estat gof - Pearson or Hosmer-Lemeshow goodness-of-fit test

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# Description

estat gof reports the Pearson goodness-of-fit test or the Hosmer-Lemeshow goodness-of-fit test.

estat gof requires that the current estimation results be from logistic, logit, or probit; see [R] logistic, [R] logit, or [R] probit. For estat gof after poisson, see [R] poisson postestimation. For estat gof after sem, see [SEM] estat gof.

# **Quick start**

Pearson goodness-of-fit test for current estimation results estat gof

As above, but apply to all observations in dataset instead of just those in e(sample) estat gof, all

Hosmer-Lemeshow goodness-of-fit test estat gof, group(10)

As above, and display table of groups used for the test estat gof, group(10) table

# Menu for estat

Statistics > Postestimation

# Title

# Syntax

estat goi	[ <i>if</i> ]	in	weight	[,	options ]
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options	Description
Main	
group(#)	perform Hosmer-Lemeshow goodness-of-fit test using # quantiles
all	execute test for all observations in the data
<u>out</u> sample	adjust degrees of freedom for samples outside estimation sample
<u>t</u> able	display table of groups used for test

fweights are allowed; see [U] 11.1.6 weight.

estat gof is not appropriate after the svy prefix.

## Options

\_∫ Main ]

group(#) specifies the number of quantiles to be used to group the data for the Hosmer-Lemeshow goodness-of-fit test. group(10) is typically specified. If this option is not given, the Pearson goodness-of-fit test is computed using the covariate patterns in the data as groups.

- all requests that the statistic be computed for all observations in the data, ignoring any if or in restrictions specified by the estimation command.
- outsample adjusts the degrees of freedom for the Pearson and Hosmer-Lemeshow goodness-of-fit tests for samples outside the estimation sample. See *Samples other than the estimation sample* later in this entry.
- table displays a table of the groups used for the Hosmer-Lemeshow or Pearson goodness-of-fit test with predicted probabilities, observed and expected counts for both outcomes, and totals for each group.

## **Remarks and examples**

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Remarks are presented under the following headings:

Introduction Samples other than the estimation sample

### Introduction

estat gof computes goodness-of-fit tests: either the Pearson  $\chi^2$  test or the Hosmer-Lemeshow test.

By default, estat gof computes statistics for the estimation sample by using the last model fit by logistic, logit, or probit. However, samples other than the estimation sample can be specified; see Samples other than the estimation sample later in this entry.

### Example 1

estat gof, typed without options, presents the Pearson  $\chi^2$  goodness-of-fit test for the fitted model. The Pearson  $\chi^2$  goodness-of-fit test is a test of the observed against expected number of responses using cells defined by the covariate patterns; see *predict with the number option* in [R] logistic postestimation for the definition of covariate patterns.

```
. use http://www.stata-press.com/data/r14/lbw
(Hosmer & Lemeshow data)
. logistic low age lwt i.race smoke ptl ht ui
(output omitted)
. estat gof
Logistic model for low, goodness-of-fit test
    number of observations = 189
number of covariate patterns = 182
    Pearson chi2(173) = 179.24
    Prob > chi2 = 0.3567
```

Our model fits reasonably well. However, the number of covariate patterns is close to the number of observations, making the applicability of the Pearson  $\chi^2$  test questionable but not necessarily inappropriate. Hosmer, Lemeshow, and Sturdivant (2013, 157–160) suggest regrouping the data by ordering on the predicted probabilities and then forming, say, 10 nearly equal-sized groups. estat gof with the group() option does this:

```
. estat gof, group(10)
Logistic model for low, goodness-of-fit test
(Table collapsed on quantiles of estimated probabilities)
number of observations = 189
number of groups = 10
Hosmer-Lemeshow chi2(8) = 9.65
Prob > chi2 = 0.2904
```

Again we cannot reject our model. If we specify the table option, estat gof displays the groups along with the expected and observed number of positive responses (low-birthweight babies):

```
. estat gof, group(10) table
```

```
Logistic model for low, goodness-of-fit test
```

