xtabond — Arellano-Bond linear dynamic panel-data estimation

Description	Quick start	Menu	Syntax	Options
Remarks and examples	Stored results	Methods and formulas	References	Also see

Description

xtabond fits a linear dynamic panel-data model where the unobserved panel-level effects are correlated with the lags of the dependent variable, known as the Arellano–Bond estimator. This estimator is designed for datasets with many panels and few periods, and it requires that there be no autocorrelation in the idiosyncratic errors.

Quick start

```
Arellano-Bond estimation of y on x1 and x2 using xtset data xtabond y x1 x2
```

```
One-step estimator with robust standard errors xtabond y x1 x2, vce(robust)
```

```
Two-step estimator with bias-corrected robust standard errors xtabond y x1 x2, vce(robust) twostep
```

```
Arellano-Bond estimation also including 2 lagged values of y xtabond y x1 x2, lags(2)
```

Menu

Statistics > Longitudinal/panel data > Dynamic panel data (DPD) > Arellano-Bond estimation

Syntax

```
xtabond depvar [indepvars] [if] [in] [, options]
                                Description
 options
Model
 noconstant
                                suppress constant term
 inst(varlist)
                                additional instrument variables
 lags(#)
                                use # lags of dependent variable as covariates; default is lags (1)
                                maximum lags of dependent variable for use as instruments
 maxldep(#)
 maxlags(#)
                                maximum lags of predetermined and endogenous variables for use
                                   as instruments
                                compute the two-step estimator instead of the one-step estimator
 <u>two</u>step
Predetermined
 pre(varlist[...])
                                predetermined variables; can be specified more than once
Endogenous
 endogenous(varlist[...])
                                endogenous variables; can be specified more than once
SE/Robust
 vce(vcetype)
                                vcetype may be gmm or robust
Reporting
 level(#)
                                set confidence level; default is level (95)
                                use # as maximum order for AR tests; default is artests(2)
 artests(#)
 display_options
                                control spacing and line width
                                display legend instead of statistics
 coeflegend
```

A panel variable and a time variable must be specified; use xtset; see [XT] xtset.

indepvars and all varlists, except pre(varlist[...]) and endogenous (varlist[...]), may contain time-series operators; see [U] 11.4.4 Time-series varlists. The specification of depvar may not contain time-series operators.

by, collect, statsby, and xi are allowed; see [U] 11.1.10 Prefix commands.

coeflegend does not appear in the dialog box.

See [U] 20 Estimation and postestimation commands for more capabilities of estimation commands.

Options

Model

noconstant; see [R] Estimation options.

inst(varlist) specifies a set of variables to be used as additional instruments. These instruments are not differenced by xtabond before including them in the instrument matrix.

lags (#) sets p, the number of lags of the dependent variable to be included in the model. The default is p = 1.

maxldep(#) sets the maximum number of lags of the dependent variable that can be used as instruments. The default is to use all $T_i - p - 2$ lags.

maxlags (#) sets the maximum number of lags of the predetermined and endogenous variables that can be used as instruments. For predetermined variables, the default is to use all $T_i - p - 1$ lags. For endogenous variables, the default is to use all $T_i - p - 2$ lags.

Predetermined

 $\operatorname{pre}(\mathit{varlist}[$, $\underline{\operatorname{lagstruct}}(\mathit{prelags}, \mathit{premaxlags})])$ specifies that a set of predetermined variables be included in the model. Optionally, you may specify that $\mathit{prelags}$ lags of the specified variables also be included. The default for $\mathit{prelags}$ is 0. Specifying $\mathit{premaxlags}$ sets the maximum number of further lags of the predetermined variables that can be used as instruments. The default is to include $T_i - p - 1$ lagged levels as instruments for predetermined variables. You may specify as many sets of predetermined variables as you need within the standard Stata limits on matrix size. Each set of predetermined variables may have its own number of $\mathit{prelags}$ and $\mathit{premaxlags}$.

Endogenous

endogenous (varlist[, \underline{lag} struct(endlags, endmaxlags)]) specifies that a set of endogenous variables be included in the model. Optionally, you may specify that endlags lags of the specified variables also be included. The default for endlags is 0. Specifying endmaxlags sets the maximum number of further lags of the endogenous variables that can be used as instruments. The default is to include $T_i - p - 2$ lagged levels as instruments for endogenous variables. You may specify as many sets of endogenous variables as you need within the standard Stata limits on matrix size. Each set of endogenous variables may have its own number of endlags and endmaxlags.

SE/Robust

vce(vcetype) specifies the type of standard error reported, which includes types that are derived from asymptotic theory and that are robust to some kinds of misspecification; see Remarks and examples below.

vce(gmm), the default, uses the conventionally derived variance estimator for generalized method of moments estimation.

vce(robust) uses the robust estimator. After one-step estimation, this is the Arellano-Bond robust VCE estimator. After two-step estimation, this is the Windmeijer (2005) WC-robust estimator.

Reporting

level(#); see [R] Estimation options.

artests (#) specifies the maximum order of the autocorrelation test to be calculated. The tests are reported by estat abond; see [XT] **xtabond postestimation**. Specifying the order of the highest test at estimation time is more efficient than specifying it to estat abond, because estat abond must refit the model to obtain the test statistics. The maximum order must be less than or equal to the number of periods in the longest panel. The default is artests(2).

display_options: vsquish and nolstretch; see [R] Estimation options.

The following option is available with xtabond but is not shown in the dialog box:

coeflegend; see [R] Estimation options.

Linear dynamic panel-data models include p lags of the dependent variable as covariates and contain unobserved panel-level effects, fixed or random. By construction, the unobserved panel-level effects are correlated with the lagged dependent variables, making standard estimators inconsistent. Arellano and Bond (1991) derived a consistent generalized method of moments (GMM) estimator for the parameters of this model; xtabond implements this estimator.

