Title

boxcox — Box–Cox regression models

Description Quick st Options Remarks References Also see

Quick start Remarks and examples Also see Menu Stored results Syntax Methods and formulas

Description

boxcox finds the maximum likelihood estimates of the parameters of the Box-Cox transform, the coefficients on the independent variables, and the standard deviation of the normally distributed errors. Any *depvar* or *indepvars* to be transformed must be strictly positive. Options can be used to control which variables remain untransformed.

Quick start

Box-Cox transform of y in a model of y as a function of x1 boxcox y x1

Same as above

boxcox y x1, model(lhsonly)

Likelihood-ratio test for each scale-variant parameter boxcox y x1, lrtest

Different transform for each side and adding covariates x2 and x3 boxcox y x1 x2 x3, model(theta)

Same transform for both sides, and include x3 as an untransformed variable transformation boxcox y x1 x2, model(lambda) notrans(x3)

Menu

Statistics > Linear models and related > Box–Cox regression

Syntax

boxcox depvar [indepvars] [if] [in] [weight] [, options]

options	Description		
Model			
<u>nocons</u> tant	suppress constant term		
model(<u>lhs</u> only)	left-hand-side Box-Cox model; the default		
model(<u>rhs</u> only)	right-hand-side Box-Cox model		
model(<u>lam</u> bda)	both sides Box-Cox model with same parameter		
model(theta)	both sides Box-Cox model with different parameters		
<u>notr</u> ans(<i>varlist</i>)	do not transform specified independent variables		
Reporting			
<u>l</u> evel(#)	set confidence level; default is level(95)		
lrtest	perform likelihood-ratio test		
Maximization			
[no]log	suppress all iteration logs		
nologlr	suppress restricted-model lrtest iteration log		
maximize_options	control the maximization process; seldom used		

depvar and indepvars may contain time-series operators; see [U] 11.4.4 Time-series varlists. bootstrap, by, collect, jackknife, rolling, statsby, and xi are allowed; see [U] 11.1.10 Prefix commands. Weights are not allowed with the bootstrap prefix; see [R] bootstrap. fweights and iweights are allowed; see [U] 11.1.6 weight.

See [U] 20 Estimation and postestimation commands for more capabilities of estimation commands.

Options

_ Model

noconstant; see [R] Estimation options.

model(lhsonly|rhsonly|lambda|theta) specifies which of the four models to fit.

model(lhsonly) applies the Box-Cox transform to *depvar* only. model(lhsonly) is the default.

model(rhsonly) applies the transform to the *indepvars* only.

model(lambda) applies the transform to both *depvar* and *indepvars*, and they are transformed by the same parameter.

model(theta) applies the transform to both *depvar* and *indepvars*, but this time, each side is transformed by a separate parameter.

notrans(varlist) specifies that the variables in varlist not be transformed when included in the model. You can specify notrans(varlist) with model(lhsonly), but the results will be the same as specifying the variables in varlist in indepvars.

Reporting

level(#); see [R] Estimation options.

lrtest specifies that a likelihood-ratio test of significance be performed and reported for each independent variable.

Maximization

log and nolog specify whether to display the iteration log. The iteration log is displayed by default unless you used set iterlog off to suppress it; see set iterlog in [R] *set iter*. These options control the iteration log produced by the full model and, if option lrtest is specified, by the fitted restricted models.

nologlr suppresses the iteration log when fitting the restricted models required by the lrtest option.
maximize_options: iterate(#) and from(init_specs); see [R] Maximize.

Model	Initial value specification
lhsonly	from($ heta_0$, copy)
rhsonly	from(λ_0 , copy)
lambda	from(λ_0 , copy)
theta	from(λ_0 $ heta_0$, copy)

Remarks and examples

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Remarks are presented under the following headings:

Introduction Theta model Lambda model Left-hand-side-only model Right-hand-side-only model

Introduction

The Box-Cox transform

$$y^{(\lambda)} = \frac{y^{\lambda} - 1}{\lambda}$$

has been widely used in applied data analysis. Box and Cox (1964) developed the transformation and argued that the transformation could make the residuals more closely normal and less heteroskedastic. Cook and Weisberg (1982) discuss the transform in this light. Because the transform embeds several popular functional forms, it has received some attention as a method for testing functional forms, in particular,

$$y^{(\lambda)} = \begin{cases} y - 1 & \text{if } \lambda = 1\\ \ln(y) & \text{if } \lambda = 0\\ 1 - 1/y & \text{if } \lambda = -1 \end{cases}$$

Davidson and MacKinnon (1993) discuss this use of the transform. Atkinson (1985) also gives a good general treatment.