(Table collapsed on quantiles of estimated probabilities)

Group	Prob	Obs_1	Exp_1	Obs_0	Exp_0	Total
1	0.0827	0	1.2	19	17.8	19
2	0.1276	2	2.0	17	17.0	19
3	0.2015	6	3.2	13	15.8	19
4	0.2432	1	4.3	18	14.7	19
5	0.2792	7	4.9	12	14.1	19
6	0.3138	7	5.6	12	13.4	19
7	0.3872	6	6.5	13	12.5	19
8	0.4828	7	8.2	12	10.8	19
9	0.5941	10	10.3	9	8.7	19
10	0.8391	13	12.8	5	5.2	18
number of observations = 189						

number of observations =
 number of groups =
Hosmer-Lemeshow chi2(8) =

Prob > chi2 =

100

9.65

0.2904

#### Technical note

estat gof with the group() option puts all observations with the same predicted probabilities into the same group. If, as in the previous example, we request 10 groups, the groups that estat gof makes are  $[p_0, p_{10}], (p_{10}, p_{20}], (p_{20}, p_{30}], \ldots, (p_{90}, p_{100}]$ , where  $p_k$  is the kth percentile of the predicted probabilities, with  $p_0$  the minimum and  $p_{100}$  the maximum.

If there are many ties at the quantile boundaries, as will often happen if all independent variables are categorical and there are only a few of them, the sizes of the groups will be uneven. If the totals in some of the groups are small, the  $\chi^2$  statistic for the Hosmer–Lemeshow test may be unreliable. In this case, fewer groups should be specified, or the Pearson goodness-of-fit test may be a better choice.

### Example 2

. . .

The table option can be used without the group() option. We would not want to specify this for our current model because there were 182 covariate patterns in the data, caused by including the two continuous variables, age and lwt, in the model. As an aside, we fit a simpler model and specify table with estat gof:

. logistic lou	w i.race smoke	e ui					
Logistic regre	Logistic regression				of obs	=	189
				LR chi2	(4)	=	18.80
				Prob > o	chi2	=	0.0009
Log likelihood	d = -107.93404	4		Pseudo I	32	=	0.0801
low	Odds Ratio	Std. Err.	Z	P> z	[95%	Conf.	Interval]
race							
black	3.052746	1.498087	2.27	0.023	1.166	3747	7.987382
other	2.922593	1.189229	2.64	0.008	1.316	6457	6.488285
smoke	2.945742	1.101838	2.89	0.004	1.415	5167	6.131715
ui	2.419131	1.047359	2.04	0.041	1.035	5459	5.651788
_cons	.1402209	.0512295	-5.38	0.000	.0685	5216	.2869447

		-				
Group	Prob	Obs_1	Exp_1	Obs_0	Exp_0	Total
1	0.1230	3	4.9	37	35.1	40
2	0.2533	1	1.0	3	3.0	4
3	0.2907	16	13.7	31	33.3	47
4	0.2923	15	12.6	28	30.4	43
5	0.2997	3	3.9	10	9.1	13
6	0.4978	4	4.0	4	4.0	8
7	0.4998	4	4.5	5	4.5	9
8	0.5087	2	1.5	1	1.5	3
9	0.5469	2	4.4	6	3.6	8
10	0.5577	6	5.6	4	4.4	10
11	0.7449	3	3.0	1	1.0	4

-				
Logistic m	nodel for	low,	goodness-of-fit	test

. estat gof, table

Group	Prob	race	smoke	ui
1	0.1230	white	nonsmoker	0
2	0.2533	white	nonsmoker	1
3	0.2907	other	nonsmoker	0
4	0.2923	white	smoker	0
5	0.2997	black	nonsmoker	0
6	0.4978	other	nonsmoker	1
7	0.4998	white	smoker	1
8	0.5087	black	nonsmoker	1
9	0.5469	other	smoker	0
10	0.5577	black	smoker	0
11	0.7449	other	smoker	1
11     0.7449     other     smoker     1       number of observations =     189				

number of covariate patterns = 11 Pearson chi2(6) = 5.71 Prob > chi2 = 0.4569

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### Technical note

logistic, logit, or probit and estat gof keep track of the estimation sample. If you type, for instance, logistic ... if x==1, then when you type estat gof, the statistics will be calculated on the x==1 subsample of the data automatically.

