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rreg — Robust regression

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Description

rreg performs one version of robust regression of depvar on indepvars.

Also see *Robust standard errors* in [R] **regress** for standard regression with robust variance estimates and [R] **qreg** for quantile (including median or least-absolute-residual) regression.

Quick start

Robust regression of y on x

rreg y x

Add a categorical covariate a using factor-variable syntax

rreg y x i.a

As above, but set the tuning parameter to 8

rreg y x i.a, tune(8)

Generate a new variable wvar containing the final weight for each observation

rreg y x i.a, genwt(wvar)

Set confidence level to 99%

rreg y x i.a, level(99)

Menu

Statistics > Linear models and related > Other > Robust regression

```
rreg depvar [indepvars] [if] [in] [, options]
```

options	Description
Model	
<u>tu</u> ne(#)	use # as the biweight tuning constant; default is tune(7)
Reporting	
<u>l</u> evel(#)	set confidence level; default is level(95)
genwt(<i>newvar</i>)	create newvar containing the weights assigned to each observation
_ display_options	control columns and column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling
Optimization	
optimization_options	control the optimization process; seldom used
graph	graph weights during convergence
<u>coefl</u> egend	display legend instead of statistics

indepvars may contain factor variables; see [U] 11.4.3 Factor variables.

depvar and indepvars may contain time-series operators; see [U] 11.4.4 Time-series varlists.

by, mfp, mi estimate, rolling, and statsby are allowed; see [U] 11.1.10 Prefix commands.

coeflegend does not appear in the dialog box.

See [U] 20 Estimation and postestimation commands for more capabilities of estimation commands.

Options

Model

tune(#) is the biweight tuning constant. The default is 7, meaning seven times the median absolute deviation (MAD) from the median residual; see *Methods and formulas*. Lower tuning constants downweight outliers rapidly but may lead to unstable estimates (less than 6 is not recommended). Higher tuning constants produce milder downweighting.

```
Reporting
```

level(#); see [R] estimation options.

genwt (newvar) creates the new variable newvar containing the weights assigned to each observation.

display_options: noci, nopvalues, noomitted, vsquish, noemptycells, baselevels,
 allbaselevels, nofvlabel, fvwrap(#), fvwrapon(style), cformat(%fmt), pformat(%fmt),
 sformat(%fmt), and nolstretch; see [R] estimation options.

```
Optimization
```

optimization_options: <u>iterate(#)</u>, <u>tolerance(#)</u>, <u>nolerance()</u> specifies the maximum number of iterations; iterations stop when the maximum change in weights drops below tolerance(); and log/nolog specifies whether to show the iteration log. These options are seldom used.

graph allows you to graphically watch the convergence of the iterative technique. The weights obtained from the most recent round of estimation are graphed against the weights obtained from the previous round.

The following option is available with rreg but is not shown in the dialog box: coeflegend; see [R] estimation options.

Remarks and examples

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rreg first performs an initial screening based on Cook's distance > 1 to eliminate gross outliers before calculating starting values and then performs Huber iterations followed by biweight iterations, as suggested by Li (1985).

Example 1

We wish to examine the relationship between mileage rating, weight, and location of manufacture for the 74 cars in the auto.dta. As a point of comparison, we begin by fitting an ordinary regression:

- . use http://www.stata-press.com/data/r14/auto
 (1978 Automobile Data)
- . regress mpg weight foreign

Source	SS	df	MS	Number of obs	=	74 69.75
Model Residual	1619.2877 824.171761	2 71	809.643849 11.608053	Prob > F R-squared	=	0.0000 0.6627 0.6532
Total	2443.45946	73	33.4720474	- Adj R-squared Root MSE	=	3.4071
mpg	Coef.	Std. Err.	t	P> t [95% C	onf.	Interval]
weight foreign _cons	0065879 -1.650029 41.6797	.0006371 1.075994 2.165547	-1.53	0.00000785 0.130 -3.79 0.000 37.361	55	0053175 .4954422 45.99768

