Title

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polyeval( ) — Manipulate and evaluate polynomials

Description Syntax Remarks and examples Conformability
Diagnostics Also see

Description

`polyeval(`c`,` x`)` evaluates polynomial c at each value recorded in x, returning the results in a p-conformable-with-x vector. For instance, `polyeval((4,2,1), (3\5))` returns `(4+2*3+3^2 \ 4+2*5+5^2) = (19\39)`.

`polysolve(`y`,` x`)` returns the minimal-degree polynomial c fitting $y =$ `polyeval(`c`,` x`)`. Solution is via Lagrange's interpolation formula.

`polytrim(`c`)` returns polynomial c with trailing zeros removed. For instance, `polytrim((1,2,3,0))` returns `(1,2,3)`. `polytrim((0,0,0,0))` returns `(0)`. Thus if $n =$ `cols(polytrim(`c`))`, then c records an $(n-1)$th degree polynomial.

`polyderiv(`c`,` i`)` returns the polynomial that is the ith derivative of polynomial c. For instance, `polyderiv((4,2,1), 1)` returns `(2,2)` (the derivative of $4+2x+x^2$ is $2+2x$). The value of the first derivative of polynomial c at x is `polyeval(polyderiv(`c`,1),`x`)`.

`polyinteg(`c`,` i`)` returns the polynomial that is the ith integral of polynomial c. For instance, `polyinteg((4,2,1), 1)` returns `(0,4,1,.3333)` (the integral of $4+2x+x^2$ is $0+4x+x^2+.3333x^3$). The value of the integral of polynomial c at x is `polyeval(polyinteg(`c`,1),` x`)`.

`polyadd(`c_1`,` c_2`)` returns the polynomial that is the sum of the polynomials c_1 and c_2. For instance, `polyadd((2,1), (3,5,1))` is `(5,6,1)` (the sum of $2+x$ and $3+5x+x^2$ is $5+6x+x^2$).

`polymult(`c_1`,` c_2`)` returns the polynomial that is the product of the polynomials c_1 and c_2. For instance, `polymult((2,1), (3,5,1))` is `(6,13,7,1)` (the product of $2+x$ and $3+5x+x^2$ is $6+13x+7x^2+x^3$).

`polydiv(`c_1`,` c_2`,` c_q`,` c_r`)` calculates polynomial c_1/c_2, storing the quotient polynomial in c_q and the remainder polynomial in c_r. For instance, `polydiv((3,5,1), (2,1),` c_q`,` c_r`)` returns c_q`=(3,1)` and c_r`=(-3)`; that is,

$$\frac{3+5x+x^2}{2+x} = 3+x \text{ with a remainder of } -3$$

or

$$3+5x+x^2 = (3+x)(2+x) - 3$$

`polyroots(`c`)` find the roots of polynomial c and returns them in complex row vector (complex even if c is real). For instance, `polyroots((3,5,1))` returns `(-4.303+0i, -.697+0i)` (the roots of $3+5x+x^2$ are -4.303 and $-.697$).

Syntax

numeric vector	`polyeval(`*numeric rowvector* c`,` *numeric vector* x`)`
numeric rowvector	`polysolve(`*numeric vector* y`,` *numeric vector* x`)`
numeric rowvector	`polytrim(`*numeric vector* c`)`
numeric rowvector	`polyderiv(`*numeric rowvector* c`,` *real scalar* i`)`
numeric rowvector	`polyinteg(`*numeric rowvector* c`,` *real scalar* i`)`
numeric rowvector	`polyadd(`*numeric rowvector* c_1`,` *numeric rowvector* c_2`)`
numeric rowvector	`polymult(`*numeric rowvector* c_1`,` *numeric rowvector* c_2`)`
void	`polydiv(`*numeric rowvector* c_1`,` *numeric rowvector* c_2`,` c_q`,` c_r`)`
complex rowvector	`polyroots(`*numeric rowvector* c`)`