You should specify if or in with estat gof only when you wish to calculate statistics for a set of observations other than the estimation sample. See *Samples other than the estimation sample* later in this entry.

If the logistic model was fit with fweights, estat gof properly accounts for the weights in its calculations. (estat gof only allows fweights.) You do not have to specify the weights when you run estat gof. Weights should be specified with estat gof only when you wish to use a different set of weights.

#### Samples other than the estimation sample

estat gof can be used with samples other than the estimation sample. By default, estat gof remembers the estimation sample used with the last logistic, logit, or probit command. To override this, simply use an if or in restriction to select another set of observations, or specify the all option to force the command to use all the observations in the dataset.

If you use estat gof with a sample that is completely different from the estimation sample (that is, no overlap), you should also specify the outsample option so that the  $\chi^2$  statistic properly adjusts the degrees of freedom upward. For an overlapping sample, the conservative thing to do is to leave the degrees of freedom the same as they are for the estimation sample.

Example 3

We want to develop a model for predicting low-birthweight babies. One approach would be to divide our data into two groups, a developmental sample and a validation sample. See Lemeshow and Gall (1994) and Tilford, Roberson, and Fiser (1995) for more information on developing prediction models and severity-scoring systems.

We will do this with the low-birthweight data that we considered previously. First, we randomly divide the data into two samples.

```
. use http://www.stata-press.com/data/r14/lbw, clear
(Hosmer & Lemeshow data)
. set seed 101
. generate r = runiform()
. sort r
. generate group = 1 if _n <= _N/2
(95 missing values generated)
. replace group = 2 if group==.
(95 real changes made)
```

Then we fit a model using the first sample (group = 1), which is our developmental sample.

. logistic low	v age iwt i.i.	ace smoke pt	I IIC UI I	ri group	•1	
Logistic regre	ession			Number o	of obs =	94
• •				LR chi2(	(8) =	28.03
				Prob > c	:hi2 =	0.0005
Log likelihood	d = -42.35111	2		Pseudo R	.2 =	0.2487
low	Odds Ratio	Std. Err.	z	P> z	[95% Conf.	Interval]
age	.922865	.0555349	-1.33	0.182	.8201924	1.03839
lwt	.9825782	.0114438	-1.51	0.131	.9604029	1.005265
race						
black	5.975476	4.936135	2.16	0.030	1.183652	30.16621
other	3.364479	2.760784	1.48	0.139	.6736724	16.803
smoke	3.442716	2.53779	1.68	0.094	.8117831	14.60032
ptl	3.467274	2.337648	1.84	0.065	.9249222	12.99784
ht	5.928512	6.047106	1.74	0.081	.8030021	43.76982
ui	4.045883	2.947396	1.92	0.055	.9703295	16.8697
_cons	3.120871	5.977489	0.59	0.552	.0731049	133.231

. logistic low age lwt i.race smoke ptl ht ui if group==1

To test calibration in the developmental sample, we calculate the Hosmer-Lemeshow goodness-of-fit test by using estat gof.

```
. estat gof, group(10)
Logistic model for low, goodness-of-fit test
(Table collapsed on quantiles of estimated probabilities)
number of observations = 94
number of groups = 10
Hosmer-Lemeshow chi2(8) = 5.64
Prob > chi2 = 0.6871
```

We did not specify an if statement with estat gof because we wanted to use the estimation sample. Because the test is not significant, we are satisfied with the fit of our model.

Running lroc (see [R] lroc) gives a measure of the discrimination:

```
. lroc, nograph
Logistic model for low
number of observations = 94
area under ROC curve = 0.8145
```

Now we test the calibration of our model by performing a goodness-of-fit test on the validation sample. We specify the outsample option so that the number of degrees of freedom is 10 rather than 8.