We now compare this with the results from rreg:

```
. rreg mpg weight foreign
   Huber iteration 1: maximum difference in weights = .80280176
   Huber iteration 2: maximum difference in weights = .2915438
   Huber iteration 3: maximum difference in weights = .08911171
   Huber iteration 4: maximum difference in weights = .02697328
Biweight iteration 5: maximum difference in weights = .29186818
Biweight iteration 6: maximum difference in weights = .11988101
Biweight iteration 7: maximum difference in weights = .03315872
Biweight iteration 8: maximum difference in weights = .00721325
Robust regression
                                                Number of obs
                                                                             74
                                                F( 2,
                                                              71) =
                                                                         168.32
                                                Prob > F
                                                                         0.0000
                    Coef.
                            Std. Err.
                                                P>|t|
                                                           [95% Conf. Interval]
         mpg
                                           t
      weight
                -.0063976
                            .0003718
                                       -17.21
                                                0.000
                                                           -.007139
                                                                      -.0056562
```

-5.07

32.16

0.000

0.000

-4.434763

38.1202

.627964

1.263841

Note the large change in the foreign coefficient.

-3.182639

40.64022

foreign

_cons

-1.930514

43.16025

□ Technical note

It would have been better if we had fit the previous robust regression by typing rreg mpg weight foreign, genwt(w). The new variable, w, would then contain the estimated weights. Let's pretend that we did this:

- . rreg mpg weight foreign, genwt(w)
 (output omitted)
- . summarize w, detail

Robust Regression Weight

	Percentiles	Smallest		
1%	0	0		
5%	.0442957	0		
10%	.4674935	0	Obs	74
25%	.8894815	.0442957	Sum of Wgt.	74
50%	.9690193		Mean	.8509966
		Largest	Std. Dev.	.2746451
75%	.9949395	.9996715		
90%	.9989245	.9996953	Variance	.0754299
95%	.9996715	.9997343	Skewness	-2.287952
99%	.9998585	.9998585	Kurtosis	6.874605

We discover that 3 observations in our data were dropped altogether (they have weight 0). We could further explore our data:

- . sort w
- . list make mpg weight w if w < .467, sep(0)

	make	mpg	weight	w
1.	Datsun 210	35	2,020	0
2.	VW Diesel	41	2,040	0
3.	Subaru	35	2,050	0
4.	Plym. Arrow	28	3,260	.04429567
5.	Cad. Seville	21	4,290	.08241943
6.	Toyota Corolla	31	2,200	.10443129
7.	Olds 98	21	4,060	.28141296

Being familiar with the automobile data, we immediately spotted two things: the VW is the only diesel car in our data, and the weight recorded for the Plymouth Arrow is incorrect.

Example 2

If we specify no explanatory variables, rreg produces a robust estimate of the mean:

```
. rreg mpg
   Huber iteration 1: maximum difference in weights = .64471879
   Huber iteration 2: maximum difference in weights = .05098336
   Huber iteration 3: maximum difference in weights = .0099887
Biweight iteration 4: maximum difference in weights = .25197391
Biweight iteration 5: maximum difference in weights = .00358606
Robust regression
                                                 Number of obs
                                                                             74
                                                 F( 0,
                                                               73) =
                                                                           0.00
                                                Prob > F
                    Coef.
                            Std. Err.
                                           t
                                                P>|t|
                                                           [95% Conf. Interval]
                                        32.23
                 20.68825
                                                 0.000
                                                           19.40912
                                                                       21.96738
       _cons
                             .641813
```

The estimate is given by the coefficient on $_cons$. The mean is 20.69 with an estimated standard error of 0.6418. The 95% confidence interval is [19.4, 22.0]. By comparison, ci means (see [R] ci) gives us the standard calculation:

Ī	mpg	74	21.2973	.6725511	19.9569	22.63769
	Variable	Obs	Mean	Std. Err.	[95% Conf.	Interval]
	. ci means mpg	S				

