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Intro 1 — Interpretation of choice models

Description Remarks and examples Also see

Description

Choice models have a reputation for being difficult to interpret. The coefficients that we estimate when we fit a choice model rarely allow a researcher to directly test hypotheses of interest. From the sign of the coefficient, we can determine the direction of an effect, and in the cases of conditional logit and mixed logit models, we can compute odds ratios and relative-risk ratios. Beyond this, the coefficients are almost uninterpretable.

There is no need for concern, however. Stata has a unique command, margins, that can be used after any of the cm choice model commands to easily answer questions of real scientific interest. In this entry, we introduce you to margins, and we give you a preview of the types of inferences that you can make when you use margins with the results of your choice models. To stay focused, we use cmclogit to fit all models in this introduction. That is not a limitation. The inferences we make and the associated margins commands would be the same for any of the cm estimation commands.

Remarks and examples

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Remarks are presented under the following headings:

Interpretation of coefficients
Inferences from margins
Expected choice probabilities
Effects of a continuous covariate
Effects of a categorical covariate
Effects of an alternative-specific covariate
More inferences using margins

Interpretation of coefficients

We demonstrate with a transportation example. We have 210 individuals who choose a method of travel between two cities—by airplane, train, bus, or car. We also have information on the length of time each method will take, each individual's income, and the number of people traveling together.

```
. use https://www.stata-press.com/data/r18/travel
(Modes of travel)
. generate time = traveltime+termtime
```

Above, we generated a time variable representing total travel time. We use cmset to specify that the id variable identifies the travelers and the mode variable records the possible methods of travel, called alternatives. Then, we fit a conditional logistic regression model where choice indicates the selected travel method. Of our covariates, time is the only one that varies across the four travel alternatives. income and partysize are listed in the casevars() option because they have only one value per individual (or case) rather than a value for each alternative.

```
. cmset id mode

Case ID variable: id

Alternatives variable: mode
```

```
. cmclogit choice time, casevars(income partysize)
Iteration 0: Log likelihood = -249.36629
Iteration 1: Log likelihood = -236.01608
              Log likelihood = -235.65162
Iteration 2:
Iteration 3:
              Log likelihood = -235.65065
              Log likelihood = -235.65065
Iteration 4:
Conditional logit choice model
                                                 Number of obs
                                                                              840
Case ID variable: id
                                                 Number of cases
                                                                              210
Alternatives variable: mode
                                                                                4
                                                 Alts per case: min =
                                                                              4.0
                                                                avg =
                                                                                4
                                                    Wald chi2(7)
                                                                            71.14
Log likelihood = -235.65065
                                                    Prob > chi2
                                                                           0.0000
      choice
               Coefficient
                             Std. err.
                                                  P>|z|
                                                            [95% conf. interval]
                                             z
mode
        time
                -.0041641
                             .0007588
                                         -5.49
                                                  0.000
                                                           -.0056512
                                                                         -.002677
Air
                 (base alternative)
Train
                                         -5.00
                -.0613414
                             .0122637
                                                  0.000
                                                           -.0853778
                                                                        -.0373051
      income
   partysize
                  .4123606
                             .2406358
                                          1.71
                                                  0.087
                                                           -.0592769
                                                                          .883998
                   3.39349
                             .6579166
                                          5.16
                                                  0.000
                                                            2.103997
                                                                         4.682982
       _cons
Bus
                -.0363345
                             .0134318
                                         -2.71
                                                  0.007
                                                           -.0626605
                                                                        -.0100086
      income
   partysize
                 -.1370778
                             .3437092
                                         -0.40
                                                  0.690
                                                           -.8107354
                                                                         .5365798
                                          3.81
       _cons
                  2.919314
                             .7658496
                                                  0.000
                                                            1.418276
                                                                         4.420351
Car
                -.0096347
                             .0111377
                                         -0.87
                                                  0.387
                                                           -.0314641
                                                                         .0121947
      income
   partysize
                  .7350802
                             .2184636
                                          3.36
                                                  0.001
                                                            .3068993
                                                                         1.163261
       _cons
                  .7471042
                             .6732971
                                           1.11
                                                  0.267
                                                           -.5725338
                                                                         2.066742
```

What can we determine from these results? The coefficient on time is negative, so the probability of choosing a method of travel decreases as the travel time increases. For the train alternative, the coefficient on income is negative. Because air travel is the base alternative, this negative coefficient tells us that as income increases, people are less likely to choose a train over an airplane. For the car alternative, the coefficient on partysize is positive. As party size increases, people are more likely to choose a car over an airplane.

