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streg postestimation — Postestimation tools for streg

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## **Postestimation commands**

The following postestimation command is of special interest after streg:

Command	Description
*estat gofplot	produce goodness-of-fit plot
stcurve	plot the survivor, failure, hazard, or cumulative hazard function

<sup>\*</sup>estat gofplot is not appropriate with svy estimation results.

The following standard postestimation commands are also available:

Command	Description		
contrast	contrasts and ANOVA-style joint tests of estimates		
estat ic	Akaike's, consistent Akaike's, corrected Akaike's, and Schwarz's Bayesian information criteria (AIC, CAIC, AICc, and BIC)		
estat summarize	summary statistics for the estimation sample		
estat vce	variance-covariance matrix of the estimators (VCE)		
estat (svy)	postestimation statistics for survey data		
estimates	cataloging estimation results		
etable	table of estimation results		
*hausman	Hausman's specification test		
lincom	point estimates, standard errors, testing, and inference for linear combinations of coefficients		
linktest	link test for model specification		
*lrtest	likelihood-ratio test		
margins	marginal means, predictive margins, marginal effects, and average marginal effects		
marginsplot	graph the results from margins (profile plots, interaction plots, etc.)		
nlcom	point estimates, standard errors, testing, and inference for nonlinear combinations of coefficients		
predict	hazard ratios, survivor functions, influence statistics, residuals, etc.		
predictnl	point estimates, standard errors, testing, and inference for generalized predictions		
pwcompare	pairwise comparisons of estimates		
suest	seemingly unrelated estimation		
test	Wald tests of simple and composite linear hypotheses		
testnl	Wald tests of nonlinear hypotheses		

<sup>\*</sup>hausman and lrtest are not appropriate with svy estimation results.

predict [type] newvar [if] [in] [, statistic options]

# predict

## **Description for predict**

predict creates a new variable containing predictions such as median and mean survival times; hazards; hazard ratios; linear predictions; standard errors; probabilities; Cox–Snell, martingale-like, and deviance residuals.

### Menu for predict

Statistics > Postestimation

# Syntax for predict

```
predict [type] stub* [if] [in], scores
 statistic
                           Description
Main
 median time
                           median survival time; the default
 median Intime
                           median ln(survival time)
 mean time
                           mean survival time
 mean Intime
                           mean ln(survival time)
                           hazard
 hazard
                           hazard ratio, also known as the relative hazard
 hr
                           linear prediction \mathbf{x}_i \hat{\boldsymbol{\beta}}
 xb
                           standard error of the linear prediction; SE(\mathbf{x}_i \widehat{\boldsymbol{\beta}})
 stdp
                           S(t|t_0)
 surv
*csurv
                           S(t | \text{earliest } t_0 \text{ for subject})
^*csnell
                           Cox-Snell residuals
 mgale
                           martingale-like residuals
 deviance
                           deviance residuals
```

options	Description
oos	make statistic available in and out of sample
<u>nooff</u> set	ignore the offset() variable specified in streg
alpha1	predict statistic conditional on frailty value equal to one
$\frac{\overline{\underline{\underline{\underline{\underline{uncond}}}}}$ itional	predict statistic unconditionally on the frailty
marginal	synonym for unconditional
partial	produce observation-level results

Unstarred statistics are available both in and out of sample; type predict ... if e(sample) ... if wanted only for the estimation sample. Starred statistics are calculated for the estimation sample by default, but the oos option makes them available both in and out of sample.

When no option is specified, the predicted median survival time is calculated for all models. The predicted hazard ratio, option hr, is available only for the exponential, Weibull, and Gompertz models. The mean time and mean Intime options are not available for the Gompertz model. Unconditional estimates of mean time and mean 1ntime are not available if frailty() was specified with streg; see [ST] streg.

csnell, mgale, and deviance are not allowed with svy estimation results.

