

meologit — Multilevel mixed-effects ordered logistic regression
[Syntax](#)[Remarks and examples](#)[Also see](#)[Menu](#)[Stored results](#)[Description](#)[Methods and formulas](#)[Options](#)[References](#)

Syntax

```
meologit depvar fe_equation [ || re_equation ] [ || re_equation ... ] [ , options ]
```

where the syntax of *fe_equation* is

```
[ indepvars ] [ if ] [ in ] [ , fe_options ]
```

and the syntax of *re_equation* is one of the following:

for random coefficients and intercepts

```
levelvar: [ varlist ] [ , re_options ]
```

for random effects among the values of a factor variable

```
levelvar: R.varname
```

levelvar is a variable identifying the group structure for the random effects at that level or is `_all` representing one group comprising all observations.

<i>fe_options</i>	Description
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Model	<u>offset</u> (<i>varname</i>)	include <i>varname</i> in model with coefficient constrained to 1
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<i>re_options</i>	Description
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Model	<u>covariance</u> (<i>vartype</i>)	variance–covariance structure of the random effects
	<u>noconstant</u>	suppress constant term from the random-effects equation

<i>options</i>	Description
Model	
<u>constraints</u> (<i>constraints</i>)	apply specified linear constraints
<u>collinear</u>	keep collinear variables
SE/Robust	
<u>vce</u> (<i>vcetype</i>)	<i>vcetype</i> may be <code>oim</code> , <code>robust</code> , or <code>cluster clustvar</code>
Reporting	
<u>level</u> (#)	set confidence level; default is <code>level(95)</code>
or	report fixed-effects coefficients as odds ratios
<u>nocnsreport</u>	do not display constraints
<u>notable</u>	suppress coefficient table
<u>noheader</u>	suppress output header
<u>nogroup</u>	suppress table summarizing groups
<u>nolrtest</u>	do not perform likelihood-ratio test comparing with ordered logistic regression
<i>display_options</i>	control column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling
Integration	
<u>intmethod</u> (<i>intmethod</i>)	integration method
<u>intpoints</u> (#)	set the number of integration (quadrature) points for all levels; default is <code>intpoints(7)</code>
Maximization	
<i>maximize_options</i>	control the maximization process; seldom used
<u>startvalues</u> (<i>svmethod</i>)	method for obtaining starting values
<u>startgrid</u> [(<i>gridspec</i>)]	perform a grid search to improve starting values
<u>noestimate</u>	do not fit the model; show starting values instead
<u>dnnumerical</u>	use numerical derivative techniques
<u>coeflegend</u>	display legend instead of statistics

<i>vartype</i>	Description
<u>independent</u>	one unique variance parameter per random effect, all covariances 0; the default unless the <code>R.</code> notation is used
<u>exchangeable</u>	equal variances for random effects, and one common pairwise covariance
<u>identity</u>	equal variances for random effects, all covariances 0; the default if the <code>R.</code> notation is used
<u>unstructured</u>	all variances and covariances to be distinctly estimated
<u>fixed</u> (<i>matname</i>)	user-selected variances and covariances constrained to specified values; the remaining variances and covariances unrestricted
<u>pattern</u> (<i>matname</i>)	user-selected variances and covariances constrained to be equal; the remaining variances and covariances unrestricted

<i>intmethod</i>	Description
<u>m</u> vaghermite	mean-variance adaptive Gauss–Hermite quadrature; the default unless a crossed random-effects model is fit
<u>m</u> caghermite	mode-curvature adaptive Gauss–Hermite quadrature
<u>g</u> hermite	nonadaptive Gauss–Hermite quadrature
<u>l</u> aplace	Laplacian approximation; the default for crossed random-effects models

indepvars may contain factor variables; see [U] 11.4.3 Factor variables.

depvar, *indepvars*, and *varlist* may contain time-series operators; see [U] 11.4.4 Time-series varlists.

by is allowed; see [U] 11.1.10 Prefix commands.

startvalues(), *startgrid*, *noestimate*, *dnumerical*, and *coeflegend* do not appear in the dialog box.

See [U] 20 Estimation and postestimation commands for more capabilities of estimation commands.