Inferences from margins

The output from cmclogit, or from any other cm command, gives us a little information. However, it does not typically answer questions a researcher is truly interested in. In our example, for instance, we might want to know the following:

- What percentage of individuals do we expect to choose air travel?
- What is the effect of income? How does the probability of selecting car travel change as income increases from \$30,000 to \$40,000 or from \$40,000 to \$50,000? How does the probability of selecting train travel change?
- What if new security measures are implemented and wait times at the airport increase by 60 minutes? How does that affect the probability of choosing each method of travel?

We can answer each of these questions and many others using margins.

Expected choice probabilities

Let's start with the first question. We simply type margins without any options to obtain the average predicted probability of choosing each method of travel.

. margins

Predictive margins Number of obs = 840

Model VCE: 0IM

Expression: Pr(mode|1 selected), predict()

	Margin	Delta-method std. err.	z	P> z	[95% conf.	interval]
_outcome						
Air	.2761905	.0275268	10.03	0.000	.2222389	.330142
Train	.3	.0284836	10.53	0.000	.2441731	.3558269
Bus	.1428571	.0234186	6.10	0.000	.0969576	.1887567
Car	.2809524	.028043	10.02	0.000	.2259891	.3359156

Based on this model and our random sample of travelers between the two cities, we expect 28% of individuals to travel by air. We also expect 30% to travel by train, 14% to travel by bus, and 28% to travel by car.

Effects of a continuous covariate

What does our model say would happen if values of a covariates change? We will first explore the effect of income. What would the expected probability of choosing car travel be if everyone made \$30,000? What if everyone made \$40,000? We can estimate expected probabilities of car travel for counterfactual income levels from \$30,000 to \$70,000 in \$10,000 increments by using the at() option with margins. We type

. margins, at(income=(30(10)70)) outcome(Car)

Predictive margins

Model VCE: OIM

Expression: Pr(mode|1 selected), predict()

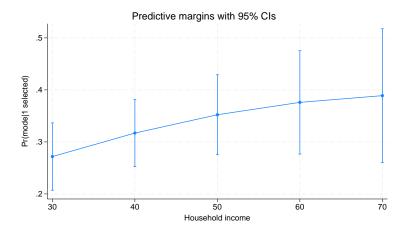
Outcome: 1._at: income = 30 $2._at: income = 40$ 3._at: income = 50 4._at: income = 60 5. at: income = 70

	Margin	Delta-method std. err.	z	P> z	[95% conf.	interval]
_at						
1	.2717914	.0329811	8.24	0.000	.2071497	.3364331
2	.3169817	.0329227	9.63	0.000	.2524544	.3815091
3	.3522391	.0391994	8.99	0.000	.2754097	.4290684
4	.3760093	.050679	7.42	0.000	.2766802	.4753383
5	.3889296	.0655865	5.93	0.000	.2603825	.5174768

We can plot these probabilities to visualize the effect of income.

