STATA FUNCTIONS REFERENCE MANUAL RELEASE 18



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Cross-referencing the documentation

When reading this manual, you will find references to other Stata manuals, for example, [U] **27 Overview of Stata estimation commands**; [R] **regress**; and [D] **reshape**. The first example is a reference to chapter 27, Overview of Stata estimation commands, in the User's Guide; the second is a reference to the regress entry in the Base Reference Manual; and the third is a reference to the reshape entry in the Data Management Reference Manual.

All the manuals in the Stata Documentation have a shorthand notation:

[GSM]	Getting Started with Stata for Mac
[GSU]	Getting Started with Stata for Unix
[GSW]	Getting Started with Stata for Windows
[U]	Stata User's Guide
[R]	Stata Base Reference Manual
[ADAPT]	Stata Adaptive Designs: Group Sequential Trials Reference Manual
[BAYES]	Stata Bayesian Analysis Reference Manual
[BMA]	Stata Bayesian Model Averaging Reference Manual
[CAUSAL]	Stata Causal Inference and Treatment-Effects Estimation Reference Manual
[CM]	Stata Choice Models Reference Manual
[D]	Stata Data Management Reference Manual
[DSGE]	Stata Dynamic Stochastic General Equilibrium Models Reference Manual
[ERM]	Stata Extended Regression Models Reference Manual
[FMM]	Stata Finite Mixture Models Reference Manual
[FN]	Stata Functions Reference Manual
[G]	Stata Graphics Reference Manual
[IRT]	Stata Item Response Theory Reference Manual
[LASSO]	Stata Lasso Reference Manual
[XT]	Stata Longitudinal-Data/Panel-Data Reference Manual
[META]	Stata Meta-Analysis Reference Manual
[ME]	Stata Multilevel Mixed-Effects Reference Manual
[MI]	Stata Multiple-Imputation Reference Manual
[MV]	Stata Multivariate Statistics Reference Manual
[PSS]	Stata Power, Precision, and Sample-Size Reference Manual
[P]	Stata Programming Reference Manual
[RPT]	Stata Reporting Reference Manual
[SP]	Stata Spatial Autoregressive Models Reference Manual
[SEM]	Stata Structural Equation Modeling Reference Manual
[SVY]	Stata Survey Data Reference Manual
[ST]	Stata Survival Analysis Reference Manual
[TABLES]	Stata Customizable Tables and Collected Results Reference Manual
[TS]	Stata Time-Series Reference Manual
[I]	Stata Index

[M]

Mata Reference Manual

Title

Intro — Introduction to functions reference manual

Description

This manual describes the functions allowed by Stata. For information on Mata functions, see [M-4] Intro.

A quick note about missing values: Stata denotes a numeric missing value by ., .a, .b, ..., or .z. A string missing value is denoted by "" (the empty string). Here any one of these may be referred to by *missing*. If a numeric value x is missing, then $x \ge .$ is true. If a numeric value x is not missing, then x < . is true.

See [U] 12.2.1 Missing values for details.

Reference

Cox, N. J. 2011. Speaking Stata: Fun and fluency with functions. Stata Journal 11: 460-471.

Also see

[U] 1.3 What's new

Functions by category

Contents

Date and time functions
Mathematical functions
Matrix functions
Programming functions
Random-number functions
Selecting time-span functions
Statistical functions
String functions
Trigonometric functions