Menu

Statistics > Multilevel mixed-effects models > Ordered logistic regression

Description

meologit fits mixed-effects logistic models for ordered responses. The actual values taken on by the response are irrelevant except that larger values are assumed to correspond to “higher” outcomes. The conditional distribution of the response given the random effects is assumed to be multinomial, with success probability determined by the logistic cumulative distribution function.

Options

Model

offset(*varname*) specifies that *varname* be included in the fixed-effects portion of the model with the coefficient constrained to be 1.

covariance(*vartype*) specifies the structure of the covariance matrix for the random effects and may be specified for each random-effects equation. *vartype* is one of the following: *independent*, *exchangeable*, *identity*, *unstructured*, *fixed*(*matname*), or *pattern*(*matname*).

covariance(*independent*) covariance structure allows for a distinct variance for each random effect within a random-effects equation and assumes that all covariances are 0. The default is *covariance*(*independent*) unless a crossed random-effects model is fit, in which case the default is *covariance*(*identity*).

covariance(*exchangeable*) structure specifies one common variance for all random effects and one common pairwise covariance.

covariance(*identity*) is short for “multiple of the identity”; that is, all variances are equal and all covariances are 0.

covariance(*unstructured*) allows for all variances and covariances to be distinct. If an equation consists of p random-effects terms, the unstructured covariance matrix will have $p(p + 1)/2$ unique parameters.

`covariance(fixed(matname))` and `covariance(pattern(matname))` covariance structures provide a convenient way to impose constraints on variances and covariances of random effects. Each specification requires a *matname* that defines the restrictions placed on variances and covariances. Only elements in the lower triangle of *matname* are used, and row and column names of *matname* are ignored. A missing value in *matname* means that a given element is unrestricted. In a `fixed(matname)` covariance structure, (co)variance (*i, j*) is constrained to equal the value specified in the *i, j*th entry of *matname*. In a `pattern(matname)` covariance structure, (co)variances (*i, j*) and (*k, l*) are constrained to be equal if *matname*[*i, j*] = *matname*[*k, l*].

`noconstant` suppresses the constant (intercept) term; may be specified for any or all of the random-effects equations.

`constraints(constraints)`, `collinear`; see [R] [estimation options](#).

SE/Robust

`vce(vcetype)` specifies the type of standard error reported, which includes types that are derived from asymptotic theory (`oim`), that are robust to some kinds of misspecification (`robust`), and that allow for intragroup correlation (`cluster clustvar`); see [R] [vce_option](#). If `vce(robust)` is specified, robust variances are clustered at the highest level in the multilevel model.

Reporting

`level(#)`; see [R] [estimation options](#).

`or` reports estimated fixed-effects coefficients transformed to odds ratios, that is, $\exp(\beta)$ rather than β . Standard errors and confidence intervals are similarly transformed. This option affects how results are displayed, not how they are estimated. `or` may be specified either at estimation or upon replay.

`nocnsreport`; see [R] [estimation options](#).

`notable` suppresses the estimation table, either at estimation or upon replay.

`noheader` suppresses the output header, either at estimation or upon replay.

`nogroup` suppresses the display of group summary information (number of groups, average group size, minimum, and maximum) from the output header.

`nolrtest` prevents `meologit` from performing a likelihood-ratio test that compares the mixed-effects ordered logistic model with standard (marginal) ordered logistic regression. This option may also be specified upon replay to suppress this test from the output.

display_options: `noomitted`, `vsquish`, `noemptycells`, `baselevels`, `allbaselevels`, `nofvlabel`, `fvwrap(#)`, `fvwrapon(style)`, `cformat(%fmt)`, `pformat(%fmt)`, `sformat(%fmt)`, and `nolstretch`; see [R] [estimation options](#).

Integration

`intmethod(intmethod)` specifies the integration method to be used for the random-effects model. `mvaghermite` performs mean and variance adaptive Gauss–Hermite quadrature; `mcaghermite` performs mode and curvature adaptive Gauss–Hermite quadrature; `ghermite` performs nonadaptive Gauss–Hermite quadrature; and `laplace` performs the Laplacian approximation, equivalent to mode curvature adaptive Gaussian quadrature with one integration point.

