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mi test — Test hypotheses after mi estimate

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Also see

Description

mi test performs joint tests of coefficients.

mi testtransform performs joint tests of transformed coefficients as specified with mi estimate or mi estimate using (see [MI] mi estimate or [MI] mi estimate using).

Menu

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Syntax

```
Test that coefficients are zero
```

```
mi test coeflist
```

Test that coefficients within a single equation are zero

```
mi test [eqno] [: coeflist]
```

Test that subsets of coefficients are zero (full syntax)

```
mi test (spec) [(spec) ...] [, test\_options]
```

Test that subsets of transformed coefficients are zero

```
mi <u>testtr</u>ansform name [(name) ...] [, transform_options]
```

test_options	Description					
Test						
<u>ufmit</u> est	perform unrestricted FMI model test					
nosmall	do not apply small-sample correction to degrees of freedom					
<u>cons</u> tant	include the constant in coefficients to be tested					
transform_options	Description					
Test						
<u>ufmit</u> est	perform unrestricted FMI model test					
nosmall	do not apply small-sample correction to degrees of freedom					
$\underline{\mathtt{noleg}}\mathtt{end}$	suppress transformation legend					

coeflist may contain factor variables and time-series operators; see [U] 11.4.3 Factor variables and [U] 11.4.4 Time-series variists.

collect is allowed with mi test; see [U] 11.1.10 Prefix commands.

coeflist is

```
coef [coef ...]
[eqno]coef [ [eqno]coef... ]
[eqno]_b[coef] [ [eqno]_b[coef]... ]
```

eqno is

##

spec is

coeflist
[eqno] [: coeflist]

eqname

coef identifies a coefficient in the model; see the description in [R] test for details. eqname is an equation name.

name is an expression name as specified with mi estimate or mi estimate using (see [MI] mi estimate or [MI] mi estimate using).

Options

Test

ufmitest specifies that the unrestricted fraction missing information (FMI) model test be used. The default test performed assumes equal fractions of information missing due to nonresponse for all coefficients. This is equivalent to the assumption that the between-imputation and within-imputation variances are proportional. The unrestricted test may be preferable when this assumption is suspect provided that the number of imputations is large relative to the number of estimated coefficients.

nosmall specifies that no small-sample adjustment be made to the degrees of freedom. By default, individual tests of coefficients (and transformed coefficients) use the small-sample adjustment of Barnard and Rubin (1999), and the overall model test uses the small-sample adjustment of Reiter (2007).

constant specifies that _cons be included in the list of coefficients to be tested when using the [eqno] form of spec with mi test. The default is to not include _cons.

nolegend, specified with mi testtransform, suppresses the transformation legend.

Remarks and examples

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Remarks are presented under the following headings:

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Example 1: Testing subsets of coefficients equal to zero

Example 2: Testing linear hypotheses Example 3: Testing nonlinear hypotheses

Introduction

The major issue arising when performing tests after MI estimation is the validity of the variance–covariance estimator (VCE) of the MI estimates. MI variance consists of two sources of variation: within-imputation variation and between-imputation variation. With a small number of imputations, the estimate of the between-imputation variance—covariance matrix is imprecise. In fact, when the number of imputations is less than or equal to the number of estimated parameters, the between-imputation matrix does not even have a full rank. As such, the estimated VCE may not be a valid variance—covariance matrix and thus not suitable for joint inference.

One solution to this problem was proposed by Rubin (1987) and Li et al. (1991). The idea is to assume that the between-imputation variance is proportional to the within-imputation variance. This assumption implies equal FMIs for all jointly tested parameters. Li et al. (1991) found that the procedure performs well in terms of power and maintaining the significance level even with moderately variable FMIs. mi test and mi testtransform, by default, perform tests using this procedure.

When the number of imputations is large enough relative to the number of tested parameters so that the corresponding VCE is trustworthy, you can request the unrestricted FMI test by specifying the ufmitest option. The unrestricted FMI test is the conventional test described by Rubin (1987, 77).