Anderson and Hsiao (1981, 1982) propose using further lags of the level or the difference of the dependent variable to instrument the lagged dependent variables that are included in a dynamic panel-data model after the panel-level effects have been removed by first-differencing. A version of this estimator can be obtained from xtivreg (see [XT] xtivreg). Arellano and Bond (1991) build upon this idea by noting that, in general, there are many more instruments available. Building on Holtz-Eakin, Newey, and Rosen (1988) and using the GMM framework developed by Hansen (1982), they identify how many lags of the dependent variable, the predetermined variables, and the endogenous variables are valid instruments and how to combine these lagged levels with first differences of the strictly exogenous variables into a potentially large instrument matrix. Using this instrument matrix, Arellano and Bond (1991) derive the corresponding one-step and two-step GMM estimators, as well as the robust VCE estimator for the one-step model. They also found that the robust two-step VCE was seriously biased. Windmeijer (2005) worked out a bias-corrected (WC) robust estimator for VCEs of two-step GMM estimators, which is implemented in xtabond. The test of autocorrelation of order m and the Sargan test of overidentifying restrictions derived by Arellano and Bond (1991) can be obtained with estat abond and estat sargan, respectively; see [XT] xtabond postestimation.

The Arellano–Bond estimator is designed for datasets with many panels and few periods, and it requires that there be no autocorrelation in the idiosyncratic errors. For a related estimator that uses additional moment conditions, but still requires no autocorrelation in the idiosyncratic errors, see [XT] **xtd-pdsys**. For estimators that allow for some autocorrelation in the idiosyncratic errors, at the cost of a more complicated syntax, see [XT] **xtdpd**.

Example 1: One-step estimator

Arellano and Bond (1991) apply their new estimators and test statistics to a model of dynamic labor demand that had previously been considered by Layard and Nickell (1986) using data from an unbalanced panel of firms from the United Kingdom. All variables are indexed over the firm i and time t. In this dataset, \mathbf{n}_{it} is the log of employment in firm i at time t, \mathbf{w}_{it} is the natural log of the real product wage, \mathbf{k}_{it} is the natural log of the gross capital stock, and \mathbf{ys}_{it} is the natural log of industry output. The model also includes time dummies yr1980, yr1981, yr1982, yr1983, and yr1984. In table 4 of Arellano and Bond (1991), the authors present the results they obtained from several specifications.

In column a1 of table 4, Arellano and Bond report the coefficients and their standard errors from the robust one-step estimators of a dynamic model of labor demand in which n_{it} is the dependent variable and its first two lags are included as regressors. To clarify some important issues, we will begin with the homoskedastic one-step version of this model and then consider the robust case. Here is the command using xtabond and the subsequent output for the homoskedastic case:

```
. use https://www.stata-press.com/data/r19/abdata
. xtabond n 1(0/1).w 1(0/2).(k ys) yr1980-yr1984 year, lags(2) noconstant
Arellano-Bond dynamic panel-data estimation
                                                  Number of obs
                                                                               611
Group variable: id
                                                  Number of groups
                                                                               140
Time variable: year
                                                  Obs per group:
                                                                                 4
                                                                 min =
                                                                          4.364286
                                                                 avg =
                                                                 max =
                                                                                 6
Number of instruments =
                                                                           1757.07
                             41
                                                  Wald chi2(16)
                                                  Prob > chi2
                                                                            0.0000
One-step results
               Coefficient
                             Std. err.
                                                  P>|z|
                                                             [95% conf. interval]
           n
                                             7.
           n
                              .1486163
                  .6862261
                                           4.62
                                                  0.000
                                                             .3949435
                                                                          .9775088
         L1.
                                          -1.92
         L2.
                -.0853582
                              .0444365
                                                  0.055
                                                            -.1724523
                                                                          .0017358
           W
                -.6078208
                              .0657694
                                          -9.24
                                                  0.000
                                                            -.7367265
                                                                         -.4789151
         L1.
                  .3926237
                              .1092374
                                           3.59
                                                  0.000
                                                             .1785222
                                                                          .6067251
           k
                                           9.64
                                                  0.000
         --.
                  .3568456
                              .0370314
                                                             .2842653
                                                                          .4294259
         L1.
                -.0580012
                              .0583051
                                          -0.99
                                                  0.320
                                                             -.172277
                                                                          .0562747
         L2.
                -.0199475
                                          -0.48
                                                  0.632
                                                            -.1015357
                                                                          .0616408
                             .0416274
          уs
                  .6085073
                              .1345412
                                           4.52
                                                  0.000
                                                             .3448115
                                                                          .8722031
         -- .
         L1.
                -.7111651
                              . 1844599
                                          -3.86
                                                  0.000
                                                              -1.0727
                                                                         -.3496304
         L2.
                  .1057969
                              .1428568
                                           0.74
                                                  0.459
                                                            -.1741974
                                                                          .3857912
      vr1980
                 .0029062
                             .0212705
                                           0.14
                                                  0.891
                                                            -.0387832
                                                                          .0445957
      yr1981
                -.0404378
                             .0354707
                                          -1.14
                                                  0.254
                                                            -.1099591
                                                                          .0290836
      yr1982
                 -.0652767
                              .048209
                                          -1.35
                                                  0.176
                                                            -.1597646
                                                                          .0292111
      yr1983
                 -.0690928
                              .0627354
                                          -1.10
                                                  0.271
                                                            -.1920521
                                                                          .0538664
      yr1984
                 -.0650302
                              .0781322
                                          -0.83
                                                  0.405
                                                            -.2181665
                                                                          .0881061
                  .0095545
                                           0.67
                                                                          .0374002
        year
                              .0142073
                                                  0.501
                                                            -.0182912
```

Instruments for differenced equation

GMM-type: L(2/.).n

Standard: D.w LD.w D.k LD.k L2D.k D.ys LD.ys L2D.ys D.yr1980

D.yr1981 D.yr1982 D.yr1983 D.yr1984 D.year

The coefficients are identical to those reported in column a1 of table 4, as they should be. Of course, the standard errors are different because we are considering the homoskedastic case. Although the moment conditions use first-differenced errors, xtabond estimates the coefficients of the level model and reports them accordingly.