#### Options for predict

median time calculates the predicted median survival time in analysis-time units. This is the prediction from time 0 conditional on constant covariates. When no options are specified with predict, the predicted median survival time is calculated for all models.

median Intime calculates the natural logarithm of what median time produces.

mean time calculates the predicted mean survival time in analysis-time units. This is the prediction from time 0 conditional on constant covariates. This option is not available for Gompertz regressions and is available for frailty models only if alpha1 is specified, in which case what you obtain is an estimate of the mean survival time conditional on a frailty effect of one.

mean Intime predicts the mean of the natural logarithm of time. This option is not available for Gompertz regression and is available for frailty models only if alpha1 is specified, in which case what you obtain is an estimate of the mean log survival-time conditional on a frailty effect of one.

hazard calculates the predicted hazard.

hr calculates the hazard ratio. This option is valid only for models having a proportional-hazards parameterization.

xb calculates the linear prediction from the fitted model. That is, you fit the model by estimating a set of parameters,  $\beta_0, \beta_1, \beta_2, \dots, \beta_k$ , and the linear prediction is  $\widehat{y}_j = \widehat{\beta}_0 + \widehat{\beta}_1 x_{1j} + \widehat{\beta}_2 x_{2j} + \dots + \widehat{\beta}_k x_{kj}$ , often written in matrix notation as  $\hat{y}_j = \mathbf{x}_j \hat{\boldsymbol{\beta}}$ .

The  $x_{1j}, x_{2j}, \ldots, x_{kj}$  used in the calculation are obtained from the data currently in memory and need not correspond to the data on the independent variables used in estimating  $\beta$ .

stdp calculates the standard error of the prediction, that is, the standard error of  $\hat{y}_i$ .

surv calculates each observation's predicted survivor probability,  $S(t|t_0)$ , where  $t_0$  is  $_{-}$ t0, the analysis time at which each record became at risk. For multiple-record data, see the csurv option below.

csurv calculates the predicted  $S(t|earliest t_0)$  for each subject in multiple-record data by calculating the conditional survivor values,  $S(t|t_0)$  (see the surv option above), and then multiplying them.

What you obtain from surv will differ from what you obtain from csurv only if you have multiple records for that subject.

In the presence of gaps or delayed entry, the estimates obtained from csurv can be different for subjects with gaps from those without gaps, having the same covariate values, because the probability of survival over gaps is assumed to be 1. Thus the predicted cumulative conditional survivor function is not a smooth function of time \_t for constant values of the covariates. Use stcurve, survival to obtain a smooth estimate of the cumulative survivor function S(t|x).

csnell calculates the Cox-Snell generalized residuals. For multiple-record-per-subject data, by default only one value per subject is calculated and it is placed on the last record for the subject.

Adding the partial option will produce partial Cox-Snell residuals, one for each record within subject; see partial below. Partial Cox-Snell residuals are the additive contributions to a subject's overall Cox-Snell residual. In single-record-per-subject data, the partial Cox-Snell residuals are the Cox-Snell residuals.

mgale calculates the martingale-like residuals. For multiple-record data, by default only one value per subject is calculated and it is placed on the last record for the subject.

Adding the partial option will produce partial martingale residuals, one for each record within subject; see partial below. Partial martingale residuals are the additive contributions to a subject's overall martingale residual. In single-record data, the partial martingale residuals are the martingale residuals.

deviance calculates the deviance residuals. Deviance residuals are martingale residuals that have been transformed to be more symmetric about zero. For multiple-record data, by default only one value per subject is calculated and it is placed on the last record for the subject.

Adding the partial option will produce partial deviance residuals, one for each record within subject; see partial below. Partial deviance residuals are transformed partial martingale residuals. In single-record data, the partial deviance residuals are the deviance residuals.

oos makes csurv, csnell, mgale, and deviance available both in and out of sample. oos also dictates that summations and other accumulations take place over the sample as defined by if and in. By default, the summations are taken over the estimation sample, with if and in merely determining which values of *newvar* are to be filled in once the calculation is finished.

nooffset is relevant only if you specified offset (*varname*) with streg. It modifies the calculations made by predict so that they ignore the offset variable; the linear prediction is treated as  $x\beta$  rather than  $x\beta$  + offset.

alpha1, when used after fitting a frailty model, specifies that *statistic* be predicted conditional on a frailty value equal to one. This is the default for shared-frailty models.

unconditional and marginal, when used after fitting a frailty model, specify that *statistic* be predicted unconditional on the frailty. That is, the prediction is averaged over the frailty distribution. This is the default for unshared-frailty models.

partial is relevant only for multiple-record data and is valid with csnell, mgale, and deviance. Specifying partial will produce "partial" versions of these statistics, where one value is calculated for each record instead of one for each subject. The subjects are determined by the id() option of stset.

Specify partial if you wish to perform diagnostics on individual records rather than on individual subjects. For example, a partial deviance can be used to diagnose the fitted characteristics of an individual record rather than those of the set of records for a given subject.

scores calculates equation-level score variables. The number of score variables created depends upon the chosen distribution.