Stored results

rreg stores the following in e():

```
Scalars
                          number of observations
    e(N)
    e(mss)
                          model sum of squares
    e(df_m)
                          model degrees of freedom
    e(rss)
                          residual sum of squares
    e(df_r)
                          residual degrees of freedom
    e(r2)
                          R-squared
    e(r2_a)
                          adjusted R-squared
    e(F)
                          F statistic
    e(rmse)
                          root mean squared error
    e(rank)
                          rank of e(V)
Macros
    e(cmd)
                          rreg
    e(cmdline)
                          command as typed
                          name of dependent variable
    e(depvar)
    e(genwt)
                          variable containing the weights
                          title in estimation output
    e(title)
    e(model)
                          ols
    e(vce)
                          ols
    e(properties)
    e(predict)
                          program used to implement predict
    e(marginsok)
                          predictions allowed by margins
                          factor variables fvset as asbalanced
    e(asbalanced)
    e(asobserved)
                          factor variables fyset as asobserved
```

Matrices e(b) e(V)	coefficient vector variance-covariance matrix of the estimators
Functions e(sample)	marks estimation sample

Methods and formulas

See Berk (1990), Goodall (1983), and Rousseeuw and Leroy (1987) for a general description of the issues and methods. Hamilton (1991a, 1992) provides a more detailed description of rreg and some Monte Carlo evaluations.

rreg begins by fitting the regression (see [R] regress), calculating Cook's D (see [R] predict and [R] regress postestimation), and excluding any observation for which D > 1.

Thereafter rreg works iteratively: it performs a regression, calculates case weights from absolute residuals, and regresses again using those weights. Iterations stop when the maximum change in weights drops below tolerance(). Weights derive from one of two weight functions, Huber weights and biweights. Huber weights (Huber 1964) are used until convergence, and then, from that result, biweights are used until convergence. The biweight was proposed by Beaton and Tukey (1974, 151–152) after the Princeton robustness study (Andrews et al. 1972) had compared various estimators. Both weighting functions are used because Huber weights have problems dealing with severe outliers, whereas biweights sometimes fail to converge or have multiple solutions. The initial Huber weighting should improve the behavior of the biweight estimator.

In Huber weighting, cases with small residuals receive weights of 1; cases with larger residuals receive gradually smaller weights. Let $e_i = y_i - \mathbf{X}_i \mathbf{b}$ represent the *i*th-case residual. The *i*th scaled residual $u_i = e_i/s$ is calculated, where s = M/0.6745 is the residual scale estimate and $M = \text{med}(|e_i - \text{med}(e_i)|)$ is the median absolute deviation from the median residual. Huber estimation obtains case weights:

$$w_i = \begin{cases} 1 & \text{if } |u_i| \le c_h \\ c_h/|u_i| & \text{otherwise} \end{cases}$$

rreg defines $c_h=1.345$, so downweighting begins with cases whose absolute residual exceeds $(1.345/0.6745)M\approx 2M$.

With biweights, all cases with nonzero residuals receive some downweighting, according to the smoothly decreasing biweight function

$$w_i = \begin{cases} \{1 - (u_i/c_b)^2\}^2 & \text{if } |u_i| \le c_b \\ 0 & \text{otherwise} \end{cases}$$

where $c_b = 4.685 \times \text{tune}()/7$. Thus when tune() = 7, cases with absolute residuals of $(4.685/0.6745)M \approx 7M$ or more are assigned 0 weight and thus are effectively dropped. Goodall (1983, 377) suggests using a value between 6 and 9, inclusive, for tune() in the biweight case and states that performance is good between 6 and 12, inclusive.

The tuning constants $c_h = 1.345$ and $c_b = 4.685$ (assuming tune() is set at the default 7) give rreg about 95% of the efficiency of OLS when applied to data with normally distributed errors (Hamilton 1991b). Lower tuning constants downweight outliers more drastically (but give up Gaussian efficiency); higher tuning constants make the estimator more like OLS.

Standard errors are calculated using the pseudovalues approach described in Street, Carroll, and Ruppert (1988).

Acknowledgment

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Also see

- [R] **rreg postestimation** Postestimation tools for rreg
- [R] **qreg** Quantile regression
- [R] **regress** Linear regression
- [MI] **estimation** Estimation commands for use with mi estimate
- [U] 20 Estimation and postestimation commands