Date and time functions

```
age(e_{d DOB}, e_d[, s_{nl}])
                                    the age in integer years on e_d for date of birth e_{d,DOB} with s_{nl} the
                                        nonleap-year birthday for 29feb birthdates
age\_frac(e_{d DOB}, e_d[, s_{nl}])
                                    the age in years, including the fractional part, on e_d for date of birth
                                        e_{d \, \text{DOB}} with s_{nl} the nonleap-year birthday for 29feb birthdates
\mathtt{birthday}(e_{d_{\hspace{0.05cm}\mathsf{DOB}}},Y\lceil,s_{nl}
ceil)
                                    the e_d date of the birthday in year Y for date of birth e_{d_{DOB}} with
                                        s_{nl} the nonleap-year birthday for 29feb birthdates
bofd("cal",e_d)
                                    the e_b business date corresponding to e_d
Cdhms(e_d,h,m,s)
                                    the e_{tC} datetime (ms. with leap seconds since 01jan1960
                                       00:00:00.000) corresponding to e_d, h, m, s
Chms (h, m, s)
                                    the e_{tC} datetime (ms. with leap seconds since 01jan1960
                                       00:00:00.000) corresponding to h, m, s on 01jan1960
Clock(s_1, s_2[, Y])
                                    the e_{tC} datetime (ms. with leap seconds since 01jan1960
                                       00:00:00.000) corresponding to s_1 based on s_2 and Y
\operatorname{clock}(s_1, s_2[, Y])
                                    the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding
                                        to s_1 based on s_2 and Y
Clockdiff (e_{tC1}, e_{tC2}, s_u)
                                    the e_{tC} datetime difference, rounded down to an integer, from
                                        e_{tC1} to e_{tC2} in s_u units of days, hours, minutes, seconds, or
                                        milliseconds
clockdiff(e_{tc1}, e_{tc2}, s_u)
                                    the e_{tc} datetime difference, rounded down to an integer, from e_{tc1} to
                                        e_{tc2} in s_u units of days, hours, minutes, seconds, or milliseconds
Clockdiff_frac(e_{tC1}, e_{tC2}, s_u)
                                    the e_{tC} datetime difference, including the fractional part, from
                                        e_{tC1} to e_{tC2} in s_u units of days, hours, minutes, seconds, or
                                        milliseconds
clockdiff_frac(e_{tc1}, e_{tc2}, s_u)
                                    the e_{tc} datetime difference, including the fractional part, from e_{tc1} to
                                        e_{tc2} in s_u units of days, hours, minutes, seconds, or milliseconds
Clockpart (e_{tC}, s_u)
                                    the integer year, month, day, hour, minute, second, or millisecond
                                       of e_{tC} with s_u specifying which time part
clockpart(e_{tc}, s_u)
                                    the integer year, month, day, hour, minute, second, or millisecond
                                       of e_{tc} with s_u specifying which time part
```

```
Cmdyhms (M, D, Y, h, m, s)
                                 the e_{tC} datetime (ms. with leap seconds since 01jan1960
                                    00:00:00.000) corresponding to M, D, Y, h, m, s
Cofc(e_{tc})
                                 the e_{tC} datetime (ms. with leap seconds since 01jan1960
                                    00:00:00.000) of e_{tc} (ms. without leap seconds since 01jan1960
                                    00:00:00.000)
cofC(e_{tC})
                                 the e_{tc} datetime (ms. without leap seconds since 01jan1960
                                    00:00:00.000) of e_{tC} (ms. with leap seconds since 01jan1960
                                    00:00:00.000)
Cofd(e_d)
                                 the e_{tC} datetime (ms. with leap seconds since 01jan1960
                                    00:00:00.000) of date e_d at time 00:00:00.000
                                 the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) of date e_d at
cofd(e_d)
                                    time 00:00:00.000
daily(s_1, s_2[, Y])
                                 a synonym for date(s_1, s_2 \mid Y \mid)
date(s_1, s_2[, Y])
                                 the e_d date (days since 01jan1960) corresponding to s_1 based on
                                     s_2 and Y
datediff(e_{d1}, e_{d2}, s_u[, s_{nl}])
                                 the difference, rounded down to an integer, from e_{d1} to e_{d2} in
                                     s_u units of days, months, or years with s_{nl} the nonleap-year
                                     anniversary for e_{d1} on 29feb
datediff\_frac(e_{d1}, e_{d2}, s_u | , s_{nl} |)
                                 the difference, including the fractional part, from e_{d1} to e_{d2} in