Theta model

boxcox obtains the maximum likelihood estimates of the parameters for four different models. The most general of the models, the theta model, is

$$y_{j}^{(\theta)} = \beta_{0} + \beta_{1}x_{1j}^{(\lambda)} + \beta_{2}x_{2j}^{(\lambda)} + \dots + \beta_{k}x_{kj}^{(\lambda)} + \gamma_{1}z_{1j} + \gamma_{2}z_{2j} + \dots + \gamma_{l}z_{lj} + \epsilon_{j}$$

where $\epsilon \sim N(0, \sigma^2)$. Here the dependent variable, y, is subject to a Box-Cox transform with parameter θ . Each of the *indepvars*, x_1, x_2, \ldots, x_k , is transformed by a Box-Cox transform with parameter λ . The z_1, z_2, \ldots, z_l specified in the notrans() option are independent variables that are not transformed.

Box and Cox (1964) argued that this transformation would leave behind residuals that more closely follow a normal distribution than those produced by a simple linear regression model. Bear in mind that the normality of ϵ is assumed and that boxcox obtains maximum likelihood estimates of the k+l+4 parameters under this assumption. boxcox does not choose λ and θ so that the residuals are approximately normally distributed. If you are interested in this type of transformation to normality, see the official Stata commands lnskew0 and bcskew0 in [R] lnskew0. However, those commands work on a more restrictive model in which none of the independent variables is transformed.

Example 1

Below, we fit a theta model to a nonrepresentative extract of the Second National Health and Nutrition Examination Survey (NHANES II) dataset discussed in McDowell et al. (1981).

We model individual-level diastolic blood pressure (bpdiast) as a function of the transformed variables body mass index (bmi) and cholesterol level (tcresult) and of the untransformed variables age (age) and sex (sex).

10,351

0.000

```
. use https://www.stata-press.com/data/r18/nhanes2
. boxcox bpdiast bmi tcresult, notrans(age sex) model(theta) lrtest
Fitting comparison model
Iteration 0: Log likelihood = -41178.61
Iteration 1: Log likelihood = -41032.51
Iteration 2: Log likelihood = -41032.488
Iteration 3: Log likelihood = -41032.488
Fitting full model
Iteration 0: Log likelihood = -39928.606
Iteration 1: Log likelihood = -39775.026
Iteration 2: Log likelihood = -39774.987
Iteration 3: Log likelihood = -39774.987
Fitting comparison models for LR tests
Iteration 0: Log likelihood = -39947.144
Iteration 1: Log likelihood = -39934.55
Iteration 2: Log likelihood = -39934.516
Iteration 3: Log likelihood = -39934.516
Iteration 0: Log likelihood = -39906.96
Iteration 1: Log likelihood = -39896.63
Iteration 2: Log likelihood = -39896.629
Iteration 0: Log likelihood = -40464.599
Iteration 1: Log likelihood = -40459.765
Iteration 2: Log likelihood = -40459.604
Iteration 3: Log likelihood = -40459.604
Iteration 0: Log likelihood = -39829.859
Iteration 1: Log likelihood = -39815.576
Iteration 2: Log likelihood = -39815.575
                                                 Number of obs
                                                                 =
```

Log likelihood	d = -39774.987			LR ch Prob	ni2(5) > chi2	= =	2515.00 0.000
bpdiast	Coefficient	Std. err.	z	P> z	[95%	conf.	interval]
/lambda /theta	.6383286 .1988197	.1577601 .0454088	4.05 4.38	0.000	.3291 .1098	245 201	.9475327 .2878193

307.24

Estimates of scale-variant parameters

theta=lambda = 1

	Coefficient	chi2(df)	P>chi2(df)	df of chi2
Notrans				
age	.003811	319.060	0.000	1
sex	1054887	243.284	0.000	1
_cons	5.835555			
Trans				
bmi	.0872041	1369.235	0.000	1
tcresult	.004734	81.177	0.000	1
/sigma	.3348267			
Test	Rest	ricted		
HO:	log li	kelihood	chi2	Prob > chi2
theta=lambda	= -1 -401	62.898	775.82	0.000
theta=lambda	= 0 -397	90.945	31.92	0.000

-39928.606

The output is composed of the iteration logs and three distinct tables. The first table contains a standard header for a maximum likelihood estimator and a standard output table for the Box–Cox transform parameters. The second table contains the estimates of the scale-variant parameters. The third table contains the output from likelihood-ratio tests on three standard functional form specifications.