The default integration method is `mvaghermite` unless a crossed random-effects model is fit, in which case the default integration method is `laplace`. The Laplacian approximation has been known to produce biased parameter estimates; however, the bias tends to be more prominent in the estimates of the variance components rather than in the estimates of the fixed effects.

For crossed random-effects models, estimation with more than one quadrature point may be prohibitively intensive even for a small number of levels. For this reason, the integration method defaults to the Laplacian approximation. You may override this behavior by specifying a different integration method.

`intpoints(#)` sets the number of integration points for quadrature. The default is `intpoints(7)`, which means that seven quadrature points are used for each level of random effects. This option is not allowed with `intmethod(laplace)`.

The more integration points, the more accurate the approximation to the log likelihood. However, computation time increases as a function of the number of quadrature points raised to a power equaling the dimension of the random-effects specification. In crossed random-effects models and in models with many levels or many random coefficients, this increase can be substantial.

Maximization

`maximize_options`: `difficult`, `technique(algorithm_spec)`, `iterate(#)`, `[no]log`, `trace`, `gradient`, `showstep`, `hessian`, `showtolerance`, `tolerance(#)`, `ltolerance(#)`, `nrtolerance(#)`, `nonrtolerance`, and `from(init_specs)`; see [R] [maximize](#). Those that require special mention for `meologit` are listed below.

`from()` accepts a properly labeled vector of initial values or a list of coefficient names with values. A list of values is not allowed.

The following options are available with `meologit` but are not shown in the dialog box:

`startvalues(svmethod)`, `startgrid[(gridspec)]`, `noestimate`, and `dnumerical`; see [ME] [meglm](#).

`coeflegend`; see [R] [estimation options](#).

Remarks and examples

[stata.com](#)

For a general introduction to `me` commands, see [ME] [me](#).

`meologit` is a convenience command for `meglm` with a `logit` link and an `ordinal` family; see [ME] [meglm](#).

Remarks are presented under the following headings:

Introduction

Two-level models

Three-level models

Introduction

Mixed-effects ordered logistic regression is ordered logistic regression containing both fixed effects and random effects. An ordered response is a variable that is categorical and ordered, for instance, “poor”, “good”, and “excellent”, which might indicate a person’s current health status or the repair record of a car. In the absence of random effects, mixed-effects ordered logistic regression reduces to ordered logistic regression; see [R] [ologit](#).

Comprehensive treatments of mixed models are provided by, for example, Searle, Casella, and McCulloch (1992); Verbeke and Molenberghs (2000); Raudenbush and Bryk (2002); Demidenko (2004); Hedeker and Gibbons (2006); McCulloch, Searle, and Neuhaus (2008); and Rabe-Hesketh and Skrondal (2012). Agresti (2010, chap. 10) and Rabe-Hesketh and Skrondal (2012, chap. 11) are good introductory readings on applied multilevel modeling of ordinal data.

meologit allows for many levels of nested clusters of random effects. For example, in a three-level model you can specify random effects for schools and then random effects for classes nested within schools. In this model, the observations (presumably, the students) comprise the first level, the classes comprise the second level, and the schools comprise the third.

However, for simplicity, for now we consider the two-level model, where for a series of M independent clusters, and conditional on a set of fixed effects \mathbf{x}_{ij} , a set of cutpoints $\boldsymbol{\kappa}$, and a set of random effects \mathbf{u}_j , the cumulative probability of the response being in a category higher than k is

$$\Pr(y_{ij} > k | \mathbf{x}_{ij}, \boldsymbol{\kappa}, \mathbf{u}_j) = H(\mathbf{x}_{ij}\boldsymbol{\beta} + \mathbf{z}_{ij}\mathbf{u}_j - \kappa_k) \quad (1)$$

for $j = 1, \dots, M$ clusters, with cluster j consisting of $i = 1, \dots, n_j$ observations. The cutpoints $\boldsymbol{\kappa}$ are labeled $\kappa_1, \kappa_2, \dots, \kappa_{K-1}$, where K is the number of possible outcomes. $H(\cdot)$ is the logistic cumulative distribution function that represents cumulative probability.