                                     s_u units of days, months, or years with s_{nl} the nonleap-year
                                     anniversary for e_{d1} on 29feb
                                 the integer year, month, or day of e_d with s_u specifying year, month,
datepart(e_d, s_u)
                                    or day
day(e_d)
                                 the numeric day of the month corresponding to e_d
daysinmonth(e_d)
                                 the number of days in the month of e_d
dayssincedow(e_d,d)
                                 a synonym for dayssinceweekday (e_d, d)
dayssinceweekday(e_d,d)
                                 the number of days until e_d since previous day-of-week d
daysuntildow(e_d,d)
                                 a synonym for daysuntilweekday (e_d, d)
daysuntilweekday(e_d, d)
                                 the number of days from e_d until next day-of-week d
                                 the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding
dhms(e_d,h,m,s)
                                     to e_d, h, m, and s
dmy(D,M,Y)
                                 the e_d date (days since 01jan1960) corresponding to D, M, Y
dofb(e_b, "cal")
                                 the e_d datetime corresponding to e_b
dofC(e_{tC})
                                 the e_d date (days since 01jan1960) of datetime e_{tC} (ms. with leap
                                     seconds since 01jan1960 00:00:00.000)
dofc(e_{tc})
                                 the e_d date (days since 01jan1960) of datetime e_{tc} (ms. since
                                    01jan1960 00:00:00.000)
dofh(e_h)
                                 the e_d date (days since 01jan1960) of the start of half-year e_h
dofm(e_m)
                                 the e_d date (days since 01jan1960) of the start of month e_m
dofq(e_a)
                                 the e_d date (days since 01jan1960) of the start of quarter e_q
dofw(e_w)
                                 the e_d date (days since 01jan1960) of the start of week e_w
dofy(e_y)
                                 the e_d date (days since 01jan1960) of 01jan in year e_q
                                 the numeric day of the week corresponding to date e_d; 0 = \text{Sunday},
dow(e_d)
                                     1 = Monday, \ldots, 6 = Saturday
```

```
doy(e_d)
                                 the numeric day of the year corresponding to date e_d
firstdayofmonth(e_d)
                                 the e_d date of the first day of the month of e_d
firstdowofmonth(M,Y,d)
                                 a synonym for firstweekdayofmonth (M, Y, d)
firstweekdayofmonth(M,Y,d)
                                 the e_d date of the first day-of-week d in month M of year Y
                                 the numeric half of the year corresponding to date e_d
halfyear(e_d)
halfyearly(s_1, s_2[, Y])
                                 the e_h half-yearly date (half-years since 1960h1) corresponding to
                                    s_1 based on s_2 and Y; Y specifies topyear; see date()
hh(e_{tc})
                                 the hour corresponding to datetime e_{tc} (ms. since 01jan1960
                                    00:00:00.000)
hhC(e_{tC})
                                 the hour corresponding to datetime e_{tC} (ms. with leap seconds since
                                    01jan1960 00:00:00.000)
hms(h,m,s)
                                 the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding
                                    to h, m, s on 01jan1960
hofd(e_d)
                                 the e_h half-yearly date (half years since 1960h1) containing date e_d
hours(ms)
                                 ms/3,600,000
isleapsecond(e_{tC})
                                 1 if e_{tC} is a leap second; otherwise, 0
isleapyear(Y)
                                 1 if Y is a leap year; otherwise, 0
lastdayofmonth(e_d)
                                 the e_d date of the last day of the month of e_d
lastdowofmonth (M, Y, d)
                                 a synonym for lastweekdayofmonth (M, Y, d)
lastweekdayofmonth (M, Y, d)
                                 the e_d date of the last day-of-week d in month M of year Y
mdy(M,D,Y)
                                 the e_d date (days since 01jan1960) corresponding to M, D, Y
mdyhms(M, D, Y, h, m, s)
                                 the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding
                                    to M, D, Y, h, m, s
                                 ms/60,000
minutes(ms)
mm(e_{tc})
                                 the minute corresponding to datetime e_{tc} (ms. since 01jan1960
                                    00:00:00.000)
mmC(e_{tC})
                                 the minute corresponding to datetime e_{tC} (ms. with leap seconds
                                    since 01jan1960 00:00:00.000)
