

tpoisson — Truncated Poisson regression

Syntax	Menu	Description	Options
Remarks and examples	Stored results	Methods and formulas	Acknowledgment
References	Also see		

Syntax

```
tpoisson depvar [indepvars] [if] [in] [weight] [, options]
```

<i>options</i>	Description
Model	
<u>noconstant</u>	suppress constant term
<u>ll</u> (# <i>varname</i>)	truncation point; default value is ll(0), zero truncation
<u>exposure</u> (<i>varname_e</i>)	include ln(<i>varname_e</i>) in model with coefficient constrained to 1
<u>offset</u> (<i>varname_o</i>)	include <i>varname_o</i> in model with coefficient constrained to 1
<u>constraints</u> (<i>constraints</i>)	apply specified linear constraints
<u>collinear</u>	keep collinear variables
SE/Robust	
<u>vce</u> (<i>vcetype</i>)	<i>vcetype</i> may be oim, <u>robust</u> , <u>cluster</u> <i>clustvar</i> , opg, <u>bootstrap</u> , or <u>jackknife</u>
Reporting	
<u>level</u> (#)	set confidence level; default is level(95)
<u>irr</u>	report incidence-rate ratios
<u>nocnsreport</u>	do not display constraints
<u>display_options</u>	control column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling
Maximization	
<u>maximize_options</u>	control the maximization process; seldom used
<u>coeflegend</u>	display legend instead of statistics

indepvars may contain factor variables; see [U] 11.4.3 Factor variables.

depvar and *indepvars* may contain time-series operators; see [U] 11.4.4 Time-series varlists.

bootstrap, by, fp, jackknife, rolling, statsby, and svy are allowed; see [U] 11.1.10 Prefix commands.

Weights are not allowed with the bootstrap prefix; see [R] bootstrap.

vce() and weights are not allowed with the svy prefix; see [SVY] svy.

fweights, iweights, and pweights are allowed; see [U] 11.1.6 weight.

coeflegend does not appear in the dialog box.

See [U] 20 Estimation and postestimation commands for more capabilities of estimation commands.

Menu

Statistics > Count outcomes > Truncated Poisson regression

Description

`tpoisson` estimates the parameters of a truncated Poisson model by maximum likelihood. The dependent variable *devar* is regressed on *indepvars*, where *devar* is a positive count variable whose values are all above the truncation point.

Options

Model

`noconstant`; see [R] [estimation options](#).

`ll(# | varname)` specifies the truncation point, which is a nonnegative integer. The default is zero truncation, `ll(0)`.

`exposure(varnamee)`, `offset(varnameo)`, `constraints(constraints)`, `collinear`; see [R] [estimation options](#).

SE/Robust

`vce(vcetype)` specifies the type of standard error reported, which includes types that are derived from asymptotic theory (`oim`, `opg`), that are robust to some kinds of misspecification (`robust`), that allow for intragroup correlation (`cluster clustvar`), and that use bootstrap or jackknife methods (`bootstrap`, `jackknife`); see [R] [vce_option](#).

Reporting

`level(#)`; see [R] [estimation options](#).

`irr` reports estimated coefficients transformed to incidence-rate ratios, that is, e^{β_i} rather than β_i . Standard errors and confidence intervals are similarly transformed. This option affects how results are displayed, not how they are estimated. `irr` may be specified at estimation or when replaying previously estimated results.

`nocnsreport`; see [R] [estimation options](#).

`display_options`: `noomitted`, `vsquish`, `noemptycells`, `baselevels`, `allbaselevels`, `nofvlabel`, `fvwrap(#)`, `fvwrapon(style)`, `cformat(%fmt)`, `pformat(%fmt)`, `sformat(%fmt)`, and `nolstretch`; see [R] [estimation options](#).

Maximization

`maximize_options`: `difficult`, `technique(algorithm_spec)`, `iterate(#)`, `[no]log`, `trace`, `gradient`, `showstep`, `hessian`, `showtolerance`, `tolerance(#)`, `ltolerance(#)`, `nrtolerance(#)`, `nonrtolerance`, and `from(init_specs)`; see [R] [maximize](#). These options are seldom used.

Setting the optimization type to `technique(bhhh)` resets the default *vcetype* to `vce(opg)`.

The following option is available with `tpoisson` but is not shown in the dialog box:

`coeflegend`; see [R] [estimation options](#).