The $1 \times p$ row vector \mathbf{x}_{ij} are the covariates for the fixed effects, analogous to the covariates you would find in a standard logistic regression model, with regression coefficients (fixed effects) $\boldsymbol{\beta}$. In our parameterization, \mathbf{x}_{ij} does not contain a constant term because its effect is absorbed into the cutpoints. For notational convenience here and throughout this manual entry, we suppress the dependence of y_{ij} on \mathbf{x}_{ij} .

The $1 \times q$ vector \mathbf{z}_{ij} are the covariates corresponding to the random effects and can be used to represent both random intercepts and random coefficients. For example, in a random-intercept model, \mathbf{z}_{ij} is simply the scalar 1. The random effects \mathbf{u}_j are M realizations from a multivariate normal distribution with mean $\mathbf{0}$ and $q \times q$ variance matrix $\boldsymbol{\Sigma}$. The random effects are not directly estimated as model parameters but are instead summarized according to the unique elements of $\boldsymbol{\Sigma}$, known as variance components. One special case of (1) places $\mathbf{z}_{ij} = \mathbf{x}_{ij}$, so that all covariate effects are essentially random and distributed as multivariate normal with mean $\boldsymbol{\beta}$ and variance $\boldsymbol{\Sigma}$.

From (1), we can derive the probability of observing outcome k as

$$\begin{aligned} \Pr(y_{ij} = k | \boldsymbol{\kappa}, \mathbf{u}_j) &= \Pr(\kappa_{k-1} < \mathbf{x}_{ij}\boldsymbol{\beta} + \mathbf{z}_{ij}\mathbf{u}_j + \epsilon_{ij} \leq \kappa_k) \\ &= \Pr(\kappa_{k-1} - \mathbf{x}_{ij}\boldsymbol{\beta} - \mathbf{z}_{ij}\mathbf{u}_j < \epsilon_{ij} \leq \kappa_k - \mathbf{x}_{ij}\boldsymbol{\beta} - \mathbf{z}_{ij}\mathbf{u}_j) \\ &= H(\kappa_k - \mathbf{x}_{ij}\boldsymbol{\beta} - \mathbf{z}_{ij}\mathbf{u}_j) - H(\kappa_{k-1} - \mathbf{x}_{ij}\boldsymbol{\beta} - \mathbf{z}_{ij}\mathbf{u}_j) \end{aligned}$$

where κ_0 is taken as $-\infty$ and κ_K is taken as $+\infty$.

From the above, we may also write the model in terms of a latent linear response, where observed ordinal responses y_{ij} are generated from the latent continuous responses, such that

$$y_{ij}^* = \mathbf{x}_{ij}\boldsymbol{\beta} + \mathbf{z}_{ij}\mathbf{u}_j + \epsilon_{ij}$$

and

$$y_{ij} = \begin{cases} 1 & \text{if } y_{ij}^* \leq \kappa_1 \\ 2 & \text{if } \kappa_1 < y_{ij}^* \leq \kappa_2 \\ \vdots & \\ K & \text{if } \kappa_{K-1} < y_{ij}^* \end{cases}$$

The errors ϵ_{ij} are distributed as logistic with mean 0 and variance $\pi^2/3$ and are independent of \mathbf{u}_j .

Model (1) is an example of a generalized linear mixed model (GLMM), which generalizes the linear mixed-effects (LME) model to non-Gaussian responses. You can fit LMES in Stata by using `mixed` and fit GLMMs by using `meglm`. Because of the relationship between LMES and GLMMs, there

is insight to be gained through examination of the linear mixed model. This is especially true for Stata users because the terminology, syntax, options, and output for fitting these types of models are nearly identical. See [ME] [mixed](#) and the references therein, particularly in the *Introduction*, for more information.

Log-likelihood calculations for fitting any generalized mixed-effects model require integrating out the random effects. One widely used modern method is to directly estimate the integral required to calculate the log likelihood by Gauss–Hermite quadrature or some variation thereof. Because the log likelihood itself is estimated, this method has the advantage of permitting likelihood-ratio tests for comparing nested models. Also, if done correctly, quadrature approximations can be quite accurate, thus minimizing bias.

`meologit` supports three types of Gauss–Hermite quadrature and the Laplacian approximation method; see *Methods and formulas* of [ME] [meglm](#) for details.