. marginsplot

Variables that uniquely identify margins: income



The expected probability of choosing car transportation increases as income increases. But are these differences statistically significant? We can test for differences in the expected probabilities for each \$10,000 increase in income. For this, we use the contrast() option and request reverse adjacent (ar) contrasts. We also simplify the output that reports a test of the differences by including the nowald and effects options.

```
. margins, at(income=(30(10)70)) outcome(Car)
```

> contrast(atcontrast(ar) nowald effects)

Contrasts of predictive margins

Model VCE: OIM

Expression: Pr(mode|1 selected), predict()

Outcome: Car
1._at: income = 30
2._at: income = 40
3._at: income = 50
4._at: income = 60

 $5._at: income = 70$

Number of obs = 840	Number	of	obs	=	840
-----------------------	--------	----	-----	---	-----

	Contrast	Delta-method std. err.	z	P> z	[95% conf.	interval]
_at (2 vs 1) (3 vs 2) (4 vs 3) (5 vs 4)	.0451903	.016664	2.71	0.007	.0125296	.0778511
	.0352574	.017903	1.97	0.049	.0001681	.0703466
	.0237702	.0190387	1.25	0.212	013545	.0610854
	.0129204	.0200549	0.64	0.519	0263866	.0522273

From the first line in this table, we see that the effect of having \$40,000 instead of \$30,000 is a 0.045 increase in the expected probability of selecting car travel. Having \$50,000 instead of \$40,000 increases the expected probability of car travel by 0.035. Both of these effects are significant at a 5% significance level, but increases in income from \$50,000 to \$60,000 and from \$60,000 to \$70,000 do not lead to significantly different probabilities of car travel.

We can also evaluate the effect of income on the probability of taking a train. We include the outcome(Train) option instead of outcome(Car) in our margins command.

. margins, at(income=(30(10)70)) outcome(Train)

Predictive margins

Model VCE: OIM

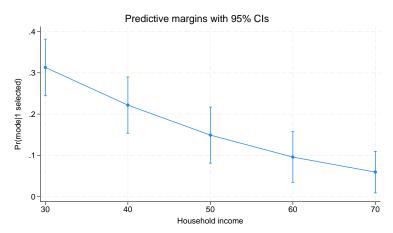
Expression: Pr(mode|1 selected), predict()

Outcome: Train 1._at: income = 30 2._at: income = 40 3._at: income = 50 4._at: income = 60 5._at: income = 70

	Margin	Delta-method std. err.	z	P> z	[95% conf.	interval]
_at						
1	.3129898	.034968	8.95	0.000	.2444538	.3815257
2	.2217291	.0346969	6.39	0.000	.1537244	.2897338
3	.1491281	.0346442	4.30	0.000	.0812268	.2170294
4	.0959391	.0313489	3.06	0.002	.0344965	.1573818
5	.0595511	.0256786	2.32	0.020	.009222	.1098802

. marginsplot

Variables that uniquely identify margins: income



As income levels increase, the expected probability of choosing train transportation decreases.

We can again test for differences in the probabilities using reverse adjacent contrasts.

```
. margins, at(income=(30(10)70)) outcome(Train)
```

> contrast(atcontrast(ar) nowald effects)

Contrasts of predictive margins Number of obs = 840

Model VCE: OIM

Expression: Pr(mode|1 selected), predict()

Outcome: Train
1._at: income = 30
2._at: income = 40
3._at: income = 50
4._at: income = 60
5._at: income = 70

	Contrast	Delta-method std. err.	z	P> z	[95% conf.	interval]
_at (2 vs 1) (3 vs 2) (4 vs 3) (5 vs 4)	0912606 072601 053189 036388	.0174009 .0104846 .0066782	-5.24 -6.92 -7.96 -5.60	0.000 0.000 0.000 0.000	1253659 0931505 0662779 0491195	0571554 0520516 0401 0236566

This time, we find a significant decrease in the expected probability of choosing train transportation for each \$10,000 increase in income.

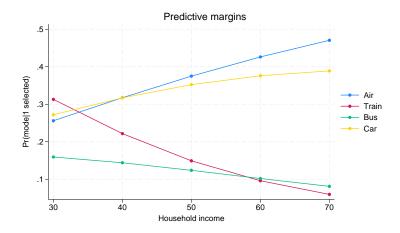
We do not need to limit our analysis to just car or train travel. How does the probability of each method of travel change with income?

We can type

. margins, at(income=(30(10)70))

This produces lots of output, so we do not show it here. We instead show you the graph of all the results. We omit the confidence intervals so that it is easy to see the probabilities for all four methods of travel.