The first new variable will always contain  $\partial \ln L/\partial(\mathbf{x}_i\beta)$ .

The subsequent new variables will contain the partial derivative of the log likelihood with respect to the ancillary parameters.

# margins

## **Description for margins**

margins estimates margins of response for median and mean survival times, hazard ratios, and linear predictions.

#### Menu for margins

Statistics > Postestimation

### Syntax for margins

```
margins [marginlist] [, options]
  margins [marginlist], predict(statistic ...) [predict(statistic ...) ...] [options]
statistic
                    Description
                    median survival time: the default
median time
                    median ln(survival time)
median Intime
mean time
                    mean survival time
mean Intime
                    mean ln(survival time)
                    hazard ratio, also known as the relative hazard
hr
                    linear prediction \mathbf{x}_i \boldsymbol{\beta}
хb
hazard
                    not allowed with margins
                    not allowed with margins
stdp
                    not allowed with margins
surv
                    not allowed with margins
csurv
csnell
                    not allowed with margins
mgale
                    not allowed with margins
                    not allowed with margins
deviance
```

Statistics not allowed with margins are functions of stochastic quantities other than e(b).

For the full syntax, see [R] margins.

# Remarks and examples

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predict after streg is used to generate a variable containing predicted values or residuals.

For a more detailed discussion on residuals, read *Residuals and diagnostic measures* in the [ST] **stcox postestimation** entry. Many of the concepts and ideas presented there also apply to streg models.

Regardless of the metric used, predict can generate predicted median survival times and median log survival-times for all models, and predicted mean times and mean log survival-times where available. Predicted survival, hazard, and residuals are also available for all models. The predicted hazard ratio can be calculated only for models with a proportional-hazards parameterization, that is, the Weibull, exponential, and Gompertz models. However, the estimation need not take place in the log-hazard metric. You can perform, for example, a Weibull regression specifying the time option and then ask that hazard ratios be predicted.

After fitting a frailty model, you can use predict with the alpha1 option to generate predicted values based on S(t) or use the unconditional option to generate predictions based on  $S_{\theta}(t)$ ; see [ST] streg.

### ▶ Example 1

Let's return to example 1 of [ST] **streg** concerning the ability of emergency generators with new-style bearings to withstand overloads. Assume that, as before, we fit a proportional hazards Weibull model:

```
. use https://www.stata-press.com/data/r18/kva (Generator experiment)
```

. stset failtime
 (output omitted)

. streg load bearings, distribution(weibull) nolog

Failure \_d: 1 (meaning all fail)

Analysis time \_t: failtime

Weibull PH regression

No. of subjects = 12 No. of failures = 12

Time at risk

Log likelihood = 5.6934189

Number of obs = 12

LR chi2(2) = 30.27Prob > chi2 = 0.0000

_t	Haz. ratio	Std. err.	z	P> z	[95% conf.	interval]
load bearings _cons	1.599315 .1887995 2.51e-20	.1883807 .1312109 2.66e-19	3.99 -2.40 -4.26	0.000 0.016 0.000	1.269616 .0483546 2.35e-29	2.014631 .7371644 2.68e-11
/ln_p	2.051552	. 2317074	8.85	0.000	1.597414	2.505691
p 1/p	7.779969 .1285352	1.802677 .0297826			4.940241 .0816192	12.25202 .2024193

Note: \_cons estimates baseline hazard.

Now we can predict both the median survival time and the log-median survival time for each observation:

```
. predict time, time (option median time assumed; predicted median time)
```

. predict lntime, lntime

(option median lntime assumed; predicted median log time)

. format time lntime %9.4f

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	failtime	load	bearings	time	lntime
1.	100	15	0	127.5586	4.8486
2.	140	15	1	158.0407	5.0629
3.	97	20	0	94.3292	4.5468
4.	122	20	1	116.8707	4.7611
5.	84	25	0	69.7562	4.2450
6.	100	25	1	86.4255	4.4593
7.	54	30	0	51.5845	3.9432
8.	52	30	1	63.9114	4.1575
9.	40	35	0	38.1466	3.6414
10.	55	35	1	47.2623	3.8557
11.	22	40	0	28.2093	3.3397

. list failtime load bearings time Intime

#### Example 2

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Using the cancer data of example 6 in [ST] **streg**, again with drug remapped into a drug-treatment indicator, we can examine the various residuals that Stata produces. For a more detailed discussion on residuals, read *Residuals and diagnostic measures* in [ST] **stcox postestimation**. Many of the concepts and ideas presented there also apply to streg models. For a more technical presentation of these residuals, see *Methods and formulas*.