Below we present two short examples of mixed-effects ordered logistic regression; refer to [ME] [melogit](#) for additional examples including crossed random-effects models and to [ME] [me](#) and [ME] [meglm](#) for examples of other random-effects models.

Two-level models

We begin with a simple application of (1) as a two-level model, because a one-level model, in our terminology, is just standard ordered logistic regression; see [R] [ologit](#).

► Example 1

We use the data from the Television, School, and Family Smoking Prevention and Cessation Project (Flay et al. 1988; Rabe-Hesketh and Skrondal 2012, chap. 11), where schools were randomly assigned into one of four groups defined by two treatment variables. Students within each school are nested in classes, and classes are nested in schools. In this example, we ignore the variability of classes within schools and fit a two-level model; we incorporate classes in a three-level model in [example 2](#). The dependent variable is the tobacco and health knowledge (THK) scale score collapsed into four ordered categories. We regress the outcome on the treatment variables and their interaction and control for the pretreatment score.

```

. use http://www.stata-press.com/data/r13/tvsfpor
. meologit thk prethk cc##tv || school:
Fitting fixed-effects model:
Iteration 0:  log likelihood = -2212.775
Iteration 1:  log likelihood = -2125.509
Iteration 2:  log likelihood = -2125.1034
Iteration 3:  log likelihood = -2125.1032
Refining starting values:
Grid node 0:  log likelihood = -2136.2426
Fitting full model:
Iteration 0:  log likelihood = -2136.2426 (not concave)
Iteration 1:  log likelihood = -2120.2577
Iteration 2:  log likelihood = -2119.7574
Iteration 3:  log likelihood = -2119.7428
Iteration 4:  log likelihood = -2119.7428
Mixed-effects ologit regression
Group variable:      school
Number of obs      =      1600
Number of groups   =       28
Obs per group: min =       18
                  avg =      57.1
                  max =      137
Integration method: mvaghermite
Integration points =       7
Wald chi2(4)      =     128.06
Prob > chi2       =     0.0000
Log likelihood = -2119.7428

```

thk	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
prethk	.4032892	.03886	10.38	0.000	.327125	.4794534
1.cc	.9237904	.204074	4.53	0.000	.5238127	1.323768
1.tv	.2749937	.1977424	1.39	0.164	-.1125744	.6625618
cc##tv						
1 1	-.4659256	.2845963	-1.64	0.102	-1.023724	.0918728
/cut1	-.0884493	.1641062	-0.54	0.590	-.4100916	.233193
/cut2	1.153364	.165616	6.96	0.000	.8287625	1.477965
/cut3	2.33195	.1734199	13.45	0.000	1.992053	2.671846
school						
var(_cons)	.0735112	.0383106			.0264695	.2041551

```
LR test vs. ologit regression:  chibar2(01) = 10.72 Prob>=chibar2 = 0.0005
```

Those of you familiar with the `mixed` command or other `me` commands will recognize the syntax and output. Below we comment on the items specific to ordered outcomes.

1. The estimation table reports the fixed effects, the estimated cutpoints ($\kappa_1, \kappa_2, \kappa_3$), and the estimated variance components. The fixed effects can be interpreted just as you would the output from `ologit`. We find that students with higher preintervention scores tend to have higher postintervention scores. Because of their interaction, the impact of the treatment variables on the knowledge score is not straightforward; we defer this discussion to [example 1](#) of [\[ME\] meologit postestimation](#). You can also specify the `or` option at estimation or on replay to display the fixed effects as odds ratios instead.
2. Underneath the fixed effects and the cutpoints, the table shows the estimated variance components. The random-effects equation is labeled `school`, meaning that these are random effects at the `school` level. Because we have only one random effect at this level, the table shows only one variance component. The estimate of σ_u^2 is 0.07 with standard error 0.04. The reported likelihood-ratio test

shows that there is enough variability between schools to favor a mixed-effects ordered logistic regression over a standard ordered logistic regression; see *Distribution theory for likelihood-ratio test* in [ME] **me** for a discussion of likelihood-ratio testing of variance components.

We now store our estimates for later use.

```
. estimates store r_2
```



Three-level models

Two-level models extend naturally to models with three or more levels with nested random effects. Below we continue with [example 1](#).

