**

margins estimates margins of response for linear predictions, probabilities, and expected values.

### Menu for margins

Statistics > Postestimation

### Syntax for margins

margins [ma	urginlist ] [, options]
margins [ma	arginlist]       , predict(statistic)       [predict(statistic)       [ options ]
statistic	Description
xb	linear prediction; the default
pr( <i>a</i> , <i>b</i> )	$\Pr(a < y_j < b)$
_ e(a,b)	$E(y_j   a < y_j < b)$
ystar(a,b)	$E(y_{j}^{*}), y_{j}^{*} = \max\{a, \min(y_{j}, b)\}$
stdp	not allowed with margins
stdf	not allowed with margins

Statistics not allowed with margins are functions of stochastic quantities other than e(b). For the full syntax, see [R] margins.

# **Remarks and examples**

stata.com

Following Cong (2000), write the tobit model as

$$y_i^* = egin{cases} y_i, & ext{if } a < y_i < b \ a, & ext{if } y_i \leq a \ b, & ext{if } y_i \geq b \end{cases}$$

 $y_i$  is a latent variable; instead, we observe  $y_i^*$ , which is bounded between a and b if  $y_i$  is outside those bounds.

There are four types of marginal effects that may be of interest in the tobit model, depending on the application:

- 1. The  $\beta$  coefficients themselves measure how the unobserved variable  $y_i$  changes with respect to changes in the regressors.
- 2. The marginal effects of the truncated expected value  $E(y_i^*|a < y_i^* < b)$  measure the changes in  $y_i$  with respect to changes in the regressors among the subpopulation for which  $y_i$  is not at a boundary.
- 3. The marginal effects of the censored expected value  $E(y_i^*)$  describe how the observed variable  $y_i^*$  changes with respect to the regressors.
- 4. The marginal effects of  $Pr(a < y_i^* < b)$  describe how the probability of being uncensored changes with respect to the regressors.

In the next example, we show how to obtain each of these.

### Example 1

In example 3 of [R] tobit, we fit a two-limit tobit model of mpg on wgt.

<pre>. use http://www.stata-press.com/data/r14/auto (1978 Automobile Data) . generate wgt = weight/1000 . tobit mpg wgt, ll(17) ul(24)</pre>							
Tobit regress:	ion			Number o	of obs	=	74
0				LR chi2	(1)	=	77.60
				Prob > d	hi2	=	0.0000
Log likelihood	d = -104.25976	3		Pseudo H	12	=	0.2712
mpg	Coef.	Std. Err.	t	P> t	[95%	Conf.	Interval]
wgt	-5.764448	.7245417	-7.96	0.000	-7.208	3457	-4.320438
_cons	38.07469	2.255917	16.88	0.000	33.57	7865	42.57072
/sigma	2.886337	.3952143			2.098	3676	3.673998
<pre>18 left-censored observations at mpg &lt;= 17 33 uncensored observations 23 right-censored observations at mpg &gt;= 24</pre>							

tobit reports the  $\beta$  coefficients for the latent regression model. The marginal effect of  $x_k$  on y is simply the corresponding  $\beta_k$ , because E(y|x) is linear in x. Thus a 1,000-pound increase in a car's weight (which is a 1-unit increase in wgt) would lower fuel economy by 5.8 mpg.

To estimate the means of the marginal effects on the expected value of the censored outcome, conditional on weight being each of three values (2,000; 3,000; and 4,000 pounds), we type

. margins, dy	dx(wgt) predi	ct(ystar(17,2	24)) at(1	wgt=(2 3	4))	
Conditional m Model VCE	arginal effec : OIM	ts		Number	of obs =	74
<pre>Expression : E(mpg* 17<mpg<24), :="" dx="" dy="" pre="" predict(ystar(17,24))="" w.r.t.="" wgt<=""></mpg<24),></pre>						
1at	: wgt	=	2			
2at	: wgt	=	3			
3at	: wgt	=	4			
	dy/dx	Delta-method Std. Err.	z	P> z	[95% Conf.	Interval]
wgt at						
1	-1.0861	.311273	-3.49	0.000	-1.696184	4760162
2	-4.45315		-9.33			
3	-1.412822	.3289702	-4.29	0.000	-2.057591	768052

The  $E(y^*|x)$  is nonlinear in x, so the marginal effect for a continuous covariate is not the same as the change in  $y^*$  induced by a one-unit change in x. Recall that the marginal effect at a point is the slope of the tangent line at that point. In our example, we estimate the mean of the marginal effects for different values of wgt. The estimated mean of the marginal effects is -1.1 mpg for a 2,000 pound car; -4.5 mpg for a 3,000 pound car; and -1.4 mpg for a 4,000 pound car.

To estimate the means of the marginal effects on the expected value of the truncated outcome at the same levels of wgt, we type

<pre>. margins, dydx(wgt) predict(e(17,24)) at(wgt=(2 3 4))</pre>						
Conditional ma Model VCE	arginal effect : OIM	.s		Number o	f obs =	74
<pre>Expression : E(mpg 17<mpg<24), :="" dx="" dy="" pre="" predict(e(17,24))="" w.r.t.="" wgt<=""></mpg<24),></pre>						
1at	: wgt	=	2			
2at	: wgt	=	3			
3at	: wgt	=	4			
	I dy/dx	Delta-method Std. Err.		P> z	[95% Conf.	Interval]
wgt						
_at 1 2 3	-1.166572 -2.308842 -1.288896		-14.10 -5.40 -14.49		-1.328768 -3.146477 -1.463188	-1.004375 -1.471207 -1.114604

The mean of the marginal effects of a change in wgt on  $y_i$  (which is bounded between 17 and 24) is about -1.2 mpg for a 2,000 pound car; -2.3 mpg for a 3,000 pound car; and -1.3 for a 4,000 pound car.

# References

Cong, R. 2000. sg144: Marginal effects of the tobit model. Stata Technical Bulletin 56: 27–34. Reprinted in Stata Technical Bulletin Reprints, vol. 10, pp. 189–197. College Station, TX: Stata Press.

McDonald, J. F., and R. A. Moffitt. 1980. The use of tobit analysis. Review of Economics and Statistics 62: 318-321.

# Also see

- [R] tobit Tobit regression
- [U] 20 Estimation and postestimation commands