The right-hand-side and the left-hand-side transformations each add to the regression fit at the 1% significance level and are both positive but less than 1. All the variables have significant impacts on diastolic blood pressure, bpdiast. As expected, the transformed variables—the body mass index, bmi, and cholesterol level, tcresult—contribute to higher blood pressure. The last output table shows that the linear, multiplicative inverse, and log specifications are strongly rejected.

Technical note

Spitzer (1984) showed that the Wald tests of the joint significance of the coefficients of the right-hand-side variables, either transformed or untransformed, are not invariant to changes in the scale of the transformed dependent variable. Davidson and MacKinnon (1993) also discuss this point. This problem demonstrates that Wald statistics can be manipulated in nonlinear models. Lafontaine and White (1986) analyze this problem numerically, and Phillips and Park (1988) analyze it by using Edgeworth expansions. See Drukker (2000) for a more detailed discussion of this issue. Because the parameter estimates and their Wald tests are not scale invariant, no Wald tests or confidence intervals are reported for these parameters. However, when the lrtest option is specified, likelihood-ratio tests are performed and reported. Schlesselman (1971) showed that, if a constant is included in the model, the parameter estimates of the Box–Cox transforms are scale invariant. For this reason, we strongly recommend that you not use the noconstant option.

The lrtest option does not perform a likelihood-ratio test on the constant, so no value for this statistic is reported. Unless the data are properly scaled, the restricted model does not often converge. For this reason, no likelihood-ratio test on the constant is performed by the lrtest option. However, if you have a special interest in performing this test, you can do so by fitting the constrained model separately. If problems with convergence are encountered, rescaling the data by their means may help.

Lambda model

A less general model than the one above is called the lambda model. It specifies that the same parameter be used in both the left-hand-side and right-hand-side transformations. Specifically,

$$y_j^{(\lambda)} = \beta_0 + \beta_1 x_{1j}^{(\lambda)} + \beta_2 x_{2j}^{(\lambda)} + \dots + \beta_k x_{kj}^{(\lambda)} + \gamma_1 z_{1j} + \gamma_2 z_{2j} + \dots + \gamma_l z_{lj} + \epsilon_j$$

where $\epsilon \sim N(0, \sigma^2)$. Here the *depvar* variable, y, and each of the *indepvars*, x_1, x_2, \ldots, x_k , is transformed by a Box–Cox transform with the common parameter λ . Again, the z_1, z_2, \ldots, z_l are independent variables that are not transformed.

Left-hand-side-only model

Even more restrictive than a common transformation parameter is transforming the dependent variable only. Because the dependent variable is on the left-hand side of the equation, this model is known as the lhsonly model. Here you are estimating the parameters of the model

$$y_j^{(\theta)} = \beta_0 + \beta_1 x_{1j} + \beta_2 x_{2j} + \dots + \beta_k x_{kj} + \epsilon_j$$

where $\epsilon \sim N(0, \sigma^2)$. Here only the *depvar*, y, is transformed by a Box–Cox transform with the parameter θ .

Example 2

In this example, we model the transform of diastolic blood pressure as a linear combination of the untransformed body mass index, cholesterol level, age, and sex.

```
. boxcox bpdiast bmi tcresult age sex, model(lhsonly) lrtest nolog nologlr
Fitting comparison model
Fitting full model
Fitting comparison models for LR tests
                                                     Number of obs
                                                                            10,351
                                                                      =
                                                     LR chi2(4)
                                                                      =
                                                                           2509.56
Log likelihood = -39777.709
                                                     Prob > chi2
                                                                      =
                                                                             0.000
     bpdiast
                                                   P>|z|
                                                              [95% conf. interval]
                Coefficient
                             Std. err.
                                             z
                  .2073268
                              .0452895
                                           4.58
                                                   0.000
                                                              .1185611
                                                                          .2960926
      /theta
Estimates of scale-variant parameters
                Coefficient chi2(df)
                                       P>chi2(df)
                                                      df of chi2
Notrans
                            1375.841
                                         0.000
                                                         1
         bmi
                  .0272628
    tcresult
                  .0006929
                              82.380
                                         0.000
                                                         1
                  .0040141
                             334.117
                                         0.000
                                                         1
         age
                 -.1122274
                             263.219
                                         0.000
                                                         1
         sex
       _cons
                  6.302855
      /sigma
                  .3476615
   Test
                                 LR statistic
                 Restricted
                                                Prob > chi2
    H0:
               log likelihood
                                     chi2
                 -40146.678
                                   737.94
                                                     0.000
theta = -1
theta =
         0
                 -39788.241
                                    21.06
                                                     0.000
theta =
                 -39928.606
                                   301.79
                                                     0.000
         1
```

The maximum likelihood estimate of the transformation parameter for this model is positive and significant. Once again, all the scale-variant parameters are significant, and we find a positive impact of body mass index (bmi) and cholesterol levels (tcresult) on the transformed diastolic blood pressure (bpdiast). This model rejects the linear, multiplicative inverse, and log specifications.