▷ Example 2

In this example, we fit a three-level model incorporating classes nested within schools as an additional level. The fixed-effects part remains the same.

```

. meologit thk prethk cc##tv || school: || class:
Fitting fixed-effects model:
Iteration 0:  log likelihood = -2212.775
Iteration 1:  log likelihood = -2125.509
Iteration 2:  log likelihood = -2125.1034
Iteration 3:  log likelihood = -2125.1032
Refining starting values:
Grid node 0:  log likelihood = -2152.1514
Fitting full model:
Iteration 0:  log likelihood = -2152.1514 (not concave)
Iteration 1:  log likelihood = -2125.9213 (not concave)
Iteration 2:  log likelihood = -2120.1861
Iteration 3:  log likelihood = -2115.6177
Iteration 4:  log likelihood = -2114.5896
Iteration 5:  log likelihood = -2114.5881
Iteration 6:  log likelihood = -2114.5881
Mixed-effects ologit regression          Number of obs    =      1600

```

Group Variable	No. of Groups	Observations per Group		
		Minimum	Average	Maximum
school	28	18	57.1	137
class	135	1	11.9	28

```

Integration method: mvaghermite          Integration points =      7
Wald chi2(4)          =      124.39
Prob > chi2          =      0.0000
Log likelihood = -2114.5881

```

thk	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
prethk	.4085273	.039616	10.31	0.000	.3308814	.4861731
1.cc	.8844369	.2099124	4.21	0.000	.4730161	1.295858
1.tv	.236448	.2049065	1.15	0.249	-.1651614	.6380575
cc##tv						
1 1	-.3717699	.2958887	-1.26	0.209	-.951701	.2081612
/cut1	-.0959459	.1688988	-0.57	0.570	-.4269815	.2350896
/cut2	1.177478	.1704946	6.91	0.000	.8433151	1.511642
/cut3	2.383672	.1786736	13.34	0.000	2.033478	2.733865
school						
var(_cons)	.0448735	.0425387			.0069997	.2876749
school>class						
var(_cons)	.1482157	.0637521			.063792	.3443674

```

LR test vs. ologit regression:          chi2(2) =      21.03  Prob > chi2 = 0.0000

```

Note: LR test is conservative and provided only for reference.

Notes:

1. Our model now has two random-effects equations, separated by ||. The first is a random intercept (constant only) at the school level (level three), and the second is a random intercept at the class level (level two). The order in which these are specified (from left to right) is significant—meologit assumes that class is nested within school.

2. The information on groups is now displayed as a table, with one row for each grouping. You can suppress this table with the `nogroup` or the `noheader` option, which will suppress the rest of the header as well.
3. The variance-component estimates are now organized and labeled according to level. The variance component for `class` is labeled `school>class` to emphasize that classes are nested within schools.

Compared with the two-level model from [example 1](#), the estimate of the variance of the random intercept at the school level dropped from 0.07 to 0.04. This is not surprising because we now use two random components versus one random component to account for unobserved heterogeneity among students. We can use `lrtest` and our stored estimation result from [example 1](#) to see which model provides a better fit:

```
. lrtest r_2 .
Likelihood-ratio test                                LR chi2(1) =    10.31
(Assumption: r_2 nested in .)                       Prob > chi2 =    0.0013
Note: The reported degrees of freedom assumes the null hypothesis is not on
the boundary of the parameter space. If this is not true, then the
reported test is conservative.
```

The likelihood-ratio test favors the three-level model. For more information about the likelihood-ratio test in the context of mixed-effects models, see [Distribution theory for likelihood-ratio test](#) in [ME] [me](#). ↴

The above extends to models with more than two levels of nesting in the obvious manner, by adding more random-effects equations, each separated by `||`. The order of nesting goes from left to right as the groups go from biggest (highest level) to smallest (lowest level).

