| Description | Syntax | Remarks and examples |
| :--- | :--- | :--- |
| Diagnostics | Reference | Also see |

## Description

spline3 $(x, y)$ returns the coefficients of a cubic natural spline $S(x)$. The elements of $x$ must be strictly monotone increasing.
spline3eval (spline_info, $x$ ) uses the information returned by spline3() to evaluate and return the spline at the abscissas $x$. Elements of the returned result are set to missing if outside the range of the spline. $x$ is assumed to be monotonically increasing.

## Syntax

real matrix $\operatorname{spline3(real~vector~} x$, real vector $y$ )
real vector spline3eval(real matrix spline_info, real vector $x$ )

## Remarks and examples

spline3() and spline3eval() is a translation into Mata of Herriot and Reinsch (CUBNATSPLINE) (1973).

For $x x$ in $\left[x_{i}, x_{i+1}\right)$ :

$$
\mathbf{S}(x x)=\left\{\left(d_{i} t+c_{i}\right) t+b_{i}\right\} t+y_{i}
$$

with $t=x x-x_{i}$.
spline3() returns $(b, c, d, x, y)$ or, if x and y are row vectors, $\left(b, c, d, x^{\prime}, y^{\prime}\right)$.

## Conformability

$$
\begin{array}{rlll}
\text { spline3 }(x, y): & & & \\
x: & n \times 1 & \text { or } & 1 \times n \\
y: & n \times 1 & \text { or } & 1 \times n \\
\text { result: } & n \times 5 & & \\
\text { spline3eval (spline_info, } x): \\
\text { spline_info: } & n \times 5 & \\
x: & m \times 1 & \text { or } & 1 \times m \\
\text { result: } & m \times 1 & \text { or } & 1 \times m
\end{array}
$$

## Diagnostics

spline3 $(x, y)$ requires that $x$ be in ascending order.
spline3eval (spline_info, $x$ ) requires that $x$ be in ascending order.

## Reference

Herriot, J. G., and C. H. Reinsch. 1973. Algorithm 472: Procedures for natural spline interpolation [E1]. Communications of the ACM 16: 763-768. https://doi.org/10.1145/362552.362558.

## Also see

[M-4] Mathematical - Important mathematical functions

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