mofd(e_d)
                                 the e_m monthly date (months since 1960m1) containing date e_d
month(e_d)
                                 the numeric month corresponding to date e_d
monthly (s_1, s_2 \mid Y \mid)
                                 the e_m monthly date (months since 1960m1) corresponding to s_1
                                    based on s_2 and Y; Y specifies topyear; see date()
msofhours(h)
                                 h \times 3,600,000
msofminutes(m)
                                 m \times 60,000
msofseconds(s)
                                 s \times 1,000
nextbirthday(e_{d \text{ DOB}}, e_d[, s_{nl}])
                                 the e_d date of the first birthday after e_d for date of birth e_{d_{DOB}}
                                    with s_{nl} the nonleap-year birthday for 29feb birthdates
nextdow(e_d,d)
                                 a synonym for nextweekday (e_d, d)
                                 the first leap year after year Y
nextleapyear(Y)
nextweekday(e_d,d)
                                 the e_d date of the first day-of-week d after e_d
now()
                                 the current e_{tc} datetime
```

```
previousbirthday(e_{d \text{ DOB}}, e_d[, s_{nl}])
                                 the e_d date of the birthday immediately before e_d for date of birth
                                    e_{d \, \text{DOB}} with s_{nl} the nonleap-year birthday for 29feb birthdates
                                 a synonym for previousweekday (e_d, d)
previousdow(e_d,d)
previousleapyear(Y)
                                 the leap year immediately before year Y
previousweekday(e_d,d)
                                 the e_d date of the last day-of-week d before e_d
qofd(e_d)
                                 the e_q quarterly date (quarters since 1960q1) containing date e_d
quarter(e_d)
                                 the numeric quarter of the year corresponding to date e_d
quarterly(s_1, s_2[,Y])
                                 the e_q quarterly date (quarters since 1960q1) corresponding to s_1
                                    based on s_2 and Y; Y specifies topyear, see date()
seconds(ms)
                                 ms/1,000
ss(e_{tc})
                                 the second corresponding to datetime e_{tc} (ms. since 01jan1960
                                    00:00:00.000
ssC(e_{tC})
                                 the second corresponding to datetime e_{tC} (ms. with leap seconds
                                    since 01jan1960 00:00:00.000)
tC(l)
                                 convenience function to make typing dates and times in expressions
                                    easier
tc(l)
                                 convenience function to make typing dates and times in expressions
td(l)
                                 convenience function to make typing dates in expressions easier
th(l)
                                 convenience function to make typing half-yearly dates in expressions
tm(l)
                                 convenience function to make typing monthly dates in expressions
                                    easier
today()
                                 today's e_d date
tq(l)
                                 convenience function to make typing quarterly dates in expressions
                                    easier
tw(l)
                                 convenience function to make typing weekly dates in expressions
week(e_d)
                                 the numeric week of the year corresponding to date e_d, the %td
                                    encoded date (days since 01jan1960)
weekly(s_1, s_2[, Y])
                                 the e_w weekly date (weeks since 1960w1) corresponding to s_1
                                    based on s_2 and Y; Y specifies topyear; see date()
wofd(e_d)
                                 the e_w weekly date (weeks since 1960w1) containing date e_d
year(e_d)
                                 the numeric year corresponding to date e_d
yearly(s_1, s_2[, Y])
                                 the e_y yearly date (year) corresponding to s_1 based on s_2 and Y;
                                    Y specifies topyear; see date()
                                 the e_h half-yearly date (half-years since 1960h1) corresponding to
yh(Y, H)
                                    year Y, half-year H
ym(Y, M)
                                 the e_m monthly date (months since 1960m1) corresponding to year
                                    Y, month M
yofd(e_d)
                                 the e_y yearly date (year) containing date e_d
yq(Y,Q)
                                 the e_q quarterly date (quarters since 1960q1) corresponding to year
                                    Y, quarter Q
yw(Y,W)
                                 the e_w weekly date (weeks since 1960w1) corresponding to year Y,
                                    week W
```

