

**ghkfast()** — GHK multivariate normal simulator using pregenerated points

Syntax Diagnostics	Description Also see	Remarks and examples	Conformability
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## Syntax

$S = \text{ghkfast\_init}(\text{real scalar } n, \text{npts}, \text{dim}, \text{string scalar method})$

(varies)  $\text{ghkfast\_init\_pivot}(S [, \text{real scalar pivot}])$

(varies)  $\text{ghkfast\_init\_antithetics}(S [, \text{real scalar anti}])$

real scalar  $\text{ghkfast\_query\_n}(S)$

real scalar  $\text{ghkfast\_query\_npts}(S)$

real scalar  $\text{ghkfast\_query\_dim}(S)$

string scalar  $\text{ghkfast\_query\_method}(S)$

string scalar  $\text{ghkfast\_query\_rseed}(S)$

real matrix  $\text{ghkfast\_query\_pointset\_i}(S, i)$

real colvector  $\text{ghkfast}(S, \text{real matrix } X, V)$

real colvector  $\text{ghkfast}(S, \text{real matrix } X, V, \text{dfdx}, \text{dfdV})$

real scalar  $\text{ghkfast\_i}(S, \text{real matrix } X, V, i)$

real scalar  $\text{ghkfast\_i}(S, \text{real matrix } X, V, i, \text{dfdx}, \text{dfdV})$

where  $S$ , if it is declared, should be declared

transmorphic  $S$

and where *method* specified in  $\text{ghkfast\_init}()$  is

<i>method</i>	Description
"halton"	Halton sequences
"hammersley"	Hammersley's variation of the Halton set
"random"	pseudorandom uniforms
"ghalton"	generalized Halton sequences

## Description

Please see [M-5] [ghk\(\)](#). The routines documented here do the same thing, but [ghkfast\(\)](#) can be faster at the expense of using more memory. First, code  $S = \text{ghkfast\_init}(\dots)$  and then use [ghkfast\(S, \dots\)](#) to obtain the simulated values. There is a time savings because the simulation points are generated once in [ghkfast\\\_init\(\)](#), whereas for [ghk\(\)](#) the points are generated on each call to [ghk\(\)](#). Also, [ghkfast\(\)](#) can generate simulated probabilities from the generalized Halton sequence; see [M-5] [halton\(\)](#).

[ghkfast\\\_init\( \$n, npts, dim, method\$ \)](#) computes the simulation points to be used by [ghkfast\(\)](#). Inputs  $n$ ,  $npts$ , and  $dim$  are the number of observations, the number of repetitions for the simulation, and the maximum dimension of the multivariate normal (MVN) distribution, respectively. Input  $method$  specifies the type of points to generate and can be one of "halton", "hammersley", "random", or "ghalton".

[ghkfast\( \$S, X, V\$ \)](#) returns an  $n \times 1$  real vector containing the simulated values of the MVN distribution with  $dim \times dim$  variance–covariance matrix  $V$  at the points stored in the rows of the  $n \times dim$  matrix  $X$ .

[ghkfast\( \$S, X, V, dfdx, dfdv\$ \)](#) does the same thing as [ghkfast\( \$S, X, V\$ \)](#) but also returns the first-order derivatives of the simulated probability with respect to the rows of  $X$  in  $dfdx$  and the simulated probability derivatives with respect to  $\text{vech}(V)$  in  $dfdv$ . See [vech\(\)](#) in [M-5] [vec\(\)](#) for details of the half-vectorized operator.

The [ghk\\\_query\\\_n\( \$S\$ \)](#), [ghk\\\_query\\\_npts\( \$S\$ \)](#), [ghk\\\_query\\\_dim\( \$S\$ \)](#), and [ghk\\\_query\\\_method\( \$S\$ \)](#) functions extract the number of observations, number of simulation points, maximum dimension, and method of point-set generation that is specified in the construction of the transmorphic object  $S$ . Use [ghk\\\_query\\\_rseed\( \$S\$ \)](#) to retrieve the uniform random-variate seed used to generate the "random" or "ghalton" point sets. The [ghkfast\\\_query\\\_pointset\\\_i\( \$S, i\$ \)](#) function will retrieve the  $i$ th point set used to simulate the MVN probability for the  $i$ th observation.

The [ghkfast\\\_i\( \$S, X, V, i, \dots\$ \)](#) function computes the probability and derivatives for the  $i$ th observation,  $i = 1, \dots, n$ .

