Description Syntax Remarks and examples Conformability Diagnostics Also see

Description

qrsolve(A, B, ...) uses QR decomposition to solve AX = B and returns X. When A is singular or nonsquare, qrsolve() computes a least-squares generalized solution. When *rank* is specified, in it is placed the rank of A.

 $_qrsolve(A, B, ...)$, does the same thing, except that it destroys the contents of A and it overwrites B with the solution. Returned is the rank of A.

In both cases, *tol* specifies the tolerance for determining whether A is of full rank. *tol* is interpreted in the standard way—as a multiplier for the default if tol > 0 is specified and as an absolute quantity to use in place of the default if $tol \le 0$ is specified; see [M-1] **Tolerance**.

Syntax

numerie mainix qiborve(1, D)	
<pre>numeric matrix qrsolve(A, B, rank)</pre>	
<pre>numeric matrix qrsolve(A, B, rank,</pre>	tol)
real scalar _qrsolve(A, B)	
real scalarqrsolve(A, B, tol)	

where

A:	numeric matrix
<i>B</i> :	numeric matrix
rank:	irrelevant; real scalar returned
tol:	real scalar

Remarks and examples

qrsolve(A, B, ...) is suitable for use with square and possibly rank-deficient matrix A, or when A has more rows than columns. When A is square and full rank, qrsolve() returns the same solution as lusolve() (see [M-5] lusolve()), up to roundoff error. When A is singular, qrsolve() returns a generalized (least-squares) solution.

Remarks are presented under the following headings:

Derivation Relationship to inversion Tolerance

Derivation

We wish to solve for X

$$AX = B \tag{1}$$

Perform QR decomposition on A so that we have A = QRP'. Then (1) can be rewritten as

QRP'X = B

Premultiplying by Q' and remembering that Q'Q = QQ' = I, we have

$$RP'X = Q'B \tag{2}$$

Define

$$Z = P'X \tag{3}$$

Then (2) can be rewritten as

$$RZ = Q'B \tag{4}$$

It is easy to solve (4) for Z because R is upper triangular. Having Z, we can obtain X via (3), because Z = P'X, premultiplied by P (and if we remember that PP' = I), yields

$$X = PZ$$

For more information on QR decomposition, see [M-5] qrd().

Relationship to inversion

For a general discussion, see Relationship to inversion in [M-5] lusolve().

For an inverse based on QR decomposition, see [M-5] **qrinv()**. qrinv(A) amounts to qrsolve(A, I(rows(A))), although it is not actually implemented that way.

Tolerance

The default tolerance used is

$$eta = 1e-13 * trace(abs(R))/rows(R)$$

where R is the upper-triangular matrix of the QR decomposition; see *Derivation* above. When A is less than full rank, by, say, d degrees of freedom, then R is also rank deficient by d degrees of freedom and the bottom d rows of R are essentially zero. If the *i*th diagonal element of R is less than or equal to *eta*, then the *i*th row of Z is set to zero. Thus if the matrix is singular, qrsolve() provides a generalized solution.

If you specify tol > 0, the value you specify is used to multiply *eta*. You may instead specify $tol \le 0$, and then the negative of the value you specify is used in place of *eta*; see [M-1] **Tolerance**.

Conformability

qrsolve(A ,	B, rank, to	l):	
input:			
	A:	$m \times n$,	$m \ge n$
	<i>B</i> :	$m \times k$	
	tol:	1×1	(optional)
output:			
	rank:	1×1	(optional)
	result:	$n \times k$	
_qrsolve(A	, B, tol):		
input:			
	A:	$m \times n$,	$m \ge n$
	<i>B</i> :	$m \times k$	
	tol:	1×1	(optional)
output:			
	A:	0 imes 0	
	<i>B</i> :	$n \times k$	
	result:	1×1	

Diagnostics

qrsolve(A, B, ...) and $_qrsolve(A, B, ...)$ return a result containing missing if A or B contain missing values.

 $_qrsolve(A, B, ...)$ aborts with error if A or B are views.

Also see

- [M-5] cholsolve() Solve AX=B for X using Cholesky decomposition
- [M-5] lusolve() Solve AX=B for X using LU decomposition
- [M-5] qrd() QR decomposition
- [M-5] qrinv() Generalized inverse of matrix via QR decomposition
- [M-5] solvelower() Solve AX=B for X, A triangular
- [M-5] _solvemat() Solve AX=B for X
- [M-5] solve_tol() Tolerance used by solvers and inverters
- [M-5] svsolve() Solve AX=B for X using singular value decomposition
- [M-4] Matrix Matrix functions

[M-4] Solvers — Functions to solve AX=B and to obtain A inverse

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