34.9504

3.5539

We will begin by evaluating goodness of fit based on the generalized Cox-Snell residuals. If the model fits the data, these residuals should have a standard exponential distribution with  $\lambda=1$ . One way to verify the fit is to calculate an empirical estimate of the cumulative hazard function—based, for example, on the Kaplan-Meier survival estimates or the Aalen-Nelson estimator, taking the Cox-Snell residuals as the time variable and the censoring variable as before—and plot it against the Cox-Snell residuals. If the model fits the data, the plot should be a straight line with a slope of 1.

After fitting the model, we can use the estat gofplot command to create this graph. Here the km option specifies that the cumulative hazard function be based on the minus log of the Kaplan-Meier estimator. By default, the cumulative hazard function is based on the Nelson-Aalen estimator.

We did this separately for each of four distributions. Results are plotted in figure 1:

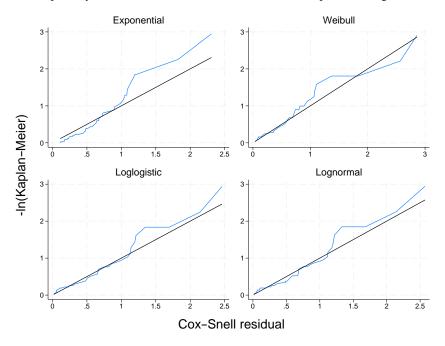


Figure 1. Cox-Snell residuals to evaluate model fit of four regression models

The plots indicate that the Weibull and lognormal models fit the data best and that the exponential model fits poorly. These results are consistent with our previous results (in [ST] **streg**) based on Akaike's information criterion.

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#### Example 3

Let's now look at the martingale-like and deviance residuals. We use the term "martingale-like" because, although these residuals do not arise naturally from martingale theory for parametric survival models as they do for the Cox proportional hazards model, they do share similar form. We can generate these residuals by using predict's mgale option. Martingale residuals take values between  $-\infty$  and 1 and therefore are difficult to interpret. The deviance residuals are a rescaling of the martingale-like residuals so that they are symmetric about zero and thus more like residuals obtained from linear regression. Plots of either deviance residuals against the linear predictor (that is, the log relative hazard in PH models) or of deviance residuals against individual predictors can be useful in identifying aberrant observations and in assessing model fit. Continuing with our modified cancer data, we plot the deviance residual obtained after fitting a lognormal model:

- . quietly streg age drug, distribution(lnormal)
- . predict dev, deviance
- . scatter dev studytime, yline(0) m(o)

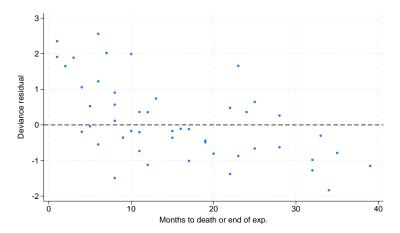


Figure 2. Deviance residuals to evaluate model fit of lognormal model

Figure 2 shows the deviance residuals to be relatively well behaved, with a few minor early exceptions.

## Methods and formulas

predict newvar, options may be used after streg to predict various quantities, according to the following options:

median time:

$$newvar_j = \{t : \hat{S}_j(t) = 1/2\}$$

where  $\widehat{S}_{j}(t)$  is  $S_{j}(t)$  with the parameter estimates "plugged in".

median Intime:

$$\mathit{newvar}_j = \left\{y: \widehat{S}_j(e^y) = 1/2\right\}$$

mean time:

$$newvar_j = \int_0^\infty \widehat{S}_j(t)dt$$

mean Intime:

$$newvar_j = \int_{-\infty}^{\infty} y e^y \widehat{f_j}(e^y) dy$$

where  $\widehat{f_j}(t)$  is  $f_j(t)$  with the parameter estimates plugged in.

hazard:

$$\textit{newvar}_j = \widehat{f}_j(t_j)/\widehat{S}_j(t_j)$$

hr (PH models only):

$$newvar_j = \exp(\mathbf{x}_j^* \widehat{\boldsymbol{\beta}^*})$$

where  $\widehat{\beta}^*$  does not contain the constant and  $\mathbf{x}_j^*$  does not contain the coefficient of 1 corresponding to the constant.

