

minindex() — Indices of minimums and maximums

Description	Syntax	Remarks and examples	Conformability
Diagnostics	Also see		

Description

`minindex(v, k, i, w)` returns in i and w the indices of the k minimums of v .

`maxindex(v, k, i, w)` does the same, except that it returns the indices of the k maximums.

`minindex()` may be called with $k < 0$; it is then equivalent to `maxindex()`.

`maxindex()` may be called with $k < 0$; it is then equivalent to `minindex()`.

Syntax

void minindex(real vector v, real scalar k, i, w)

void maxindex(real vector v, real scalar k, i, w)

Results are returned in i and w .

i will be a *real colvector*.

w will be a $K \times 2$ *real matrix*, $K \leq |k|$.

Remarks and examples

Remarks are presented under the following headings:

Use of functions when v has all unique values
Use of functions when v has repeated (tied) values
Summary

Remarks are cast in terms of `minindex()` but apply equally to `maxindex()`.

Use of functions when v has all unique values

Consider $v = (3, 1, 5, 7, 6)$.

1. `minindex(v, 1, i, w)` returns $i = 2$, which means that $v[2]$ is the minimum value in v .
2. `minindex(v, 2, i, w)` returns $i = (2, 1)'$, which means that $v[2]$ is the minimum value of v and that $v[1]$ is the second minimum.

...

5. `minindex(v, 5, i, w)` returns $i = (2, 1, 3, 5, 4)'$, which means that the ordered values in v are $v[2]$, $v[1]$, $v[3]$, $v[5]$, and $v[4]$.

6. `minindex(v, 6, i, w)`, `minindex(v, 7, i, w)`, and so on, return the same as (5), because there are only five minimums in a five-element vector.

When v has unique values, the values returned in w are irrelevant.

- In (1), w will be (1, 1).
- In (2), w will be (1, 1\2, 1).
- ...
- In (5), w will be (1, 1\2, 1\3, 1\4, 1\5, 1).

The second column of w records the number of tied values. Since the values in v are unique, the second column of w will be ones. If you have a problem where you are uncertain whether the values in v are unique, code

```
if (!allOf(w[,2], 1)) {  
    /* uniqueness assumption false */  
}
```

Use of functions when v has repeated (tied) values

Consider $v = (3, 2, 3, 2, 3, 3)$.

1. `minindex(v, 1, i, w)` returns $i = (2, 4)'$, which means that there is one minimum value and that it is repeated in two elements of v , namely, $v[2]$ and $v[4]$.

Here, w will be (1, 2), but you can ignore that. There are two values in i corresponding to the same minimum.

When $k=1$, `rows(i)` equals the number of observations in v corresponding to the minimum, as does $w[1, 2]$.

2. `minindex(v, 2, i, w)` returns $i = (2, 4, 1, 3, 5, 6)'$ and $w = (1, 2\3, 4)$.

Begin with w . The first row of w is (1, 2), which states that the indices of the first minimums of v start at $i[1]$ and consist of two elements. Thus the indices of the first minimums are $i[1]$ and $i[2]$ (the minimums are $v[i[1]]$ and $v[i[2]]$, which of course are equal).

The second row of w is (3, 4), which states that the indices of the second minimums of v start at $i[3]$ and consist of four elements: $i[3]$, $i[4]$, $i[5]$, and $i[6]$ (which are 1, 3, 5, and 6).

In summary, `rows(w)` records the number of minimums returned. $w[m, 1]$ records where in i the m th minimum begins (it begins at $i[w[m, 1]]$). $w[m, 2]$ records the total number of tied values. Thus one could step across the minimums and the tied values by coding

```
minindex(v, k, i, w)  
for (m=1; m<=rows(w); m++) {  
    for (j=w[m,1]; j<w[m,1]+w[m,2]; j++) {  
        /* i[j] is the index in v of an mth minimum */  
    }  
}
```

3. `minindex(v, 3, i, w)`, `minindex(v, 4, i, w)`, and so on, return the same as (2) because, with $v = (3, 2, 3, 2, 3, 3)$, there are only two minimums.

Summary

Consider `minindex(v, k, i, w)`. Returned will be

$$w = \begin{bmatrix} i1 & n1 \\ i2 & n2 \\ \cdot & \cdot \\ \cdot & \cdot \end{bmatrix} \quad w: K \times 2, \quad K \leq |k|$$

$$i = \begin{bmatrix} j1 \\ j2 \\ j3 \\ j4 \\ \cdot \\ \cdot \\ \cdot \end{bmatrix} \quad \left. \begin{array}{l} \leftarrow i[i1] \text{ is start of first minimums} \\ \leftarrow i[i2] \text{ is start of second minimums} \\ \text{etc.} \end{array} \right\} \begin{array}{l} \text{has } n1 \text{ values} \\ \text{has } n2 \text{ values} \end{array}$$

$$i: 1 \times m, \quad m = n1 + n2 + \dots$$

$j1, j2, \dots$, are indices into v .

Conformability

`minindex(v, k, i, w)`, `maxindex(v, k, i, w)`:

input:

$$\begin{array}{ll} v: & n \times 1 \text{ or } 1 \times n \\ k: & 1 \times 1 \end{array}$$

output:

$$\begin{array}{ll} i: & L \times 1, \quad L \geq K \\ w: & K \times 2, \quad K \leq |k| \end{array}$$

Diagnostics

`minindex(v, k, i, w)` and `maxindex(v, k, i, w)` abort with error if i or w is a view.

In `minindex(v, k, i, w)` and `maxindex(v, k, i, w)`, missing values in v are ignored in obtaining minimums and maximums.

In the examples above, we have shown input vector v as a row vector. It can also be a column vector; it makes no difference.

In `minindex(v, k, i, w)`, input argument k specifies the number of minimums to be obtained. k may be zero. If k is negative, $-k$ maximums are obtained.

Similarly, in `maxindex(v, k, i, w)`, input argument k specifies the number of maximums to be obtained. k may be zero. If k is negative, $-k$ minimums are obtained.

`minindex()` and `maxindex()` are designed for use when k is small relative to `length(v)`; otherwise, see `order()` in [M-5] `sort()`.

Also see

[M-5] [minmax\(\)](#) — Minimums and maximums

[M-4] [utility](#) — Matrix utility functions