The footer in the output reports the instruments used. The first line indicates that xtabond used lags from 2 on back to create the GMM-type instruments described in Arellano and Bond (1991) and Holtz-Eakin, Newey, and Rosen (1988); also see *Methods and formulas* in [XT] **xtdpd**. The second and third lines indicate that the first difference of all the exogenous variables were used as standard instruments. GMM-type instruments use the lags of a variable to contribute multiple columns to the instrument matrix, whereas each standard instrument contributes one column to the instrument matrix. The notation L(2/.).n indicates that GMM-type instruments were created using lag 2 of n from on back. (L(2/4).n would indicate that GMM-type instruments were created using only lags 2, 3, and 4 of n.)

After xtabond, estat sargan reports the Sargan test of overidentifying restrictions.

Only for a homoskedastic error term does the Sargan test have an asymptotic χ^2 distribution. In fact, Arellano and Bond (1991) show that the one-step Sargan test overrejects in the presence of heteroskedasticity. Because its asymptotic distribution is not known under the assumptions of the vce(robust) model, xtabond does not compute it when vce(robust) is specified. The Sargan test, reported by Arellano and Bond (1991, table 4, column a1), comes from the one-step homoskedastic estimator and is the same as the one reported here. The output above presents strong evidence against the null hypothesis that the overidentifying restrictions are valid. Rejecting this null hypothesis implies that we need to reconsider our model or our instruments, unless we attribute the rejection to heteroskedasticity in the data-generating process. Although performing the Sargan test after the two-step estimator is an alternative, Arellano and Bond (1991) found a tendency for this test to underreject in the presence of heteroskedasticity. (See [XT] xtdpd for an example indicating that this rejection may be due to misspecification.)

By default, xtabond calculates the Arellano-Bond test for first- and second-order autocorrelation in the first-differenced errors. (Use artests() to compute tests for higher orders.) There are versions of this test for both the homoskedastic and the robust cases, although their values are different. Use estat abond to report the test results.

```
. estat abond

Arellano-Bond test for zero autocorrelation in first-differenced errors

HO: No autocorrelation

Order z Prob > z

1 -3.9394 0.0001
2 -.54239 0.5876
```

When the idiosyncratic errors are independent and identically distributed (i.i.d.), the first-differenced errors are first-order serially correlated. So, as expected, the output above presents strong evidence against the null hypothesis of zero autocorrelation in the first-differenced errors at order 1. Serial correlation in the first-differenced errors at an order higher than 1 implies that the moment conditions used by xtabond are not valid; see [XT] xtdpd for an example of an alternative estimation method. The output above presents no significant evidence of serial correlation in the first-differenced errors at order 2.

Example 2: A one-step estimator with robust VCE

Consider the output from the one-step robust estimator of the same model:

. xtabond n 1(0/1).w 1(0/2).(k ys) yr1980-yr1984 year, lags(2) vce(robust)

> noconstant

Arellano-Bond dynamic panel-data estimation Number of obs

Time variable: year

Group variable: id Number of groups = 140

Obs per group:

min =4.364286 avg = max =

Number of instruments = 41 = 1727.45 Wald chi2(16) Prob > chi2 0.0000

One-step results

(Std. err. adjusted for clustering on id)

n	Coefficient	Robust std. err.	z	P> z	[95% conf.	interval]
n						
L1.	.6862261	.1445943	4.75	0.000	.4028266	.9696257
L2.	0853582	.0560155	-1.52	0.128	1951467	.0244302
W						
	6078208	.1782055	-3.41	0.001	9570972	2585445
L1.	.3926237	.1679931	2.34	0.019	.0633632	.7218842
k						
	.3568456	.0590203	6.05	0.000	.241168	.4725233
L1.	0580012	.0731797	-0.79	0.428	2014308	.0854284
L2.	0199475	.0327126	-0.61	0.542	0840631	.0441681
ys						
	.6085073	. 1725313	3.53	0.000	.2703522	.9466624
L1.	7111651	.2317163	-3.07	0.002	-1.165321	2570095
L2.	.1057969	.1412021	0.75	0.454	1709542	.382548
yr1980	.0029062	.0158028	0.18	0.854	0280667	.0338791
yr1981	0404378	.0280582	-1.44	0.150	0954307	.0145552
yr1982	0652767	.0365451	-1.79	0.074	1369038	.0063503
yr1983	0690928	.047413	-1.46	0.145	1620205	.0238348
yr1984	0650302	.0576305	-1.13	0.259	1779839	.0479235
year	.0095545	.0102896	0.93	0.353	0106127	.0297217

Instruments for differenced equation

GMM-type: L(2/.).n

Standard: D.w LD.w D.k LD.k L2D.k D.ys LD.ys L2D.ys D.yr1980

D.yr1981 D.yr1982 D.yr1983 D.yr1984 D.year

The coefficients are the same, but now the standard errors match that reported in Arellano and Bond (1991, table 4, column a1). Most of the robust standard errors are higher than those that assume a homoskedastic error term.

The Sargan statistic cannot be calculated after requesting a robust VCE, but robust tests for serial correlation are available.

. estat abond

Arellano-Bond test for zero autocorrelation in first-differenced errors HO: No autocorrelation

Order z Prob > z 1 -3.5996 0.0003 2 -.51603 0.6058

The value of the test for second-order autocorrelation matches those reported in Arellano and Bond (1991, table 4, column a1) and presents no evidence of model misspecification.