Remarks and examples

Truncated Poisson regression is used to model the number of occurrences of an event when that number is restricted to be above the truncation point. If the dependent variable is not truncated, standard Poisson regression may be more appropriate; see [R] [tpoisson](#). Truncated Poisson regression was first proposed by [Grogger and Carson \(1991\)](#). For an introduction to Poisson regression, see [Cameron and Trivedi \(2005, 2010\)](#) and [Long and Freese \(2014\)](#). For an introduction to truncated Poisson models, see [Cameron and Trivedi \(2013\)](#) and [Long \(1997, chap. 8\)](#).

Suppose that the patients admitted to a hospital for a given condition form a random sample from a population of interest and that each admitted patient stays at least one day. You are interested in modeling the length of stay of patients in days. The sample is truncated at zero because you only have data on individuals who stayed at least one day. `tpoisson` accounts for the truncated sample, whereas `poisson` does not.

Truncation is not the same as censoring. Right-censored Poisson regression was implemented in Stata by [Raciborski \(2011\)](#).

► Example 1

Consider the [Simonoff \(2003\)](#) dataset of running shoes for a sample of runners who registered an online running log. A running-shoe marketing executive is interested in knowing how the number of running shoes purchased relates to other factors such as gender, marital status, age, education, income, typical number of runs per week, average miles run per week, and the preferred type of running. These data are naturally truncated at zero. A truncated Poisson model is fit to the number of shoes owned on runs per week, miles run per week, gender, age, and marital status.

No options are needed because zero truncation is the default for `tpoisson`.

```
. use http://www.stata-press.com/data/r13/runshoes
. tpoisson shoes rpweek mpweek male age married
Iteration 0:  log likelihood = -88.328151
Iteration 1:  log likelihood = -86.272639
Iteration 2:  log likelihood = -86.257999
Iteration 3:  log likelihood = -86.257994

Truncated Poisson regression          Number of obs   =          60
Truncation point: 0                   LR chi2(5)      =         22.75
                                       Prob > chi2     =         0.0004
Log likelihood = -86.257994           Pseudo R2      =         0.1165
```

shoes	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
rpweek	.1575811	.1097893	1.44	0.151	-.057602	.3727641
mpweek	.0210673	.0091113	2.31	0.021	.0032094	.0389252
male	.0446134	.2444626	0.18	0.855	-.4345246	.5237513
age	.0185565	.0137786	1.35	0.178	-.008449	.045562
married	-.1283912	.2785044	-0.46	0.645	-.6742498	.4174674
_cons	-1.205844	.6619774	-1.82	0.069	-2.503296	.0916078

Using the zero-truncated Poisson regression with these data, only the coefficient on average miles per week is statistically significant at the 5% level.

▷ Example 2

Semiconductor manufacturing requires that silicon wafers be coated with a layer of metal oxide. The depth of this layer is strictly controlled. In this example, a critical oxide layer is designed for 300 ± 20 angstroms (\AA).

After the oxide layer is coated onto a wafer, the wafer enters a photolithography step in which the lines representing the electrical connections are printed on the oxide and later etched and filled with metal. The widths of these lines are measured. In this example, they are controlled to 90 ± 5 micrometers (μm).

After these and other steps, each wafer is electrically tested at probe. If too many failures are discovered, the wafer is rejected and sent for engineering analysis. In this example, the maximum number of probe failures tolerated for this product is 10.

A major failure at probe has been encountered—88 wafers had more than 10 failures each. The 88 wafers that failed were tested using 4 probe machines. The engineer suspects that the failures were a result of faulty probe machines, poor depth control, or poor line widths. The line widths and depths in these data are the actual measurement minus its specification target, 300 \AA for the oxide depths and $90 \mu\text{m}$ for the line widths.

The following table tabulates the average failure rate for each probe using Stata's mean command; see [R] mean.

```
. use http://www.stata-press.com/data/r13/probe
. mean failures, over(probe) nolegend
```

```
Mean estimation      Number of obs      =      88
```

	Over	Mean	Std. Err.	[95% Conf. Interval]
failures				
	1	15.875	1.186293	13.51711 18.23289
	2	14.95833	.5912379	13.78318 16.13348
	3	16.47059	.9279866	14.62611 18.31506
	4	23.09677	.9451117	21.21826 24.97529

The 95% confidence intervals in this table suggest that there are about 5–11 additional failures per wafer on probe 4. These are unadjusted for varying line widths and oxide depths. Possibly, probe 4 received the wafers with larger line widths or extreme oxide depths.