. marginsplot, noci
Variables that uniquely identify margins: income _outcome



Number of obs = 840

As income goes up, the expected probabilities of selecting bus and train transportation decrease, and the expected probabilities of choosing air and car transportation increase.

This graph allows us to visually compare the travel methods at each income level. We can formally test for differences in the expected probabilities of the travel methods. For instance, at the \$30,000 income level, are all four methods of travel equally likely to be selected? We can use the contrast(outcomejoint) option to request this test.

. margins, at(income=30) contrast(outcomejoint)

Contrasts of predictive margins

Model VCE: OIM

Expression: Pr(mode|1 selected), predict()

At: income = 30

	df	chi2	P>chi2
_outcome	3	12.80	0.0051

We find that at least one of these expected probabilities is significantly different from the others.

We might want to ask a more specific question. Is there a difference in the expected probabilities of selecting train and bus travel when income is \$50,000? We use the outcome() option to specify these two methods of travel and the contrast(outcomecontrast(r)) option to request that margins estimate the difference between the two probabilities.

```
. margins, at(income=50) outcome(Bus Train)
```

> contrast(outcomecontrast(r) nowald effects)

Contrasts of predictive margins

Model VCE: OIM

Expression: Pr(mode|1 selected), predict()

At: income = 50

	Contrast	Delta-method std. err.	z	P> z	[95% conf.	interval]
_outcome (Bus vs Train)	0254125	.0504996	-0.50	0.615	1243899	.0735648

We do not find a significant difference in the probabilities of selecting bus and train travel at this income level.

Effects of a categorical covariate

The questions we answered above were about a continuous variable, income. What if we want to evaluate the effect of a categorical variable instead? We include the variable as a factor variable in our model and again use margins. To demonstrate, we create a variable representing income quartiles and change our model to use it rather than the continuous income covariate.

```
. xtile income_cat = income, nquantiles(4)
```

. label define quartiles 1 "Quartile 1" 2 "Quartile 2" 3 "Quartile 3" 4 "Quartile 4"

. label values income_cat quartiles

. cmclogit choice time, casevars(i.income_cat partysize) (output omitted)

We estimate the expected probability of selecting train travel for each income quartile by typing

. margins income_cat, outcome(Train)

Predictive margins Number of obs = 840

Model VCE: OIM

Expression: Pr(mode|1 selected), predict()

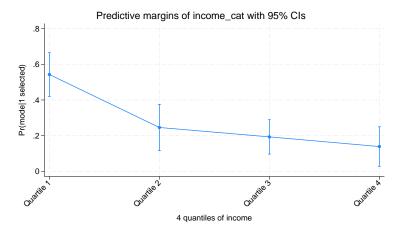
Outcome: Train

	Margin	Delta-method std. err.	z	P> z	[95% conf.	interval]
income_cat						
Quartile 1	.5424554	.0624929	8.68	0.000	.4199715	.6649392
Quartile 2	. 2459475	.0661098	3.72	0.000	.1163746	.3755203
Quartile 3	. 1933788	.0490343	3.94	0.000	.0972733	.2894843
Quartile 4	.1391895	.0563599	2.47	0.014	.0287262	.2496529

We can again plot the results using marginsplot.

. marginsplot

Variables that uniquely identify margins: income_cat



We use the ar. operator to test for differences in the expected probabilities across adjacent income quartiles. This time, we attach the contrast operator to the name of the variable.

. margins ar.income_cat, outcome(Train) contrast(nowald effects)

Number of obs = 840 Contrasts of predictive margins

Model VCE: OIM

Expression: Pr(mode|1 selected), predict()

Outcome: Train

	Contrast	Delta-method std. err.	z	P> z	[95% conf.	interval]
income_cat (Quartile 2						
vs Quartile 1) (Quartile 3	2965079	.0905087	-3.28	0.001	4739018	1191141
vs Quartile 2) (Quartile 4	0525687	.082642	-0.64	0.525	214544	.1094067
vs Quartile 3)	0541893	.0744351	-0.73	0.467	2000794	.0917009

We find that the expected probability of choosing train travel is significantly different when moving from the first to the second income quartile.