Example 3: The Wald model test

xtabond reports the Wald statistic of the null hypothesis that all the coefficients except the constant are zero. Here the null hypothesis is that all the coefficients are zero, because there is no constant in the model. In our previous example, the null hypothesis is soundly rejected. In column a1 of table 4, Arellano and Bond report a χ^2 test of the null hypothesis that all the coefficients are zero, except the time trend and the time dummies. Here is this test in Stata:

```
. test 1.n 12.n w 1.w k 1.k 12.k ys 1.ys 12.ys
(1)
     L.n = 0
(2)
      L2.n = 0
(3)
      w = 0
(4)
      L.w = 0
      k = 0
(5)
(6)
      L.k = 0
(7)
      L2.k = 0
      ys = 0
(8)
(9)
     L.ys = 0
(10)
      L2.vs = 0
          chi2(10) = 408.29
        Prob > chi2 =
                         0.0000
```

4

4

Example 4: A two-step estimator with Windmeijer bias-corrected robust VCE

The two-step estimator with the Windmeijer bias-corrected robust VCE of the same model produces the following output:

```
. xtabond n 1(0/1).w 1(0/2).(k ys) yr1980-yr1984 year, lags(2) twostep
> vce(robust) noconstant
Arellano-Bond dynamic panel-data estimation
                                                Number of obs
                                                                            611
                                                Number of groups =
Group variable: id
                                                                            140
Time variable: year
                                                Obs per group:
                                                               min =
                                                                              4
                                                               avg =
                                                                       4.364286
                                                               max =
                                                                              6
Number of instruments =
                            41
                                                Wald chi2(16)
                                                                        1104.72
                                                Prob > chi2
                                                                         0.0000
```

(Std. err. adjusted for clustering on id)

n	Coefficient	WC-robust std. err.	z	P> z	[95% conf.	interval]
n						
L1.	.6287089	.1934138	3.25	0.001	.2496248	1.007793
L2.	0651882	.0450501	-1.45	0.148	1534847	.0231084
W						
".	5257597	.1546107	-3.40	0.001	828791	2227284
L1.	.3112899	.2030006	1.53	0.125	086584	.7091638
k	000000					
	.2783619	.0728019	3.82	0.000	.1356728	.4210511
L1.	.0140994	.0924575	0.15	0.879	167114	.1953129
L2.	0402484	.0432745	-0.93	0.352	1250649	.0445681
ys						
 .	.5919243	.1730916	3.42	0.001	.252671	.9311776
L1.	5659863	.2611008	-2.17	0.030	-1.077734	0542381
L2.	.1005433	.1610987	0.62	0.533	2152043	.4162908
1000	.0006378	.0168042	0.04	0.970	0322978	.0335734
yr1980						
yr1981	0550044	.0313389	-1.76	0.079	1164275	.0064187
yr1982	075978	.0419276	-1.81	0.070	1581545	.0061986
yr1983	0740708	.0528381	-1.40	0.161	1776315	.02949
yr1984	0906606	.0642615	-1.41	0.158	2166108	.0352896
year	.0112155	.0116783	0.96	0.337	0116735	.0341045

Instruments for differenced equation

GMM-type: L(2/.).n

Two-step results

Standard: D.w LD.w D.k LD.k L2D.k D.ys LD.ys L2D.ys D.yr1980 D.yr1981 D.yr1982 D.yr1983 D.yr1984 D.year

Arellano and Bond recommend against using the two-step nonrobust results for inference on the coefficients because the standard errors tend to be biased downward (see Arellano and Bond 1991 for details). The output above uses the Windmeijer bias-corrected (WC) robust VCE, which Windmeijer (2005) showed to work well. The magnitudes of several of the coefficient estimates have changed, and one even switched its sign.

The test for autocorrelation presents no evidence of model misspecification:

. estat abond

Arellano-Bond test for zero autocorrelation in first-differenced errors HO: No autocorrelation

Order	z	Prob > z
1	-2.1255	0.0335
2	35166	0.7251

4

Manuel Arellano (1957-) was born in Elda in Alicante, Spain. He earned degrees in economics from the University of Barcelona and the London School of Economics. After various posts in Oxford and London, he returned to Spain as professor of econometrics at Madrid in 1991. He is a leading expert on panel-data econometrics.

Stephen Roy Bond (1963-) earned degrees in economics from Cambridge and Oxford. Following various posts at Oxford, he now works mainly at the Institute for Fiscal Studies in London. His research interests include company taxation, dividends, and the links between financial markets, corporate control, and investment.

Example 5: Including an estimator for the constant

Thus far we have been specifying the noconstant option to keep to the standard Arellano-Bond estimator, which uses instruments only for the difference equation. The constant estimated by xtabond is a constant in the level equation, and it is estimated from the level errors. The output below illustrates that including a constant in the model does not affect the other parameter estimates.

. xtabond n 1(0/1).w 1(0/2).(k ys) yr1980-yr1984 year, lags(2) twostep vce(robust)

Arellano-Bond dynamic panel-data estimation Number of obs Number of groups = Group variable: id 140

Time variable: year

Obs per group:

4 min =4.364286 avg = max = 6

Number of instruments = 42

1104.72 Wald chi2(16) Prob > chi2 0.0000

Two-step results

(Std. err. adjusted for clustering on id)

n	Coefficient	WC-robust std. err.	z	P> z	[95% conf.	interval]
n						
L1.	.6287089	. 1934138	3.25	0.001	.2496248	1.007793
L2.	0651882	.0450501	-1.45	0.148	1534847	.0231084
W						
	5257597	.1546107	-3.40	0.001	828791	2227284
L1.	.3112899	.2030006	1.53	0.125	086584	.7091638
k						
	.2783619	.0728019	3.82	0.000	.1356728	.4210511
L1.	.0140994	.0924575	0.15	0.879	167114	.1953129
L2.	0402484	.0432745	-0.93	0.352	1250649	.0445681
ys						
	.5919243	.1730916	3.42	0.001	.252671	.9311776
L1.	5659863	.2611008	-2.17	0.030	-1.077734	0542381
L2.	.1005433	.1610987	0.62	0.533	2152043	.4162908
yr1980	.0006378	.0168042	0.04	0.970	0322978	.0335734
yr1981	0550044	.0313389	-1.76	0.079	1164275	.0064187
yr1982	075978	.0419276	-1.81	0.070	1581545	.0061986
yr1983	0740708	.0528381	-1.40	0.161	1776315	.02949
yr1984	0906606	.0642615	-1.41	0.158	2166108	.0352896
year	.0112155	.0116783	0.96	0.337	0116735	.0341045
_cons	-21.53725	23.23138	-0.93	0.354	-67.06992	23.99542

Instruments for differenced equation

GMM-type: L(2/.).n

Standard: D.w LD.w D.k LD.k L2D.k D.ys LD.ys L2D.ys D.yr1980

D.yr1981 D.yr1982 D.yr1983 D.yr1984 D.year

Instruments for level equation

Standard: _cons

Including the constant does not affect the other parameter estimates because it is identified only by the level errors; see [XT] xtdpd for details.

> pre(k, lag(2,.)) noconstant vce(robust)

Instruments for differenced equation

D.year

GMM-type: L(2/.).n L(1/.).L.w L(1/.).L2.k

Sometimes we cannot assume strict exogeneity. Recall that a variable, x_{it} , is said to be strictly exogenous if $E[x_{it}\epsilon_{is}]=0$ for all t and s. If $E[x_{it}\epsilon_{is}]\neq 0$ for s< t but $E[x_{it}\epsilon_{is}]=0$ for all $s\geq t$, the variable is said to be predetermined. Intuitively, if the error term at time t has some feedback on the subsequent realizations of x_{it} , x_{it} is a predetermined variable. Because unforecastable errors today might affect future changes in the real wage and in the capital stock, we might suspect that the log of the real product wage and the log of the gross capital stock are predetermined instead of strictly exogenous. Here we treat w and k as predetermined and use lagged levels as instruments.

. xtabond n 1(0/1).ys yr1980-yr1984 year, lags(2) twostep pre(w, lag(1,.))

```
Arellano-Bond dynamic panel-data estimation
                                                  Number of obs
                                                                               611
Group variable: id
                                                  Number of groups =
                                                                               140
Time variable: year
                                                   Obs per group:
                                                                  min =
                                                                          4.364286
                                                                  avg =
                                                                  max =
                                                                                  6
Number of instruments =
                             83
                                                  Wald chi2(15)
                                                                            958.30
                                                                            0.0000
                                                  Prob > chi2
Two-step results
                                       (Std. err. adjusted for clustering on id)
                             WC-robust
               Coefficient
                             std. err.
                                                             [95% conf. interval]
           n
                                             z
                                                  P>|z|
           n
                  .8580958
                              .1265515
                                           6.78
                                                  0.000
                                                             .6100594
                                                                          1.106132
         T.1.
         L2.
                  -.081207
                              .0760703
                                          -1.07
                                                  0.286
                                                            -.2303022
                                                                          .0678881
           W
                -.6910855
                                          -4.98
                                                  0.000
                                                                         -.4191044
                              .1387684
                                                            -.9630666
         L1.
                  .5961712
                              .1497338
                                           3.98
                                                  0.000
                                                             .3026982
                                                                          .8896441
           k
         --.
                  .4140654
                              .1382788
                                           2.99
                                                  0.003
                                                             .1430439
                                                                          .6850868
         L1.
                -.1537048
                              .1220244
                                          -1.26
                                                  0.208
                                                            -.3928681
                                                                          .0854586
         L2.
                -.1025833
                                          -1.44
                                                            -.2419143
                                                                          .0367477
                              .0710886
                                                  0.149
          уs
         --.
                  .6936392
                              .1728623
                                           4.01
                                                  0.000
                                                             .3548354
                                                                          1.032443
         L1.
                -.8773678
                              .2183085
                                          -4.02
                                                  0.000
                                                            -1.305245
                                                                          -.449491
      yr1980
                -.0072451
                              .017163
                                          -0.42
                                                  0.673
                                                            -.0408839
                                                                          .0263938
      yr1981
                -.0609608
                              .030207
                                          -2.02
                                                  0.044
                                                            -.1201655
                                                                         -.0017561
      yr1982
                -.1130369
                              .0454826
                                          -2.49
                                                  0.013
                                                            -.2021812
                                                                         -.0238926
                                          -2.22
      yr1983
                 -.1335249
                              .0600213
                                                  0.026
                                                             -.2511645
                                                                         -.0158853
      yr1984
                -.1623177
                              .0725434
                                          -2.24
                                                            -.3045001
                                                                         -.0201352
                                                  0.025
        year
                  .0264501
                              .0119329
                                           2.22
                                                  0.027
                                                               .003062
                                                                          .0498381
```

The footer informs us that we are now including GMM-type instruments from the first lag of L.w on back and from the first lag of L2.k on back.

Standard: D.ys LD.ys D.yr1980 D.yr1981 D.yr1982 D.yr1983 D.yr1984

□ Technical note

The above example illustrates that xtabond understands pre(w, lag(1, .)) to mean that L.w is a predetermined variable and pre(k, lag(2, .)) to mean that L2.k is a predetermined variable. This is a stricter definition than the alternative that pre(w, lag(1, .)) means only that w is predetermined but includes a lag of w in the model and that pre(k, lag(2, .)) means only that k is predetermined but includes first and second lags of k in the model. If you prefer the weaker definition, xtabond still gives you consistent estimates, but it is not using all possible instruments; see [XT] xtdpd for an example of how to include all possible instruments.