For testing nonlinear hypotheses, direct application of the conventional delta method to the estimated coefficients may not be feasible when the number of imputations is small enough that the VCE of the MI estimates cannot be used for inference. To test these hypotheses, one can first obtain MI estimates of the transformed coefficients by applying Rubin's combination rules to the transformed completed-data estimates and then apply the above MI-specific hypotheses tests to the combined transformed estimates. The first step can be done by specifying expressions with mi estimate (or

mi estimate using). The second step is performed with mi testtransform. mi testtransform uses the same method to test transformed coefficients as mi test uses to test coefficients.

Overview

Use mi test to perform joint tests that coefficients are equal to zero:

```
. mi estimate: regress y x1 x2 x3 x4 . mi test x2 x3 x4 \,
```

Use mi testtransform, however, to perform tests of more general linear hypotheses, such as $_b[x1]=_b[x2]$, or $_b[x1]=_b[x2]$ and $_b[x1]=_b[x3]$. Testing general linear hypotheses requires estimation of between and within variances corresponding to the specific hypotheses and requires recombining the imputation-specific estimation results. One way you could do that would be to refit the model and include the additional parameters during the estimation step. To test $_b[x1]=_b[x2]$, you could type

```
. mi estimate (diff: _b[x1]-_b[x2]): regress y x1 x2 x3 x4 . mi testtransform diff
```

A better approach, however, is to save each of the imputation-specific results at the time the original model is fit and then later recombine results using mi estimate using. To save the imputation-specific results, specify mi estimate's saving() option when the model is originally fit:

```
. mi estimate, saving(myresults): regress y x1 x2 x3 x4
```

To test $_b[x1] = _b[x2]$, you type

- . mi estimate (diff: _b[x1]-_b[x2]) using myresults
- . mi testtransform diff

The advantage of this approach is that you can test additional hypotheses without refitting the model. For instance, if we now wanted to test $_b[x1]=_b[x2]$ and $_b[x1]=_b[x3]$, we could type

```
. mi estimate (diff1: _b[x1]-_b[x2]) (diff2: _b[x1]=_b[x3]) using myresults . mi testtransform diff1 diff2
```

To test nonlinear hypotheses, such as b[x1]/b[x2] = b[x3]/b[x4], we could then type

- . mi estimate (diff: b[x1]/b[x2]-b[x3]/b[x4]) using myresults
- . mi testtransform diff

Example 1: Testing subsets of coefficients equal to zero

We are going to test that tax, sqft, age, nfeatures, ne, custom, and corner are in the regression analysis of house resale prices we performed in *Example 1: Completed-data logistic analysis* of [MI] **mi estimate**. Following the advice above, when we fit the model, we are going to save the imputation-specific results even though we will not need them in this example; we will need them in the following examples.

```
. use https://www.stata-press.com/data/r18/mhouses1993s30
(Albuquerque home prices Feb15-Apr30, 1993)
```

- . mi estimate, saving(miest): regress price tax sqft age nfeatures ne custom
- > corner

Multiple-imputation		nputation		=	30 117	
J		A·	verage 1	RVI	=	0.0648
		L	argest 1	FMI	=	0.2533
		C	omplete	DF	=	109
DF adjustment: S	mall sample	Di	7: 1	min	=	69.12
				avg	=	94.02
			1	max	=	105.51
Model F test:	Equal FMI	F	(7,	106.5)	=	67.18
Within VCE type:	OLS	P	rob > F		=	0.0000

price	Coefficient	Std. err.	t	P> t	[95% conf.	interval]
tax	.6768015	.1241568	5.45	0.000	.4301777	.9234253
sqft	.2118129	.069177	3.06	0.003	.0745091	.3491168
age	.2471445	1.653669	0.15	0.882	-3.051732	3.546021
nfeatures	9.288033	13.30469	0.70	0.487	-17.12017	35.69623
ne	2.518996	36.99365	0.07	0.946	-70.90416	75.94215
custom	134.2193	43.29755	3.10	0.002	48.35674	220.0818
corner	-68.58686	39.9488	-1.72	0.089	-147.7934	10.61972
_cons	123.9118	71.05816	1.74	0.085	-17.19932	265.0229