4

Right-hand-side-only model

The fourth model leaves the *depvar* alone and transforms a subset of the *indepvars* using the parameter λ . This is the **rhsonly** model. In this model, the *depvar*, y, is given by

$$y_{j} = \beta_{0} + \beta_{1} x_{1j}^{(\lambda)} + \beta_{2} x_{2j}^{(\lambda)} + \dots + \beta_{k} x_{kj}^{(\lambda)} + \gamma_{1} z_{1j} + \gamma_{2} z_{2j} + \dots + \gamma_{l} z_{lj} + \epsilon_{j}$$

where $\epsilon \sim N(0, \sigma^2)$. Here each of the *indepvars*, x_1, x_2, \ldots, x_k , is transformed by a Box-Cox transform with the parameter λ . Again, the z_1, z_2, \ldots, z_l are independent variables that are not transformed.

Example 3

Now, we consider a rhsonly model in which the regressors sex and age are not transformed.

```
. boxcox bpdiast bmi tcresult, notrans(sex age) model(rhsonly) lrtest nolog
> nologlr
```

Fitting full model

Fitting comparison models for LR tests

				Number LR chi	of obs 2(5)	=	10,351 2500.79
Log likeliho	od = -39928.212	2		Prob >	chi2	=	0.000
bpdiast	Coefficient	Std. err.	Z	P> z	[95%	conf.	interval]
/lambda	.8658841	.1522387	5.69	0.000	.5675	018	1.164266

Estimates of scale-variant parameters

	Coefficient	chi2(df)	P>chi2(d	f) df	of	chi2
Notrans						
sex	-3.544042	235.020	0.000		1	
age	.128809	311.754	0.000		1	
_cons	50.01498					
Trans						
bmi	1.418215	1396.709	0.000		1	
tcresult	.0462964	78.500	0.000		1	
/sigma	11.4557					
						_
Test	Restricted	LR st	atistic			
HO:	log likelihoo	od o	:hi2	Prob >	chi	2
lambda = -1	-39989.331	122	2.24	0.0	000	-
lambda = 0	-39942.945	29	9.47	0.0	000	
lambda = 1	-39928.606	C	.79	0.3	875	

The maximum likelihood estimate of the transformation parameter in this model is positive and significant at the 1% level. The transformed bmi coefficient behaves as expected, and the remaining scale-variant parameters are significant at the 1% level. This model rejects the multiplicative inverse and log specifications strongly. However, we cannot reject the hypothesis that the model is linear.

Stored results

boxcox stores the following in e():

Scalars	
e(N)	number of observations
e(11)	log likelihood
e(chi2)	LR statistic of full vs. comparison
e(df_m)	full model degrees of freedom
e(110)	log likelihood of the restricted model
e(df_r)	restricted model degrees of freedom
e(ll_t1)	log likelihood of model $\lambda = \theta = 1$
e(chi2_t1)	LR of $\lambda = \theta = 1$ vs. full model
e(p_t1)	<i>p</i> -value of $\lambda = \theta = 1$ vs. full model
e(ll_tm1)	log likelihood of model $\lambda = \theta = -1$
e(chi2_tm1)	LR of $\lambda = \theta = -1$ vs. full model
e(p_tm1)	<i>p</i> -value of $\lambda = \theta = -1$ vs. full model
e(11_t0)	log likelihood of model $\lambda = \theta = 0$
e(chi2_t0)	LR of $\lambda = \theta = 0$ vs. full model
e(p_t0)	<i>p</i> -value of $\lambda = \theta = 0$ vs. full model
e(rank)	rank of e(V)
e(ic)	number of iterations
e(rc)	return code
Macros	
e(cmd)	boxcox
e(cmdline)	command as typed
e(depvar)	name of dependent variable
e(model)	lhsonly, rhsonly, lambda, or theta
e(wtype)	weight type
e(wexp)	weight expression
e(ntrans)	yes if untransformed <i>indepvars</i>
e(chi2type)	LR; type of model χ^2 test
e(lrtest)	lrtest, if requested
e(properties)	b V
e(predict)	program used to implement predict
e(marginsnotok)	predictions disallowed by margins
Matrices	
e(b)	coefficient vector
e(V)	variance-covariance matrix of the estimators (see note below)
e(pm)	<i>p</i> -values for LR tests on <i>indepvars</i>
e(df)	degrees of freedom of LR tests on indepvars
e(chi2m)	LR statistics for tests on indepvars
Functions	
e(sample)	marks estimation sample
1 I I	

e(V) contains all zeros, except for the elements that correspond to the parameters of the Box–Cox transform.