Example 7: Including endogenous covariates

We might instead suspect that w and k are endogenous in that $E[x_{it}\epsilon_{is}] \neq 0$ for $s \leq t$ but $E[x_{it}\epsilon_{is}] = 0$ for all s > t. By this definition, endogenous variables differ from predetermined variables only in that the former allow for correlation between the x_{it} and the ϵ_{it} at time t, whereas the latter do not. Endogenous variables are treated similarly to the lagged dependent variable. Levels of the endogenous variables lagged two or more periods can serve as instruments. In this example, we treat w and k as endogenous variables.

```
. xtabond n 1(0/1).ys yr1980-yr1984 year, lags(2) twostep
> endogenous(w, lag(1,.)) endogenous(k, lag(2,.)) noconstant vce(robust)
Arellano-Bond dynamic panel-data estimation
                                                 Number of obs
Group variable: id
                                                 Number of groups =
                                                                             140
Time variable: year
                                                 Obs per group:
                                                               min =
                                                                               4
                                                               avg =
                                                                       4.364286
                                                               max =
Number of instruments =
                            71
                                                 Wald chi2(15)
                                                                         967.61
                                                 Prob > chi2
                                                                         0.0000
Two-step results
                                      (Std. err. adjusted for clustering on id)
```

n	Coefficient	WC-robust std. err.	z	P> z	[95% conf.	interval]
n	6640937					
	6640937					
L1.	.00±0331	.1278908	5.19	0.000	.4134323	.914755
L2.	041283	.081801	-0.50	0.614	2016101	.1190441
W						
	7143942	.13083	-5.46	0.000	9708162	4579721
L1.	.3644198	.184758	1.97	0.049	.0023008	.7265388
k						
	.5028874	.1205419	4.17	0.000	.2666296	.7391452
L1.	2160842	.0972855	-2.22	0.026	4067603	025408
L2.	0549654	.0793673	-0.69	0.489	2105225	.1005917
ys						
	.5989356	.1779731	3.37	0.001	.2501148	.9477564
L1.	6770367	.1961166	-3.45	0.001	-1.061418	2926553
yr1980	0061122	.0155287	-0.39	0.694	0365478	.0243235
yr1981	04715	.0298348	-1.58	0.114	1056252	.0113251
yr1982	0817646	.0486049	-1.68	0.093	1770285	.0134993
yr1983	0939251	.0675804	-1.39	0.165	2263802	.0385299
yr1984	117228	.0804716	-1.46	0.145	2749493	.0404934
year	.0208857	.0103485	2.02	0.044	.0006031	.0411684

Instruments for differenced equation

GMM-type: L(2/.).n L(2/.).L.w L(2/.).L2.k

Standard: D.ys LD.ys D.yr1980 D.yr1981 D.yr1982 D.yr1983 D.yr1984

Although some estimated coefficients changed in magnitude, none changed in sign, and these results are similar to those obtained by treating w and k as predetermined. 4

The Arellano-Bond estimator is for datasets with many panels and few periods. (Technically, the large-sample properties are derived with the number of panels going to infinity and the number of periods held fixed.) The number of instruments increases quadratically in the number of periods. If your dataset is better described by a framework in which both the number of panels and the number of periods is large, then you should consider other estimators such as those in [XT] xtivreg or xtreg, fe in [XT] xtreg; see Alvarez and Arellano (2003) for a discussion of this case.

Treating variables as predetermined or endogenous quickly increases the size of the instrument matrix. (See Methods and formulas in [XT] xtdpd for a discussion of how this matrix is created and what determines its size.) GMM estimators with too many overidentifying restrictions may perform poorly in small samples. (See Kiviet 1995 for a discussion of the dynamic panel-data case.)

To handle these problems, you can set a maximum number of lagged levels to be included as instruments for lagged-dependent or the predetermined variables. Here is an example in which a maximum of three lagged levels of the predetermined variables are included as instruments:

```
. xtabond n 1(0/1).ys yr1980-yr1984 year, lags(2) twostep
> pre(w, lag(1,3)) pre(k, lag(2,3)) noconstant vce(robust)
Arellano-Bond dynamic panel-data estimation
                                                 Number of obs
                                                                             611
                                                 Number of groups =
Group variable: id
                                                                             140
Time variable: year
                                                 Obs per group:
                                                               min =
                                                               avg =
                                                                        4.364286
                                                               max =
Number of instruments =
                            67
                                                 Wald chi2(15)
                                                                         1116.89
                                                 Prob > chi2
                                                                         0.0000
Two-step results
                                      (Std. err. adjusted for clustering on id)
```

n	Coefficient	WC-robust std. err.	z	P> z	[95% conf.	interval]
n						
L1.	.931121	.1456964	6.39	0.000	.6455612	1.216681
L2.	0759918	.0854356	-0.89	0.374	2434425	.0914589
W						
	6475372	.1687931	-3.84	0.000	9783656	3167089
L1.	.6906238	.1789698	3.86	0.000	.3398493	1.041398
k						
	.3788106	.1848137	2.05	0.040	.0165824	.7410389
L1.	2158533	.1446198	-1.49	0.136	4993028	.0675962
L2.	0914584	.0852267	-1.07	0.283	2584997	.0755829
ys						
	.7324964	.176748	4.14	0.000	.3860766	1.078916
L1.	9428141	.2735472	-3.45	0.001	-1.478957	4066715
yr1980	0102389	.0172473	-0.59	0.553	0440431	.0235652
yr1981	0763495	.0296992	-2.57	0.010	1345589	0181402
yr1982	1373829	.0441833	-3.11	0.002	2239806	0507853
yr1983	1825149	.0613674	-2.97	0.003	3027928	0622369
yr1984	2314023	.0753669	-3.07	0.002	3791186	083686
year	.0310012	.0119167	2.60	0.009	.0076448	.0543576