## Remarks and examples

[stata.com](http://www.stata.com)

For problems where repetitive calls to the GHK algorithm are required, [ghkfast\(\)](#) might be a preferred alternative to [ghk\(\)](#). Generating the points once at the outset of a program produces a speed increase. For problems with many observations or many simulation points per observation, [ghkfast\(\)](#) will be faster than [ghk\(\)](#) at the cost of requiring more memory.

If [ghkfast\(\)](#) is used within a likelihood evaluator for [ml](#) or [optimize\(\)](#), you will need to store the transmorphic object  $S$  as an [external](#) global and reuse the object with each likelihood evaluation. Alternatively, the initialization function for [optimize\(\)](#), [optimize\\\_init\\\_argument\(\)](#), can be used.

Prior to calling [ghkfast\(\)](#), call [ghkfast\\\_init\\\_npivot\( \$S, 1\$ \)](#) to turn off the integration interval pivoting that takes place in [ghkfast\(\)](#). By default, [ghkfast\(\)](#) pivots the wider intervals of integration (and associated rows/columns of the covariance matrix) to the interior of the multivariate integration to improve quadrature accuracy. This option may be useful when [ghkfast\(\)](#) is used in a likelihood evaluator for [R] [ml](#) or [M-5] [optimize\(\)](#) and few simulation points are used for each observation. Here the pivoting may cause discontinuities when computing numerical second-order derivatives using finite differencing (for the Newton–Raphson technique), resulting in a non–positive-definite Hessian.

Also the sequences "halton", "hammersley", and "random", `ghkfast()` will use the generalized Halton sequence, "ghalton". Generalized Halton sequences have the same uniform coverage (low discrepancy) as the Halton sequences with the addition of a pseudorandom uniform component. Therefore, "ghalton" sequences are like "random" sequences in that you should set the random-number seed before using them if you wish to replicate the same point set; see [M-5] `runiform()`.

## Conformability

All initialization functions have  $1 \times 1$  inputs and have  $1 \times 1$  or *void* outputs, and all query functions have the *transmorphic* input and  $1 \times 1$  outputs except

`ghkfast_init(n, npts, dim, method):`

*input:*

*n:*  $1 \times 1$   
*npts:*  $1 \times 1$   
*dim:*  $1 \times 1$   
*method:*  $1 \times 1$

*output:*

*result:* *transmorphic*

`ghkfast_query_pointset_i(S, i):`

*input:*

*S:* *transmorphic*  
*i:*  $1 \times 1$

*output:*

*result:*  $npts \times dim$

`ghkfast(S, X, V):`

*input:*

*S:* *transmorphic*  
*X:*  $n \times dim$   
*V:*  $dim \times dim$  (symmetric, positive definite)

*output:*

*result:*  $n \times 1$

`ghkfast(S, X, V, dfdx, dfdv):`

*input:*

*S:* *transmorphic*  
*X:*  $n \times dim$   
*V:*  $dim \times dim$  (symmetric, positive definite)

*output:*

*result:*  $n \times 1$   
*dfdx:*  $n \times dim$   
*dfdv:*  $n \times dim(dim + 1)/2$

`ghkfast_i(S, X, V, i, dfdx, dfdv)`:

*input:*

*S*: *transmorphic*  
*X*:  $n \times \text{dim}$  or  $1 \times \text{dim}$   
*V*:  $\text{dim} \times \text{dim}$  (symmetric, positive definite)  
*i*:  $1 \times 1$  ( $1 \leq i \leq n$ )

*output:*

*result*:  $n \times 1$   
*dfdx*:  $1 \times \text{dim}$   
*dfdv*:  $1 \times \text{dim}(\text{dim} + 1)/2$

## Diagnostics

`ghkfast_init(n, npts, dim, method)` aborts with error if the dimension, *dim*, is greater than 20.

`ghkfast(S, X, V, ...)` and `ghkfast_i(S, X, V, i, ...)` require that *V* be symmetric and positive definite. If *V* is not positive definite, then the returned vector (scalar) is filled with missings.

## Also see

[M-5] [ghk\(\)](#) — Geweke–Hajivassiliou–Keane (GHK) multivariate normal simulator

[M-5] [halton\(\)](#) — Generate a Halton or Hammersley set

[M-4] [statistical](#) — Statistical functions