Truncated Poisson regression more clearly identifies the root causes for the increased failures by estimating the differences between probes adjusted for the line widths and oxide depths. It also allows us to determine whether the deviations from specifications in line widths or oxide depths might be contributing to the problem.

```
. tpoisson failures i.probe depth width, ll(10) nolog
Truncated Poisson regression          Number of obs   =          88
Truncation point: 10                  LR chi2(5)      =         73.70
Log likelihood = -239.35746            Prob > chi2     =          0.0000
                                       Pseudo R2       =          0.1334
```

failures	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
probe						
2	-.1113037	.1019786	-1.09	0.275	-.3111781	.0885707
3	.0114339	.1036032	0.11	0.912	-.1916245	.2144924
4	.4254115	.0841277	5.06	0.000	.2605242	.5902989
depth						
width	-.0005034	.0033375	-0.15	0.880	-.0070447	.006038
_cons	.0330225	.015573	2.12	0.034	.0025001	.063545
	2.714025	.0752617	36.06	0.000	2.566515	2.861536

The coefficients listed for the probes are testing the null hypothesis: $H_0: \text{probe}_i = \text{probe}_1$, where i equals 2, 3, and 4. Because the only coefficient that is statistically significant is the one for testing for $H_0: \text{probe}_4 = \text{probe}_1$, $p < 0.001$, and because the p -values for the other probes are not statistically significant, that is, $p \geq 0.275$, the implication is that there is a difference between probe 4 and the other machines. Because the coefficient for this test is positive, 0.425, the conclusion is that the average failure rate for probe 4, after adjusting for line widths and oxide depths, is higher than the other probes. Possibly, probe 4 needs calibration or the head used with this machine is defective.

Line-width control is statistically significant, $p = 0.034$, but variation in oxide depths is not causing the increased failure rate. The engineer concluded that the sudden increase in failures is the result of two problems. First, probe 4 is malfunctioning, and second, there is a possible lithography or etching problem.

Stored results

tpoisson stores the following in `e()`:

Scalars

<code>e(N)</code>	number of observations
<code>e(k)</code>	number of parameters
<code>e(k_eq)</code>	number of equations in <code>e(b)</code>
<code>e(k_eq_model)</code>	number of equations in overall model test
<code>e(k_dv)</code>	number of dependent variables
<code>e(df_m)</code>	model degrees of freedom
<code>e(r2_p)</code>	pseudo- <i>R</i> -squared
<code>e(ll)</code>	log likelihood
<code>e(ll_0)</code>	log likelihood, constant-only model
<code>e(N_clust)</code>	number of clusters
<code>e(chi2)</code>	χ^2
<code>e(p)</code>	significance
<code>e(rank)</code>	rank of <code>e(V)</code>
<code>e(ic)</code>	number of iterations
<code>e(rc)</code>	return code
<code>e(converged)</code>	1 if converged, 0 otherwise

Macros

<code>e(cmd)</code>	tpoisson
<code>e(cmdline)</code>	command as typed
<code>e(depvar)</code>	name of dependent variable
<code>e(llopt)</code>	contents of <code>ll()</code> , or 0 if not specified
<code>e(wtype)</code>	weight type
<code>e(wexp)</code>	weight expression
<code>e(title)</code>	title in estimation output
<code>e(clustvar)</code>	name of cluster variable
<code>e(offset)</code>	linear offset variable
<code>e(chi2type)</code>	Wald or LR; type of model χ^2 test
<code>e(vce)</code>	<i>vce</i> type specified in <code>vce()</code>
<code>e(vcetype)</code>	title used to label Std. Err.
<code>e(opt)</code>	type of optimization
<code>e(which)</code>	max or min; whether optimizer is to perform maximization or minimization
<code>e(ml_method)</code>	type of ml method
<code>e(user)</code>	name of likelihood-evaluator program
<code>e(technique)</code>	maximization technique
<code>e(properties)</code>	<code>b V</code>
<code>e(predict)</code>	program used to implement <code>predict</code>
<code>e(asbalanced)</code>	factor variables <code>fvset</code> as <code>asbalanced</code>
<code>e(asobserved)</code>	factor variables <code>fvset</code> as <code>asobserved</code>