Instruments for differenced equation

GMM-type: L(2/.).n L(1/3).L.w L(1/3).L2.k

Standard: D.ys LD.ys D.yr1980 D.yr1981 D.yr1982 D.yr1983 D.yr1984 D.year

Example 9: Missing observations in the middle of panels

xtabond handles data in which there are missing observations in the middle of the panels. In this example, we deliberately set the dependent variable to missing in the year 1980:

```
. replace n=. if year==1980
(140 real changes made, 140 to missing)
. xtabond n 1(0/1).w 1(0/2).(k ys) yr1980-yr1984 year, lags(2) noconstant
> vce(robust)
note: yr1980 omitted from div() because of collinearity.
note: yr1981 omitted from div() because of collinearity.
note: yr1982 omitted from div() because of collinearity.
note: yr1980 omitted because of collinearity.
note: yr1981 omitted because of collinearity.
note: yr1982 omitted because of collinearity.
Arellano-Bond dynamic panel-data estimation
                                                Number of obs
                                                                           115
                                                Number of groups =
                                                                           101
Group variable: id
Time variable: year
                                                Obs per group:
                                                              min =
                                                                             1
                                                                      1.138614
                                                              avg =
                                                              max =
Number of instruments =
                            18
                                                Wald chi2(12)
                                                                         44.48
                                                Prob > chi2
                                                                        0.0000
One-step results
                                     (Std. err. adjusted for clustering on id)
                             Robust
               Coefficient std. err.
                                                P>|z|
                                                          [95% conf. interval]
           n
           n
                 .1790577
                                         0.81
                                                          -.253052
         L1.
                            .2204682
                                                0.417
                                                                      .6111674
         L2.
                 .0214253
                            .0488476
                                         0.44
                                                0.661
                                                         -.0743143
                                                                      .1171649
           W
                                        -1.79
                -.2513405
                            .1402114
                                                0.073
                                                         -.5261498
                                                                      .0234689
                 .1983952
                                        1.37
                                                         -.0849912
         L1.
                            .1445875
                                                0.170
                                                                      .4817815
          k
         --.
                 .3983149
                            .0883352
                                         4.51
                                                0.000
                                                          .2251811
                                                                     .5714488
         L1.
                 -.025125
                            .0909236
                                        -0.28
                                                0.782
                                                          -.203332
                                                                      .1530821
         L2.
                -.0359338
                            .0623382
                                        -0.58
                                                0.564
                                                         -.1581144
                                                                      .0862468
         уs
                            .3824893
                                         0.96
                                                0.338
                                                         -.3833451
         --.
                 .3663201
                                                                      1.115985
         L1.
                -.6319976
                            .4823958
                                        -1.31
                                                0.190
                                                         -1.577476
                                                                      .3134807
```

Instruments for differenced equation

.5318404

-.0047543

.0014465

GMM-type: L(2/.).n

L2.

yr1983

yr1984

year

Standard: D.w LD.w D.k LD.k L2D.k D.ys LD.ys L2D.ys D.yr1983

.4105269

.024855

.010355

0 (omitted)

D.yr1984 D.year

There are two important aspects to this example. First, xtabond reports that variables have been omitted from the model and from the div() instrument list. For xtabond, the div() instrument list is the list of instruments created from the strictly exogenous variables; see [XT] xtdpd for more about the div()

1.30

-0.19

0.14

0.195

0.848

0.889

-.2727775

-.0534692

-.0188489

1.336458

.0439606

.0217419

instrument list. Second, because xtabond uses time-series operators in its computations, if statements and missing values are not equivalent. An if statement causes the false observations to be excluded from the sample, but it computes the time-series operators wherever possible. In contrast, missing data prevent evaluation of the time-series operators that involve missing observations. Thus the example above is not equivalent to the following one:

```
. use https://www.stata-press.com/data/r19/abdata, clear
. xtabond n 1(0/1).w 1(0/2).(k ys) yr1980-yr1984 year if year!=1980,
> lags(2) noconstant vce(robust)
note: yr1980 omitted from div() because of collinearity.
note: yr1980 omitted because of collinearity.
Arellano-Bond dynamic panel-data estimation
                                                Number of obs
                                                                            473
Group variable: id
                                                Number of groups =
                                                                            140
Time variable: year
                                                Obs per group:
                                                              min =
                                                                              3
                                                                       3.378571
                                                              avg =
                                                              max =
Number of instruments =
                            37
                                                Wald chi2(15)
                                                                        1041.61
                                                Prob > chi2
                                                                         0.0000
One-step results
                                     (Std. err. adjusted for clustering on id)
                             Robust
               Coefficient std. err.
                                                P>|z|
                                                           [95% conf. interval]
           n
           n
                                         5.46
                                                0.000
                                                                       .9799593
         L1.
                 .7210062
                            .1321214
                                                           .4620531
         L2.
                -.0960646
                            .0570547
                                        -1.68
                                                0.092
                                                         -.2078898
                                                                       .0157606
           W
         --.
                -.6684175
                            .1739484
                                        -3.84
                                                0.000
                                                          -1.00935
                                                                     -.3274849
         L1.
                  .482322
                            .1647185
                                         2.93
                                                0.003
                                                           .1594797
                                                                       .8051642
          k
                                         5.22
                                                0.000
                 .3802777
                            .0728546
                                                          .2374853
                                                                       .5230701
         L1.
                 -.104598
                             .088597
                                        -1.18
                                                0.238
                                                          -.278245
                                                                        .069049
         L2.
                                        -0.72
                -.0272055
                            .0379994
                                                0.474
                                                           -.101683
                                                                       .0472721
         уs
                 .4655989
                            .1864368
                                         2.50
                                                0.013
                                                          .1001895
                                                                      .8310082
         --.
         L1.
                -.8562492
                            .2187886
                                        -3.91
                                                0.000
                                                         -1.285067
                                                                     -.4274315
         L2.
                 .0896556
                            .1440035
                                        0.62 0.534
                                                          -.192586
                                                                      .3718972
      yr1981
                -.0711626
                            .0205299
                                        -3.47
                                                0.001
                                                                     -.0309247
                                                         -.1114005
      vr1982
                -.1212749
                            .0334659
                                        -3.62
                                                0.000
                                                         -.1868669
                                                                     -.0556829
                -.1470248
                                        -3.18
                                                0.001
                                                         -.2375191
                                                                     -.0565305
      yr1983
                            .0461714
      yr1984
                -.1519021
                            .0543904
                                        -2.79
                                                0.005
                                                         -.2585054
                                                                     -.0452988
                 .0203277
                            .0108732
                                        1.87
                                                0.062
                                                         -.0009833
                                                                      .0416387
```