Effects of an alternative-specific covariate

So far, we have explored the effects of the case-specific income variable. We can also ask questions about an alternative-specific variable such as travel time.

Perhaps new security measures are added. What would we expect if wait times at the airport increase by 60 minutes for all flights? We can use margins' at() option to evaluate this scenario.

. margins, at(time=generate(time+60)) alternative(Air)

Predictive margins Number of obs = 840

Model VCE: OIM

Expression: Pr(mode|1 selected), predict()

Alternative: Air At: time = time+60

	Margin	Delta-method std. err.	z	P> z	[95% conf.	interval]
_outcome						
Air	.238248	.0261139	9.12	0.000	.1870657	.2894303
Train	.3138431	.0293829	10.68	0.000	.2562537	.3714325
Bus	.1513295	.0243434	6.22	0.000	.1036173	.1990417
Car	.2965794	.0289688	10.24	0.000	.2398016	.3533572

As we would anticipate, the expected probability of selecting air travel decreases when travel time increases. The probability of choosing air travel is now 0.24. If we look back at our first margins command, we can see that with the original travel times, the expected probability of choosing air travel was 0.28. Rather than looking at results from multiple commands, we can estimate probabilities with the original travel times and with the increased travel times all with a single margins command.

```
. margins, at(time=generate(time)) at(time=generate(time+60))
> alternative(Air)
```

Predictive margins Number of obs = 840

Model VCE: OIM

Expression: Pr(mode|1 selected), predict()

Alternative: Air
1._at: time = time
2._at: time = time+60

	Margin	Delta-method std. err.	z	P> z	[95% conf.	interval]
_outcome#_at						
Air#1	.2761905	.0277787	9.94	0.000	.2217453	.3306357
Air#2	.238248	.0261139	9.12	0.000	.1870657	.2894303
Train#1	.3	.0284715	10.54	0.000	.2441968	.3558032
Train#2	.3138431	.0293829	10.68	0.000	.2562537	.3714325
Bus#1	.1428571	.0232375	6.15	0.000	.0973125	.1884018
Bus#2	.1513295	.0243434	6.22	0.000	.1036173	.1990417
Car#1	.2809524	.0280657	10.01	0.000	.2259446	.3359602
Car#2	.2965794	.0289688	10.24	0.000	.2398016	.3533572

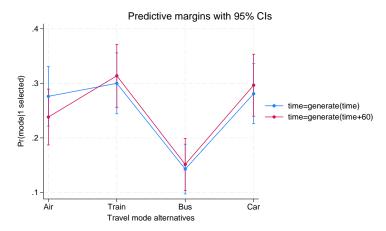
Now it is easy to plot both scenarios together using marginsplot. This time we include the xdimension() option to place the four travel choices along the x axis.

```
. marginsplot, xdimension(_outcome)
```

Variables that uniquely identify margins: _atopt _outcome

Multiple at() options specified:

_atoption=1: time=generate(time)
_atoption=2: time=generate(time+60)



We see that the probability of air travel decreases, while the probability of choosing each of the other methods of travel increases a little.

We can again use contrasts to test for a difference. We use the atcontrast(r) to request comparisons to a reference level (the original travel times).

. margins, at(time=generate(time)) at(time=generate(time+60))

> alternative(Air) contrast(atcontrast(r) nowald effects)

Contrasts of predictive margins

Number of obs = 840

Model VCE: OIM

Expression: Pr(mode|1 selected), predict()

Alternative: Air 1._at: time = $2._at: time = time+60$

	Contrast	Delta-method std. err.	z	P> z	[95% conf	. interval]
_at@_outcome (2 vs 1) Air (2 vs 1)	0379425	.0056615	-6.70	0.000	0490387	0268462
Train (2 vs 1) Bus (2 vs 1) Car	.0138431 .0084724 .015627	.0027216 .001936 .0026002	5.09 4.38 6.01	0.000 0.000 0.000	.0085089 .004678 .0105308	.0191773 .0122668 .0207232

Each of these differences is statistically significant. Of course, the researcher would need to decide whether an expected 3.8 percentage point decrease in air travel is meaningful.