Stored results

`meologit` stores the following in `e()`:

Scalars

<code>e(N)</code>	number of observations
<code>e(k)</code>	number of parameters
<code>e(k_dv)</code>	number of dependent variables
<code>e(k_cat)</code>	number of categories
<code>e(k_eq)</code>	number of equations in <code>e(b)</code>
<code>e(k_eq_model)</code>	number of equations in overall model test
<code>e(k_f)</code>	number of fixed-effects parameters
<code>e(k_r)</code>	number of random-effects parameters
<code>e(k_rs)</code>	number of variances
<code>e(k_rc)</code>	number of covariances
<code>e(df_m)</code>	model degrees of freedom
<code>e(ll)</code>	log likelihood
<code>e(N_clust)</code>	number of clusters
<code>e(chi2)</code>	χ^2
<code>e(p)</code>	significance
<code>e(ll_c)</code>	log likelihood, comparison model
<code>e(chi2_c)</code>	χ^2 , comparison model
<code>e(df_c)</code>	degrees of freedom, comparison model
<code>e(p_c)</code>	significance, comparison model
<code>e(rank)</code>	rank of <code>e(V)</code>
<code>e(ic)</code>	number of iterations
<code>e(rc)</code>	return code
<code>e(converged)</code>	1 if converged, 0 otherwise

Macros

e(cmd)	meologit
e(cmdline)	command as typed
e(depvar)	name of dependent variable
e(covariates)	list of covariates
e(ivars)	grouping variables
e(model)	ologit
e(title)	title in estimation output
e(link)	logit
e(family)	ordinal
e(clustvar)	name of cluster variable
e(offset)	offset
e(intmethod)	integration method
e(n_quad)	number of integration points
e(chi2type)	Wald; type of model χ^2
e(vce)	<i>vcetype</i> specified in <code>vce()</code>
e(vcetype)	title used to label Std. Err.
e(opt)	type of optimization
e(which)	max or min; whether optimizer is to perform maximization or minimization
e(ml_method)	type of ml method
e(user)	name of likelihood-evaluator program
e(technique)	maximization technique
e(datasignature)	the checksum
e(datasignaturevars)	variables used in calculation of checksum
e(properties)	b v
e(estat_cmd)	program used to implement <code>estat</code>
e(predict)	program used to implement <code>predict</code>

Matrices

e(b)	coefficient vector
e(Cns)	constraints matrix
e(ilog)	iteration log (up to 20 iterations)
e(gradient)	gradient vector
e(N_g)	group counts
e(g_min)	group-size minimums
e(g_avg)	group-size averages
e(g_max)	group-size maximums
e(V)	variance-covariance matrix of the estimator
e(V_modelbased)	model-based variance

Functions

e(sample)	marks estimation sample
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Methods and formulas

Without a loss of generality, consider a two-level ordered logistic model. The probability of observing outcome k for response y_{ij} is then

$$\begin{aligned}
 p_{ij} &= \Pr(y_{ij} = k | \boldsymbol{\kappa}, \mathbf{u}_j) = \Pr(\kappa_{k-1} < \boldsymbol{\eta}_{ij} + \epsilon_{it} \leq \kappa_k) \\
 &= \frac{1}{1 + \exp(-\kappa_k + \boldsymbol{\eta}_{ij})} - \frac{1}{1 + \exp(-\kappa_{k-1} + \boldsymbol{\eta}_{ij})}
 \end{aligned}$$

where $\boldsymbol{\eta}_{ij} = \mathbf{x}_{ij}\boldsymbol{\beta} + \mathbf{z}_{ij}\mathbf{u}_j + \text{offset}_{ij}$, κ_0 is taken as $-\infty$, and κ_K is taken as $+\infty$. Here \mathbf{x}_{ij} does not contain a constant term because its effect is absorbed into the cutpoints.

For cluster j , $j = 1, \dots, M$, the conditional distribution of $\mathbf{y}_j = (y_{j1}, \dots, y_{jn_j})'$ given a set of cluster-level random effects \mathbf{u}_j is

$$\begin{aligned}
 f(\mathbf{y}_j | \boldsymbol{\kappa}, \mathbf{u}_j) &= \prod_{i=1}^{n_j} p_{ij}^{I_k(y_{ij})} \\
 &= \exp \sum_{i=1}^{n_j} \left\{ I_k(y_{ij}) \log(p_{ij}) \right\}
 \end{aligned}$$

where

$$I_k(y_{ij}) = \begin{cases} 1 & \text{if } y_{ij} = k \\ 0 & \text{otherwise} \end{cases}$$