In the above, row vector c contains the coefficients for a `cols(`c`)` -1 degree polynomial. For instance,

$$c = (4, 2, 1)$$

records the polynomial

$$4 + 2x + x^2$$

Remarks and examples

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Given the real or complex coefficients c that define an $n-1$ degree polynomial in x, `polyroots(`c`)` returns the $n-1$ roots for which

$$0 = c_1 + c_2x^1 + c_3x^2 + \cdots + c_nx^{n-1}$$

`polyroots(`c`)` obtains the roots by calculating the eigenvalues of the companion matrix. The $(n-1) \times (n-1)$ companion matrix for the polynomial defined by c is

$$C = \begin{bmatrix} -c_{n-1}s & -c_{n-2}s & \cdots & -c_2s & -c_1s \\ 1 & 0 & \cdots & 0 & 0 \\ 0 & 1 & \cdots & 0 & 0 \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ 0 & 0 & \cdots & 1 & 0 \\ 0 & 0 & \cdots & 0 & 1 \end{bmatrix}$$

where $s = 1/c_n$ if c is real and

$$s = C\left(\frac{\mathrm{Re}(c_n)}{\mathrm{Re}(c_n)^2 + \mathrm{Im}(c_n)^2}, \frac{-\mathrm{Im}(c_n)}{\mathrm{Re}(c_n)^2 + \mathrm{Im}(c_n)^2}\right)$$

otherwise.

As in all nonsymmetric eigenvalue problems, the returned roots are complex and sorted from largest to smallest, see [M-5] **eigensystem( )**.

Conformability

`polyeval(`c`,` x`)`:

c:	$1 \times n$, $n > 0$		
x:	$r \times 1$	or	$1 \times c$
result:	$r \times 1$	or	$1 \times c$

`polysolve(`y`,` x`)`:

y:	$n \times 1$	or	$1 \times n$, $n \geq 1$
x:	$n \times 1$	or	$1 \times n$
result:	$1 \times k$,	$1 \leq k \leq n$	

`polytrim(`c`)`:

c:	$1 \times n$
result:	$1 \times k$, $1 \leq k \leq n$

`polyderiv(`c`,` i`)`:

c:	$1 \times n$, $n > 0$
i:	1×1, i may be negative
result:	$1 \times \max(1, n - i)$

`polyinteg(`c`,` i`)`:

c:	$1 \times n$, $n > 0$
i:	1×1, i may be negative
result:	$1 \times \max(1, n + i)$

`polyadd(`c_1`,` c_2`)`:

c_1:	$1 \times n_1$, $n_1 > 0$
c_2:	$1 \times n_2$, $n_2 > 0$
result:	$1 \times \max(n_1, n_2)$

`polymult(`c_1`,` c_2`)`:

c_1:	$1 \times n_1$, $n_1 > 0$
c_2:	$1 \times n_2$, $n_2 > 0$
result:	$1 \times n_1 + n_2 - 1$

`polydiv(`c_1`,` c_2`,` c_q`,` c_r`)`:

input:	
c_1:	$1 \times n_1$, $n_1 > 0$
c_2:	$1 \times n_2$, $n_2 > 0$
output:	
c_q:	$1 \times k_1$, $1 \leq k_1 \leq \max(n_1 - n_2 + 1, 1)$
c_r:	$1 \times k_2$, $1 \leq k_2 \leq \max(n_1 - n_2, 1)$

`polyroots(`c`)`:

c:	$1 \times n_i$, $n > 0$
result:	$1 \times k - 1$, $k =$ `cols(polytrim(`c`))`

Diagnostics

All functions abort with an error if a polynomial coefficient row vector is void, but they do not necessarily give indicative error messages as to the problem. Polynomial coefficient row vectors may contain missing values.

`polyderiv(`c`, `i`)` returns c when $i = 0$. It returns `polyinteg(`c`, `$-i$`)` when $i < 0$. It returns `(0)` when i is missing (think of missing as positive infinity).

`polyinteg(`c`, `i`)` returns c when $i = 0$. It returns `polyderiv(`c`, `$-i$`)` when $i < 0$. It aborts with error if i is missing (think of missing as positive infinity).

`polyroots(`c`)` returns a vector of missing values if any element of c equals missing.

Also see

[M-4] **mathematical** — Important mathematical functions