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estat aroots — Check the stability condition of ARIMA estimates

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Description

estat aroots checks the eigenvalue stability condition after estimating the parameters of an ARIMA model using arima. A graph of the eigenvalues of the companion matrices for the AR and MA polynomials is also produced.

estat aroots is available only after arima; see [TS] arima.

Quick start

Verify that all eigenvalues of the autoregressive polynomial lie inside the unit circle after arima estat aroots

Same as above, but suppress the graph estat aroots, nograph

Label each plotted eigenvalue with its distance from the unit circle estat aroots, dlabel

Menu for estat

Statistics > Postestimation

Syntax

```
estat aroots [, options]
```

options	Description		
nograph	suppress graph of eigenvalues for the companion matrices		
<u>d</u> label	label eigenvalues with the distance from the unit circle		
$\underline{\mathtt{mod}}$ label	label eigenvalues with the modulus		
Grid			
nogrid	suppress polar grid circles		
$ exttt{pgrid}(ig[\dotsig])$	specify radii and appearance of polar grid circles; see Options for details		
Plot			
marker_options	change look of markers (color, size, etc.)		
Reference unit circle			
<pre>rlopts(cline_options)</pre>	affect rendition of reference unit circle		
Y axis, X axis, Titles, Legend,	Overall		
twoway_options	any options other than by () documented in [G-3] twoway_options		
collect is allowed; see [II]	11.1.10 Profix commands		

collect is allowed; see [U] 11.1.10 Prefix commands.

Options

nograph specifies that no graph of the eigenvalues of the companion matrices be drawn.

dlabel labels each eigenvalue with its distance from the unit circle. dlabel cannot be specified with modlabel.

modlabel labels the eigenvalues with their moduli. modlabel cannot be specified with dlabel.

Grid _____

nogrid suppresses the polar grid circles.

pgrid([numlist] [, line_options]) determines the radii and appearance of the polar grid circles. By default, the graph includes nine polar grid circles with radii 0.1, 0.2, ..., 0.9 that have the grid line style. The numlist specifies the radii for the polar grid circles. The line_options determine the appearance of the polar grid circles; see [G-3] line_options. Because the pgrid() option can be repeated, circles with different radii can have distinct appearances.

Plot

marker_options specify the look of markers. This look includes the marker symbol, the marker size, and its color and outline; see [G-3] marker_options.

Reference unit circle

rlopts (cline_options) affect the rendition of the reference unit circle; see [G-3] cline_options.

```
Y axis, X axis, Titles, Legend, Overall
```

twoway_options are any of the options documented in [G-3] twoway_options, except by(). These include options for titling the graph (see [G-3] title_options) and for saving the graph to disk (see [G-3] saving_option).

Remarks and examples

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Inference after arima requires that the variable y_t be covariance stationary. The variable y_t is covariance stationary if its first two moments exist and are time invariant. More explicitly, y_t is covariance stationary if

- 1. $E(y_t)$ is finite and not a function of t;
- 2. $Var(y_t)$ is finite and independent of t; and
- 3. $Cov(y_t, y_s)$ is a finite function of |t s| but not of t or s alone.

The stationarity of an ARMA process depends on the autoregressive (AR) parameters. If the inverse roots of the AR polynomial all lie inside the unit circle, the process is stationary, invertible, and has an infinite-order moving-average (MA) representation. Hamilton (1994, chap. 1) shows that if the modulus of each eigenvalue of the matrix $\mathbf{F}(\rho)$ is strictly less than 1, the estimated ARMA is stationary; see *Methods and formulas* for the definition of the matrix $\mathbf{F}(\rho)$.

The MA part of an ARMA process can be rewritten as an infinite-order AR process provided that the MA process is invertible. Hamilton (1994, chap. 1) shows that if the modulus of each eigenvalue of the matrix $\mathbf{F}(\theta)$ is strictly less than 1, the estimated ARMA is invertible; see *Methods and formulas* for the definition of the matrix $\mathbf{F}(\theta)$.