xb:

$$newvar_j = \mathbf{x}_j \widehat{\boldsymbol{\beta}}$$

stdp:

$$newvar_j = \widehat{se}(\mathbf{x}_j\widehat{\boldsymbol{\beta}})$$

surv and csurv:

$$\textit{newvar}_j = \widehat{S}_j(t_j)/\widehat{S}_j(t_{0j})$$

The above represents the probability of survival past time  $t_j$  given survival up until  $t_{0j}$  and represents what you obtain when you specify surv. If csurv is specified, these probabilities are multiplied (in time order) over a subject's multiple observations. What is obtained is then equal to the probability of survival past time  $t_j$ , given survival through the earliest observed  $t_{0j}$ , and given the subject's (possibly time-varying) covariate history. In single-record-per-subject data, surv and csurv are identical.

csnell:

$$newvar_j = -\log \widehat{S}_j(t_j)$$

The Cox-Snell (1968) residual,  $CS_j$ , for observation j at time  $t_j$  is defined as  $\widehat{H}_j(t_j) = -\log \widehat{S}_j(t_j)$ , which is the estimated cumulative hazard function obtained from the fitted model (Collett 2003, 111-112). Cox and Snell argued that if the correct model has been fit to the data, these residuals are n observations from an exponential distribution with unit mean. Thus a plot of the cumulative hazard rate of the residuals against the residuals themselves should result in a straight line of slope 1. Cox-Snell residuals can never be negative and therefore are not symmetric about zero. The options csnell and partial store in each observation that observation's contribution to the subject's Cox-Snell residual, which we refer to as a partial Cox-Snell residual. If only csnell is specified, partial residuals are summed within each subject to obtain one overall Cox-Snell residual for that subject. If there is only 1 observation per subject, partial has no effect.

mgale:

$$newvar_i = d_i - CS_i$$

Martingale residuals follow naturally from martingale theory for Cox proportional hazards, but their development does not carry over for parametric survival models. However, martingale-like residuals similar to those obtained for Cox can be derived from the Cox–Snell residuals:  $M_j = d_j - \mathrm{CS}_j$ , where  $\mathrm{CS}_j$  are the Cox–Snell residuals, as previously described.

Because martingale-like residuals are calculated from the Cox-Snell residuals, they also could be partial or not. Partial martingale residuals are generated with the mgale and partial options, and overall martingale residuals are generated with the mgale option.

Martingale residuals can be interpreted as the difference over time between the number of deaths in the data and the expected number from the fitted model. These residuals take values between  $-\infty$  and 1 and have an expected value of zero, although, like the Cox-Snell residuals, they are not symmetric about zero, making them difficult to interpret.

deviance:

$$newvar_j = sign(M_j) \left[ -2 \left\{ M_j + d_j \log(d_j - M_j) \right\} \right]^{1/2}$$

Deviance residuals are a scaling of the martingale-like residuals in an attempt to make them symmetric about zero. When the model fits the data, these residuals are symmetric about zero and thus can be more readily used to examine the data for outliers. If you also specify the partial option, you obtain partial deviance residuals, one for each observation.

predict also allows two options for use after fitting frailty models: alpha1 and unconditional. If unconditional is specified, the above predictions are modified to be based on  $S_{\theta}(t)$  and  $f_{\theta}(t)$ , rather than S(t) and f(t); see [ST] streg. If alpha1 is specified, the predictions are as described above.

#### References

Boswell, T. M., and R. G. Gutierrez. 2011. Stata tip 94: Manipulation of prediction parameters for parametric survival regression models. Stata Journal 11: 143–144.

Collett, D. 2003. Modelling Binary Data. 2nd ed. London: Chapman and Hall/CRC.

Cox, D. R., and E. J. Snell. 1968. A general definition of residuals (with discussion). *Journal of the Royal Statistical Society, Series B* 30: 248–275. https://doi.org/10.1111/j.2517-6161.1968.tb00724.x.

### Also see

[ST] **streg** — Parametric survival models

[ST] estat gofplot — Goodness-of-fit plots after streg, stcox, stintreg, or stintcox

[ST] stcurve — Plot the survivor or related function after streg, stcox, and more

[U] 20 Estimation and postestimation commands

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