Matrices

<code>e(b)</code>	coefficient vector
<code>e(Cns)</code>	constraints matrix
<code>e(ilog)</code>	iteration log (up to 20 iterations)
<code>e(gradient)</code>	gradient vector
<code>e(V)</code>	variance-covariance matrix of the estimators
<code>e(V_modelbased)</code>	model-based variance

Functions

<code>e(sample)</code>	marks estimation sample
------------------------	-------------------------

Methods and formulas

The conditional probability of observing y_j events given that $y_j > \tau_j$, where τ_j is the truncation point, is given by

$$\Pr(Y = y_j | y_j > \tau_j, \mathbf{x}_j) = \frac{\exp(-\lambda)\lambda^{y_j}}{y_j! \Pr(Y > \tau_j | \mathbf{x}_j)}$$

The log likelihood (with weights w_j and offsets) is given by

$$\begin{aligned} \xi_j &= \mathbf{x}_j \boldsymbol{\beta} + \text{offset}_j \\ f(y_j) &= \frac{\exp\{-\exp(\xi_j)\} \exp(\xi_j y_j)}{y_j! \Pr(Y > \tau_j | \xi_j)} \\ \ln L &= \sum_{j=1}^n w_j [-\exp(\xi_j) + \xi_j y_j - \ln(y_j!) - \ln\{\Pr(Y > \tau_j | \xi_j)\}] \end{aligned}$$

This command supports the Huber/White/sandwich estimator of the variance and its clustered version using `vce(robust)` and `vce(cluster clustvar)`, respectively. See [P] [_robust](#), particularly [Maximum likelihood estimators](#) and [Methods and formulas](#).

`tppoisson` also supports estimation with survey data. For details on variance–covariance estimates with survey data, see [SVY] [variance estimation](#).

Acknowledgment

We gratefully acknowledge the previous work by Joseph Hilbe (1999) at Arizona State University and past editor of the *Stata Technical Bulletin* and coauthor of the Stata Press book *Generalized Linear Models and Extensions*.

References

- Cameron, A. C., and P. K. Trivedi. 2005. *Microeconometrics: Methods and Applications*. New York: Cambridge University Press.
- . 2010. *Microeconometrics Using Stata*. Rev. ed. College Station, TX: Stata Press.
- . 2013. *Regression Analysis of Count Data*. 2nd ed. New York: Cambridge University Press.
- Farbmacher, H. 2011. Estimation of hurdle models for overdispersed count data. *Stata Journal* 11: 82–94.
- Grogger, J. T., and R. T. Carson. 1991. Models for truncated counts. *Journal of Applied Econometrics* 6: 225–238.
- Hilbe, J. M. 1998. [sg91: Robust variance estimators for MLE Poisson and negative binomial regression](#). *Stata Technical Bulletin* 45: 26–28. Reprinted in *Stata Technical Bulletin Reprints*, vol. 8, pp. 177–180. College Station, TX: Stata Press.
- . 1999. [sg102: Zero-truncated Poisson and negative binomial regression](#). *Stata Technical Bulletin* 47: 37–40. Reprinted in *Stata Technical Bulletin Reprints*, vol. 8, pp. 233–236. College Station, TX: Stata Press.
- Hilbe, J. M., and D. H. Judson. 1998. [sg94: Right, left, and uncensored Poisson regression](#). *Stata Technical Bulletin* 46: 18–20. Reprinted in *Stata Technical Bulletin Reprints*, vol. 8, pp. 186–189. College Station, TX: Stata Press.
- Long, J. S. 1997. *Regression Models for Categorical and Limited Dependent Variables*. Thousand Oaks, CA: Sage.
- Long, J. S., and J. Freese. 2014. *Regression Models for Categorical Dependent Variables Using Stata*. 3rd ed. College Station, TX: Stata Press.
- Raciborski, R. 2011. [Right-censored Poisson regression model](#). *Stata Journal* 11: 95–105.
- Simonoff, J. S. 2003. *Analyzing Categorical Data*. New York: Springer.

Also see

[R] **tpoisson postestimation** — Postestimation tools for tpoisson

[R] **poisson** — Poisson regression

[R] **nbreg** — Negative binomial regression

[R] **tnbreg** — Truncated negative binomial regression

[R] **zinb** — Zero-inflated negative binomial regression

[R] **zip** — Zero-inflated Poisson regression

[SVY] **svy estimation** — Estimation commands for survey data

[XT] **xtpoisson** — Fixed-effects, random-effects, and population-averaged Poisson models

[U] **20 Estimation and postestimation commands**