Methods and formulas

In the internal computations,

$$y^{(\lambda)} = \begin{cases} \frac{y^{\lambda} - 1}{\lambda} & \text{if } |\lambda| > 10^{-10} \\\\ \ln(y) & \text{otherwise} \end{cases}$$

The unconcentrated log likelihood for the theta model is

$$\ln L = \left(\frac{-N}{2}\right) \left\{ \ln(2\pi) + \ln(\sigma^2) \right\} + (\theta - 1) \sum_{i=1}^N \ln(y_i) - \left(\frac{1}{2\sigma^2}\right) \text{SSR}$$

where

$$SSR = \sum_{i=1}^{N} (y_i^{(\theta)} - \beta_0 + \beta_1 x_{i1}^{(\lambda)} + \beta_2 x_{i2}^{(\lambda)} + \dots + \beta_k x_{ik}^{(\lambda)} + \gamma_1 z_{i1} + \gamma_2 z_{i2} + \dots + \gamma_l z_{il})^2$$

Writing the SSR in matrix form,

....

$$SSR = (\mathbf{y}^{(\theta)} - \mathbf{X}^{(\lambda)}\mathbf{b}' - \mathbf{Zg}')'(\mathbf{y}^{(\theta)} - \mathbf{X}^{(\lambda)}\mathbf{b}' - \mathbf{Zg}')$$

where $\mathbf{y}^{(\theta)}$ is an $N \times 1$ vector of elementwise transformed data, $\mathbf{X}^{(\lambda)}$ is an $N \times k$ matrix of elementwise transformed data, \mathbf{Z} is an $N \times l$ matrix of untransformed data, \mathbf{b} is a $1 \times k$ vector of coefficients, and \mathbf{g} is a $1 \times l$ vector of coefficients. Letting

$$\mathbf{W}_{\lambda} = \left(\mathbf{X}^{(\lambda)} \, \, \mathbf{Z}
ight)$$

be the horizontal concatenation of $\mathbf{X}^{(\lambda)}$ and \mathbf{Z} and

$$\mathbf{d}' = \begin{pmatrix} \mathbf{b}' \\ \mathbf{g}' \end{pmatrix}$$

be the vertical concatenation of the coefficients yields

$$SSR = (\mathbf{y}^{(\theta)} - \mathbf{W}_{\lambda} \mathbf{d}')' (\mathbf{y}^{(\theta)} - \mathbf{W}_{\lambda} \mathbf{d}')$$

For given values of λ and θ , the solutions for d' and σ^2 are

$$\widehat{\mathbf{d}}' = (W_{\lambda}' W_{\lambda})^{-1} W_{\lambda}' y^{(\theta)}$$

and

$$\widehat{\sigma}^{2} = \frac{1}{N} \left(\mathbf{y}^{(\theta)} - W_{\lambda} \widehat{d}' \right)' \left(y^{(\theta)} - W_{\lambda} \widehat{d}' \right)$$

Substituting these solutions into the log-likelihood function yields the concentrated log-likelihood function

$$\ln L_c = \left(-\frac{N}{2}\right) \left\{ \ln(2\pi) + 1 + \ln(\hat{\sigma}^2) \right\} + (\theta - 1) \sum_{i=1}^N \ln(y_i)$$

Similar calculations yield the concentrated log-likelihood function for the lambda model,

$$\ln L_{c} = \left(-\frac{N}{2}\right) \left\{ \ln(2\pi) + 1 + \ln(\widehat{\sigma}^{2}) \right\} + (\lambda - 1) \sum_{i=1}^{N} \ln(y_{i})$$

the lhsonly model,

$$\ln L_{c} = \left(-\frac{N}{2}\right) \left\{ \ln(2\pi) + 1 + \ln(\hat{\sigma}^{2}) \right\} + (\theta - 1) \sum_{i=1}^{N} \ln(y_{i})$$

and the rhsonly model,

$$\ln L_c = \left(-\frac{N}{2}\right) \left\{ \ln(2\pi) + 1 + \ln(\widehat{\sigma}^2) \right\}$$

where $\hat{\sigma}^2$ is specific to each model and is defined analogously to that in the theta model.

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Also see

- [R] **boxcox postestimation** Postestimation tools for boxcox
- [R] Inskew0 Find zero-skewness log or Box-Cox transform

[R] regress — Linear regression

[U] 20 Estimation and postestimation commands

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