Instruments for differenced equation

GMM-type: L(2/.).n

year

Standard: D.w LD.w D.k LD.k L2D.k D.ys LD.ys L2D.ys D.yr1981 D.yr1982 D.yr1983 D.yr1984 D.year

The year 1980 is omitted from the sample, but when the value of a variable from 1980 is required because a lag or difference is required, the 1980 value is used.

Stored results

xtabond stores the following in e():

```
Scalars
                               number of observations
    e(N)
                               number of groups
    e(N_g)
    e(df_m)
                               model degrees of freedom
                               smallest group size
    e(g_min)
    e(g_avg)
                               average group size
                               largest group size
    e(g_max)
    e(t_min)
                               minimum time in sample
    e(t_max)
                               maximum time in sample
    e(chi2)
    e(arm#)
                               test for autocorrelation of order #
                               number of AR tests computed
    e(artests)
                               estimate of \sigma_{\epsilon}^2
    e(sig2)
                               sum of squared differenced residuals
    e(rss)
                               Sargan test statistic
    e(sargan)
    e(rank)
                               rank of e(V)
                               rank of instrument matrix
    e(zrank)
Macros
    e(cmd)
                               xtabond
                               command as typed
    e(cmdline)
    e(depvar)
                               name of dependent variable
                               twostep, if specified
    e(twostep)
    e(ivar)
                               variable denoting groups
                               variable denoting time within groups
    e(tvar)
                               vcetvpe specified in vce()
    e(vce)
                               title used to label Std. err.
    e(vcetype)
                               system, if system estimator
    e(system)
    e(transform)
                               specified transform
                               checksum from datasignature
    e(datasignature)
                               variables used in calculation of checksum
    e(datasignaturevars)
    e(properties)
    e(estat_cmd)
                               program used to implement estat
    e(predict)
                               program used to implement predict
                               predictions allowed by margins
    e(marginsok)
Matrices
    e(b)
                               coefficient vector
    e(V)
                               variance-covariance matrix of the estimators
Functions
    e(sample)
                               marks estimation sample
```

In addition to the above, the following is stored in r():

```
Matrices
                                  matrix containing the coefficients with their standard errors, test statistics, p-values, and
     r(table)
                                      confidence intervals
```

Note that results stored in r() are updated when the command is replayed and will be replaced when any r-class command is run after the estimation command.

Methods and formulas

A dynamic panel-data model has the form

$$y_{it} = \sum_{j=1}^{p} \alpha_j y_{i,t-j} + \mathbf{x}_{it} \boldsymbol{\beta}_1 + \mathbf{w}_{it} \boldsymbol{\beta}_2 + \nu_i + \epsilon_{it} \quad i = 1, \dots, N \quad t = 1, \dots, T_i$$
 (1)

where

the α_i are p parameters to be estimated,

 \mathbf{x}_{it} is a 1 \times k_1 vector of strictly exogenous covariates,

 β_1 is a $k_1 \times 1$ vector of parameters to be estimated,

 \mathbf{w}_{it} is a $1 \times k_2$ vector of predetermined and endogenous covariates,

 β_2 is a $k_2 \times 1$ vector of parameters to be estimated,

 ν_i are the panel-level effects (which may be correlated with the covariates), and

 ϵ_{it} are i.i.d. over the whole sample with variance σ_{ϵ}^2 .

The ν_i and the ϵ_{it} are assumed to be independent for each i over all t.

By construction, the lagged dependent variables are correlated with the unobserved panel-level effects, making standard estimators inconsistent. With many panels and few periods, estimators are constructed by first-differencing to remove the panel-level effects and using instruments to form moment conditions.

xtabond uses a GMM estimator to estimate $\alpha_1, \ldots, \alpha_n, \beta_1$, and β_2 . The moment conditions are formed from the first-differenced errors from (1) and instruments. Lagged levels of the dependent variable, the predetermined variables, and the endogenous variables are used to form GMM-type instruments. See Arellano and Bond (1991) and Holtz-Eakin, Newey, and Rosen (1988) for discussions of GMM-type instruments. First differences of the strictly exogenous variables are used as standard instruments.

xtabond uses xtdpd to perform its computations, so the formulas are given in Methods and formulas of [XT] xtdpd.

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Also see

- [XT] **xtabond postestimation** Postestimation tools for xtabond
- [XT] **xtdpd** Linear dynamic panel-data estimation
- [XT] xtdpdsys Arellano-Bover/Blundell-Bond linear dynamic panel-data estimation
- [XT] xtivreg Instrumental variables and two-stage least squares for panel-data models
- [XT] **xtreg** Linear models for panel data
- [XT] **xtregar** Fixed- and random-effects linear models with an AR(1) disturbance
- [XT] **xtset** Declare data to be panel data
- [U] 20 Estimation and postestimation commands

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