▶ Example 1

In this example, we check the stability condition of the SARIMA model that we fit in example 3 of [TS] **arima**. We begin by reestimating the parameters of the model.

```
. use https://www.stata-press.com/data/r18/air2
(TIMESLAB: Airline passengers)
. generate lnair = ln(air)
```

. arima lnair, arima(0,1,1) sarima(0,1,1,12) noconstant

(setting optimization to BHHH)

 Iteration 0:
 Log likelihood = 223.8437

 Iteration 1:
 Log likelihood = 239.80405

 Iteration 2:
 Log likelihood = 244.10265

 Iteration 3:
 Log likelihood = 244.65895

 Iteration 4:
 Log likelihood = 244.68945

(switching optimization to BFGS)

Iteration 5: Log likelihood = 244.69431
Iteration 6: Log likelihood = 244.69647
Iteration 7: Log likelihood = 244.69651
Iteration 8: Log likelihood = 244.69651

ARIMA regression

Sample: 14 thru 144 Number of obs = 131 Wald chi2(2) = 84.53

Prob > chi2

0.0000

Log likelihood = 244.6965

DS12.lnair		Coefficient	OPG std. err.	z	P> z	[95% conf.	interval]
ARMA							
	ma						
	L1.	4018324	.0730307	-5.50	0.000	5449698	2586949
ARMA1	2						
	ma						
	L1.	5569342	.0963129	-5.78	0.000	745704	3681644
	/sigma	.0367167	.0020132	18.24	0.000	.0327708	.0406625

Note: The test of the variance against zero is one sided, and the two-sided confidence interval is truncated at zero.

We can now use estat aroots to check the stability condition of the MA part of the model.

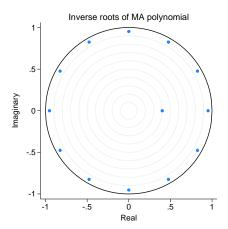
. estat aroots

Eigenvalue stability condition

Eigenvalue	Modulus	
.824798 + .4761974 <i>i</i>	.952395	
.8247984761974i	.952395	
. 9523947	.952395	
824798 + .4761974i	.952395	
8247984761974i	.952395	
4761974 + .824798i	.952395	
4761974824798i	.952395	
2.776e-16 + .9523947i	.952395	
2.776e-169523947i	.952395	
.4761974 + .824798i	.952395	
.4761974824798i	.952395	
9523947	.952395	
.4018324	.401832	
	I	

All the eigenvalues lie inside the unit circle. MA parameters satisfy invertibility condition.

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Because the modulus of each eigenvalue is strictly less than 1, the MA process is invertible and can be represented as an infinite-order AR process.

The graph produced by estat aroots displays the eigenvalues with the real components on the x axis and the imaginary components on the y axis. The graph indicates visually that these eigenvalues are just inside the unit circle.

Stored results

estat aroots stores the following in r():

Matrices

real part of the eigenvalues of $F(\rho)$ r(Re_ar) r(Im_ar) imaginary part of the eigenvalues of $F(\rho)$ r(Modulus_ar) modulus of the eigenvalues of $F(\rho)$ r(ar) $F(\rho)$, the AR companion matrix r(Re_ma) real part of the eigenvalues of $F(\theta)$ r(Im_ma) imaginary part of the eigenvalues of $F(\theta)$ r(Modulus_ma) modulus of the eigenvalues of $F(\theta)$ r(ma) $F(\theta)$, the MA companion matrix

Methods and formulas

Recall the general form of the ARMA model,

$$\boldsymbol{\rho}(L^p)(y_t - \mathbf{x}_t \boldsymbol{\beta}) = \boldsymbol{\theta}(L^q)\epsilon_t$$

where

$$\rho(L^p) = 1 - \rho_1 L - \rho_2 L^2 - \dots - \rho_p L^p$$

$$\theta(L^q) = 1 + \theta_1 L + \theta_2 L^2 + \dots + \theta_q L^q$$

and
$$L^j y_t = y_{t-j}$$
.

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estat aroots forms the companion matrix

$$\mathbf{F}(\gamma) = \begin{pmatrix} \gamma_1 & \gamma_2 & \dots & \gamma_{r-1} & \gamma_r \\ 1 & 0 & \dots & 0 & 0 \\ 0 & 1 & \dots & 0 & 0 \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ 0 & 0 & \dots & 1 & 0 \end{pmatrix}$$

where $\gamma=\rho$ and r=p for the AR part of ARMA, and $\gamma=-\theta$ and r=q for the MA part of ARMA. aroots obtains the eigenvalues of ${\bf F}$ by using matrix eigenvalues. The modulus of the complex eigenvalue $r+c{\bf i}$ is $\sqrt{r^2+c^2}$. As shown by Hamilton (1994, chap. 1), a process is stable and invertible if the modulus of each eigenvalue of ${\bf F}$ is strictly less than 1.

Reference

Hamilton, J. D. 1994. Time Series Analysis. Princeton, NJ: Princeton University Press.

Also see

[TS] arima — ARIMA, ARMAX, and other dynamic regression models

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