Because the prior distribution of \mathbf{u}_j is multivariate normal with mean $\mathbf{0}$ and $q \times q$ variance matrix $\boldsymbol{\Sigma}$, the likelihood contribution for the j th cluster is obtained by integrating \mathbf{u}_j out of the joint density $f(\mathbf{y}_j, \mathbf{u}_j)$,

$$\begin{aligned}
 \mathcal{L}_j(\boldsymbol{\beta}, \boldsymbol{\kappa}, \boldsymbol{\Sigma}) &= (2\pi)^{-q/2} |\boldsymbol{\Sigma}|^{-1/2} \int f(\mathbf{y}_j | \boldsymbol{\kappa}, \mathbf{u}_j) \exp(-\mathbf{u}_j' \boldsymbol{\Sigma}^{-1} \mathbf{u}_j / 2) d\mathbf{u}_j \\
 &= (2\pi)^{-q/2} |\boldsymbol{\Sigma}|^{-1/2} \int \exp\{h(\boldsymbol{\beta}, \boldsymbol{\kappa}, \boldsymbol{\Sigma}, \mathbf{u}_j)\} d\mathbf{u}_j
 \end{aligned} \tag{2}$$

where

$$h(\boldsymbol{\beta}, \boldsymbol{\kappa}, \boldsymbol{\Sigma}, \mathbf{u}_j) = \sum_{i=1}^{n_j} \left\{ I_k(y_{ij}) \log(p_{ij}) \right\} - \mathbf{u}_j' \boldsymbol{\Sigma}^{-1} \mathbf{u}_j / 2$$

and for convenience, in the arguments of $h(\cdot)$ we suppress the dependence on the observable data $(\mathbf{y}_j, \mathbf{r}_j, \mathbf{X}_j, \mathbf{Z}_j)$.

The integration in (2) has no closed form and thus must be approximated. `meologit` offers four approximation methods: mean–variance adaptive Gauss–Hermite quadrature (default unless a crossed random-effects model is fit), mode-curvature adaptive Gauss–Hermite quadrature, nonadaptive Gauss–Hermite quadrature, and Laplacian approximation (default for crossed random-effects models).

The Laplacian approximation is based on a second-order Taylor expansion of $h(\boldsymbol{\beta}, \boldsymbol{\kappa}, \boldsymbol{\Sigma}, \mathbf{u}_j)$ about the value of \mathbf{u}_j that maximizes it; see *Methods and formulas* in [ME] `meglm` for details.

Gaussian quadrature relies on transforming the multivariate integral in (2) into a set of nested univariate integrals. Each univariate integral can then be evaluated using a form of Gaussian quadrature; see *Methods and formulas* in [ME] `meglm` for details.

The log likelihood for the entire dataset is simply the sum of the contributions of the M individual clusters, namely, $\mathcal{L}(\boldsymbol{\beta}, \boldsymbol{\kappa}, \boldsymbol{\Sigma}) = \sum_{j=1}^M \mathcal{L}_j(\boldsymbol{\beta}, \boldsymbol{\kappa}, \boldsymbol{\Sigma})$.

Maximization of $\mathcal{L}(\boldsymbol{\beta}, \boldsymbol{\kappa}, \boldsymbol{\Sigma})$ is performed with respect to $(\boldsymbol{\beta}, \boldsymbol{\kappa}, \boldsymbol{\sigma}^2)$, where $\boldsymbol{\sigma}^2$ is a vector comprising the unique elements of $\boldsymbol{\Sigma}$. Parameter estimates are stored in `e(b)` as $(\hat{\boldsymbol{\beta}}, \hat{\boldsymbol{\kappa}}, \hat{\boldsymbol{\sigma}}^2)$, with the corresponding variance–covariance matrix stored in `e(V)`.

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Also see

- [ME] **meologit postestimation** — Postestimation tools for meologit
- [ME] **meoprobit** — Multilevel mixed-effects ordered probit regression
- [ME] **me** — Introduction to multilevel mixed-effects models
- [SEM] **intro 5** — Tour of models (*Multilevel mixed-effects models*)
- [XT] **xtologit** — Random-effects ordered logistic models
- [U] **20 Estimation and postestimation commands**