In the above mi estimate command, we use the saving() option to create a Stata estimation file called miest.ster, which contains imputation-specific estimation results.

mi estimate reports the joint test of all coefficients equal to zero in the header. We can reproduce this test with mi test by typing

- . mi test tax sqft age nfeatures ne custom corner note: assuming equal fractions of missing information.
 - $(1) \tan = 0$
 - (2) sqft = 0
 - (3) age = 0
 - (4) nfeatures = 0
 - (5) ne = 0
 - (6) custom = 0
 - (7) corner = 0

$$F(7, 106.5) = 67.18$$

 $Prob > F = 0.0000$

We obtain results identical to those from mi estimate.

We can test that a subset of coefficients, say, sqft and tax, are equal to zero by typing

- . mi test sqft tax note: assuming equal fractions of missing information. (1) sqft = 0
- $(2) \tan = 0$ F(2, 105.7) = 114.75Prob > F =0.0000

Example 2: Testing linear hypotheses

Now we want to test the equality of the coefficients for sqft and tax. Following our earlier suggestion, we use mi estimate using to estimate the difference between coefficients (and avoid refitting the models) and then use mi testtransform to test that the difference is zero:

```
. mi estimate (diff: _b[tax]-_b[sqft]) using miest, nocoef
Multiple-imputation estimates
                                                  Imputations
                                                                              30
Linear regression
                                                 Number of obs
                                                                             117
                                                  Average RVI
                                                                    =
                                                                          0.1200
                                                 Largest FMI
                                                                          0.1100
                                                                             109
                                                 Complete DF
DF adjustment:
                 Small sample
                                                 DF:
                                                                           92.10
                                                          min
                                                          avg
                                                                           92.10
Within VCE type:
                           OLS
                                                                           92.10
                                                          max
```

command: regress price tax sqft age nfeatures ne custom corner
diff: _b[tax]-_b[sqft]

price	Coefficient	Std. err.	t	P> t	[95% conf.	interval]
diff	. 4649885	.1863919	2.49	0.014	.0948037	.8351733

. mi testtransform diff

note: assuming equal fractions of missing information.

 $diff: _b[tax]-_b[sqft]$ (1) diff = 0

F(1, 92.1) = 6.22Prob > F = 0.0144

We suppress the display of the coefficient table by specifying the nocoef option with mi estimate using. We obtain the same results from the F test as those of the t test reported in the transformation table.

Similarly, we can test whether three coefficients are jointly equal:

```
. mi estimate (diff1: _b[tax]-_b[sqft]) (diff2: _b[custom]-_b[tax]) using miest,
> nocoef
Multiple-imputation estimates
                                                Imputations
                                                                             30
Linear regression
                                                Number of obs
                                                                  =
                                                                            117
                                                Average RVI
                                                                  =
                                                                        0.0748
                                                Largest FMI
                                                                  =
                                                                         0.1100
                                                Complete DF
                                                                            109
DF adjustment:
                 Small sample
                                                DF:
                                                                  =
                                                                         92.10
                                                        min
                                                                  =
                                                                         97.95
                                                        avg
Within VCE type:
                          OLS
                                                                        103.80
                                                        max
      command: regress price tax sqft age nfeatures ne custom corner
```

diff1: _b[tax]-_b[sqft] diff2: _b[custom]-_b[tax]

price	Coefficient	Std. err.	t	P> t	[95% conf.	interval]
diff1	.4649885	.1863919		0.014	.0948037	.8351733
diff2	133.5425	43.30262		0.003	47.66984	219.4151

. mi testtr diff1 diff2

note: assuming equal fractions of missing information.

diff1: _b[tax]-_b[sqft] diff2: _b[custom]-_b[tax]

- (1) diff1 = 0
- (2) diff2 = 0

F(2, 105.6) =7.34 Prob > F =0.0010

We estimate two differences, _b[tax]-_b[sqft] and _b[custom]-_b[tax], using mi estimate using and test whether they are jointly equal to zero by using mi testtransform.