. estat gof if group==2, group(10) table outsample

Prob > chi2 =

#### Logistic model for low, goodness-of-fit test

(Table collapsed on quantiles of estimated probabilities)

Group	Prob	Obs_1	Exp_1	Obs_0	Exp_0	Total
1	0.0276	0	0.2	10	9.8	10
2	0.0496	2	0.4	7	8.6	9
3	0.0875	1	0.7	9	9.3	10
4	0.1536	4	1.1	5	7.9	9
5	0.2283	4	2.0	6	8.0	10
6	0.2842	4	2.2	5	6.8	9
7	0.4190	3	3.6	7	6.4	10
8	0.5248	5	4.3	4	4.7	9
9	0.6413	5	5.8	5	4.2	10
10	0.9787	4	7.3	5	1.7	9
number of observations = 95					·	
num	number of groups =					
number of groups = 10 Hosmer-Lemeshow chi2(10) = 29.30						

We must acknowledge that our model does not fit well on the validation sample. The model's discrimination in the validation sample is appreciably lower, as well.

0.0011

. lroc if group==2, nograph Logistic model for low number of observations = 95 area under ROC curve = 0.6835

4

## Stored results

estat gof stores the following in r():

Scalars	
r(N)	number of observations
r(m)	number of covariate patterns or groups
r(df)	degrees of freedom
r(chi2)	$\chi^2$

## Methods and formulas

Let M be the total number of covariate patterns among the N observations. View the data as collapsed on covariate patterns j = 1, 2, ..., M, and define  $m_j$  as the total number of observations having covariate pattern j and  $y_j$  as the total number of positive responses among observations with covariate pattern j. Define  $p_j$  as the predicted probability of a positive outcome in covariate pattern j.

The Pearson  $\chi^2$  goodness-of-fit statistic is

$$\chi^2 = \sum_{j=1}^{M} \frac{(y_j - m_j p_j)^2}{m_j p_j (1 - p_j)}$$

This  $\chi^2$  statistic has approximately M - k degrees of freedom for the estimation sample, where k is the number of independent variables, including the constant. For a sample outside the estimation sample, the statistic has M degrees of freedom.

The Hosmer-Lemeshow goodness-of-fit  $\chi^2$  (Hosmer and Lemeshow 1980; Lemeshow and Hosmer 1982; Hosmer, Lemeshow, and Klar 1988) is calculated similarly, except that rather than using the M covariate patterns as the group definition, the quantiles of the predicted probabilities are used to form groups. Let G = # be the number of quantiles requested with group(#). The smallest index  $1 \le q(i) \le M$ , such that

$$W_{q(i)} = \sum_{j=1}^{q(i)} m_j \ge \frac{N}{G}$$

gives  $p_{q(i)}$  as the upper boundary of the *i*th quantile for i = 1, 2, ..., G. Let q(0) = 1 denote the first index.

The groups are then

$$[p_{q(0)}, p_{q(1)}], (p_{q(1)}, p_{q(2)}], \dots, (p_{q(G-1)}, p_{q(G)}]$$

If the table option is given, the upper boundaries  $p_{q(1)}, \ldots, p_{q(G)}$  of the groups appear next to the group number on the output.

The resulting  $\chi^2$  statistic has approximately G-2 degrees of freedom for the estimation sample. For a sample outside the estimation sample, the statistic has G degrees of freedom.

### References

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- Tilford, J. M., P. K. Roberson, and D. H. Fiser. 1995. sbe12: Using lfit and lroc to evaluate mortality prediction models. *Stata Technical Bulletin* 28: 14–18. Reprinted in *Stata Technical Bulletin Reprints*, vol. 5, pp. 77–81. College Station, TX: Stata Press.

## Also see

- [R] logistic Logistic regression, reporting odds ratios
- [R] logit Logistic regression, reporting coefficients
- [R] **probit** Probit regression
- [R] estat classification Classification statistics and table
- [R] **lroc** Compute area under ROC curve and graph the curve
- [R] lsens Graph sensitivity and specificity versus probability cutoff
- [U] 20 Estimation and postestimation commands