We might take this even one step further. What if the speed of train transportation improves at the same time that speed of air travel declines? What if train travel is now 60 minutes faster while air travel is 60 minutes slower? We cannot specify all of these changes directly in the at() option, but we can create a new variable that represents this scenario.

```
. generate newtime = time
. replace newtime = time+60 if mode==1
(210 real changes made)
. replace newtime = time-60 if mode==2
```

(210 real changes made)

Now we can specify our newtime variable in the at() option. We also include the alternative(simultaneous) option to specify that the changes to air and train travel be made simultaneously. . margins, at(time=generate(time)) at(time=generate(newtime))

> alternative(simultaneous)

Predictive margins Number of obs = 840

Model VCE: OIM

Expression: Pr(mode|1 selected), predict()

1._at: time = time 2. at: time = newtime

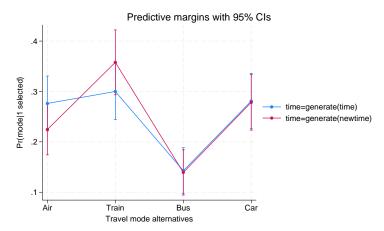
	1	Delta-method				
	Margin	std. err.	z	P> z	[95% conf.	interval]
_outcome#_at						
Air#1	.2761905	.0277787	9.94	0.000	.2217453	.3306357
Air#2	.224539	.0256826	8.74	0.000	.1742021	.274876
Train#1	.3	.0284715	10.54	0.000	.2441968	.3558032
Train#2	.3578287	.0328487	10.89	0.000	.2934464	.4222111
Bus#1	.1428571	.0232375	6.15	0.000	.0973125	.1884018
Bus#2	.1392549	.0228972	6.08	0.000	.0943773	.1841325
Car#1	.2809524	.0280657	10.01	0.000	.2259446	.3359602
Car#2	.2783773	.0281348	9.89	0.000	.2232342	.3335205

. marginsplot, xdimension(_outcome)

Variables that uniquely identify margins: _atopt _outcome

Multiple at() options specified:

_atoption=1: time=generate(time) _atoption=2: time=generate(newtime)



Now it appears that the expected probability of selecting air travel decreases, the expected probability of selecting train travel increases, and the expected probabilities of selecting the other methods of transportation do not change much. Let's test for differences.

```
. margins, at(time=generate(time)) at(time=generate(newtime))
```

> alternative(simultaneous) contrast(atcontrast(r) nowald effects)

Contrasts of predictive margins

Model VCE: OIM

Expression: Pr(mode|1 selected), predict()

1._at: time = time
2._at: time = newtime

	Contrast	Delta-method std. err.	z	P> z	[95% conf.	. interval]
_at@_outcome (2 vs 1) Air (2 vs 1)	0516514	.0080654	-6.40	0.000	0674594	0358435
Train (2 vs 1) Bus	.0578287	.0109404	5.29 -1.57	0.000	.0363859	.0792716
(2 vs 1) Car	002575	.0036587	-0.70	0.482	009746	.0045959

Now the expected probability of selecting air travel is 5.2 percentage points lower than it was with the original travel times, and the expected probability of selecting train travel is 5.7 percentage points higher.

More inferences using margins

Here we have demonstrated how you can use the results of your choice model to answer some interesting questions. But this is just a small sample of the types of inference that you can do using margins after a choice model estimator. For more examples, see [CM] margins, [CM] Intro 5, [CM] Intro 6, [CM] cmclogit, [CM] cmmixlogit, and [CM] cmxtmixlogit. Regardless of the cm command you use to fit your model, you may be interested in all of these examples because the same margins commands can be used after any of the models to estimate the same types of margins and test the same types of hypotheses.

Also see

[CM] margins — Adjusted predictions, predictive margins, and marginal effects

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