We can perform tests of other hypotheses similarly by reformulating the hypotheses of interest such that we are testing equality to zero.

Example 3: Testing nonlinear hypotheses

In the examples above, we tested linear hypotheses. Testing nonlinear hypotheses is no different. We simply replace the specification of linear expressions in mi estimate using with the nonlinear expressions corresponding to the tests of interest.

For example, let's test that the ratio of the coefficients for tax and sqft is one, an equivalent but less efficient way of testing whether the two coefficients are the same. Similarly to the earlier example, we specify the corresponding nonlinear expression with mi estimate using and then use mi testtransform to test that the ratio is one:

```
8
```

```
. mi estimate (rdiff: _b[tax]/_b[sqft] - 1) using miest, nocoef
Multiple-imputation estimates
                                                  Imputations
                                                                               30
Linear regression
                                                  Number of obs
                                                                              117
                                                                           0.0951
                                                  Average RVI
                                                  Largest FMI
                                                                           0.0892
                                                  Complete DF
                                                                              109
DF adjustment:
                 Small sample
                                                  DF:
                                                                           95.33
                                                          min
                                                                           95.33
                                                          avg
                                                                           95.33
Within VCE type:
                           OLS
                                                          max
      command: regress price tax sqft age nfeatures ne custom corner
        rdiff: _b[tax]/_b[sqft] - 1
```

price	Coefficient	Std. err.	t	P> t	[95% conf.	interval]
rdiff	2.2359	1.624546	1.38	0.172	9890876	5.460888

. mi testtr rdiff

note: assuming equal fractions of missing information.

```
rdiff: _b[tax]/_b[sqft] - 1
(1) rdiff = 0
F( 1, 95.3) = 1.89
Prob > F = 0.1719
```

We do not need to use mi testtransform (or mi test) to test one transformation (or coefficient) because the corresponding test is provided in the output from mi estimate using.

Stored results

mi test and mi testtransform store the following in r():

```
Scalars
```

r(df) test constraints degrees of freedom
r(df_r) residual degrees of freedom
r(p) two-sided p-value
r(F) F statistic
r(drop) 1 if constraints were dropped, 0 otherwise

r(dropped_i) index of ith constraint dropped

Methods and formulas

mi test and mi testtransform use the methodology described in *Multivariate case* under *Methods and formulas* of [MI] mi estimate, where we replace \mathbf{q} with $\mathbf{R}\mathbf{q} - \mathbf{r}$ and $\mathbf{q}_0 = \mathbf{0}$ for the test H_0 : $\mathbf{R}\mathbf{q} = \mathbf{r}$.

References

Barnard, J., and D. B. Rubin. 1999. Small-sample degrees of freedom with multiple imputation. *Biometrika* 86: 948–955. https://doi.org/10.1093/biomet/86.4.948.

Li, K.-H., X.-L. Meng, T. E. Raghunathan, and D. B. Rubin. 1991. Significance levels from repeated *p*-values with multiply-imputed data. *Statistica Sinica* 1: 65–92.

Reiter, J. P. 2007. Small-sample degrees of freedom for multi-component significance tests with multiple imputation for missing data. Biometrika 94: 502–508. https://doi.org/10.1093/biomet/asm028.

Rubin, D. B. 1987. Multiple Imputation for Nonresponse in Surveys. New York: Wiley.

Also see

- [MI] mi estimate postestimation Postestimation tools for mi estimate
- [MI] mi estimate Estimation using multiple imputations
- [MI] mi estimate using Estimation using previously saved estimation results
- [MI] Intro Introduction to mi
- [MI] Intro substantive Introduction to multiple-imputation analysis
- [MI] Glossary

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