Mathematical functions

```
the absolute value of x
abs(x)
ceil(x)
                                the unique integer n such that n-1 < x \le n; x (not ".") if x is
                                   missing, meaning that ceil(.a) = .a
                                the complementary \log - \log of x
cloglog(x)
                                the combinatorial function n!/\{k!(n-k)!\}
comb(n,k)
digamma(x)
                                the digamma() function, d \ln \Gamma(x)/dx
                                the exponential function e^x
exp(x)
                                e^x - 1 with higher precision than \exp(x) - 1 for small values of
expm1(x)
floor(x)
                                the unique integer n such that n \le x < n+1; x (not ".") if x is
                                   missing, meaning that floor(.a) = .a
int(x)
                                the integer obtained by truncating x toward 0 (thus, int (5.2) = 5
                                    and int(-5.8) = -5); x (not ".") if x is missing, meaning
                                    that int(.a) = .a
                                the inverse of the complementary log-log function of x
invcloglog(x)
invlogit(x)
                                the inverse of the logit function of x
ln(x)
                                the natural logarithm, ln(x)
ln1m(x)
                                the natural logarithm of 1-x with higher precision than ln(1-x)
                                   for small values of |x|
ln1p(x)
                                the natural logarithm of 1+x with higher precision than ln(1+x)
                                   for small values of |x|
lnfactorial(n)
                                the natural log of n factorial = ln(n!)
                                ln{\Gamma(x)}
lngamma(x)
log(x)
                                a synonym for ln(x)
log10(x)
                                the base-10 logarithm of x
log1m(x)
                                a synonym for ln1m(x)
log1p(x)
                                a synonym for ln1p(x)
logit(x)
                                the log of the odds ratio of x, logit(x) = \ln \{x/(1-x)\}\
\max(x_1, x_2, \ldots, x_n)
                                the maximum value of x_1, x_2, \ldots, x_n
\min(x_1, x_2, \ldots, x_n)
                                the minimum value of x_1, x_2, \ldots, x_n
mod(x,y)
                                the modulus of x with respect to y
reldif(x,y)
                                the "relative" difference |x-y|/(|y|+1); 0 if both arguments are
                                   the same type of extended missing value; missing if only one
                                    argument is missing or if the two arguments are two different
                                   types of missing
round(x,y) or round(x)
                                x rounded in units of y or x rounded to the nearest integer if the
                                    argument y is omitted; x (not ".") if x is missing (meaning
                                    that round(.a) = .a and that round(.a, y) = .a if y is not
                                    missing) and if y is missing, then "." is returned
                                the sign of x: -1 if x < 0, 0 if x = 0, 1 if x > 0, or missing if
sign(x)
                                    x is missing
                                the square root of x
sqrt(x)
sum(x)
                                the running sum of x, treating missing values as zero
```

```
the second derivative of lngamma(x) = d^2 ln\Gamma(x)/dx^2
    trigamma(x)
    trunc(x)
                                    a synonym for int(x)
Matrix functions
    cholesky(M)
                                    the Cholesky decomposition of the matrix: if R = \text{cholesky}(S),
                                       then RR^T = S
                                    the equation number of M associated with column equation s;
    coleqnumb(M,s)
                                       missing if the column equation cannot be found
    colnfreeparms(M)
                                    the number of free parameters in columns of M
                                    the column number of M associated with column name s; missing
    colnumb(M,s)
                                       if the column cannot be found
                                    the number of columns of M
    colsof(M)
                                    the correlation matrix of the variance matrix
    corr(M)
    det(M)
                                    the determinant of matrix M
    diag(M)
                                    the square, diagonal matrix created from the row or column vector
    diag0cnt(M)
                                    the number of zeros on the diagonal of M
                                    s[floor(i),floor(j)], the i,j element of the matrix named s;
    el(s,i,j)
                                       missing if i or j are out of range or if matrix s does not exist
                                    a copy of Stata internal system matrix systemname
    get(systemname)
    hadamard(M,N)
                                    a matrix whose i, j element is M[i,j] \cdot N[i,j] (if M and N are
                                       not the same size, this function reports a conformability error)
    I(n)
                                    an n \times n identity matrix if n is an integer; otherwise, a round (n) \times n
                                       round(n) identity matrix
    inv(M)
                                    the inverse of the matrix M
                                    the inverse of M if M is positive definite
    invsym(M)
    invvech(M)
                                    a symmetric matrix formed by filling in the columns of the lower
                                       triangle from a row or column vector
    invvecp(M)
                                    a symmetric matrix formed by filling in the columns of the upper
                                       triangle from a row or column vector
    issymmetric(M)
                                    1 if the matrix is symmetric; otherwise, 0
    J(r,c,z)
                                    the r \times c matrix containing elements z
    matmissing(M)
                                    1 if any elements of the matrix are missing; otherwise, 0
    matuniform(r,c)
                                    the r \times c matrices containing uniformly distributed pseudorandom
                                       numbers on the interval (0, 1)
                                    the relative difference of X and Y, where the relative difference is
    mreldif(X,Y)
                                       defined as \max_{i,j} \{ |x_{ij} - y_{ij}|/(|y_{ij}| + 1) \}
                                    use with the row-join (,) and column-join (\) operators
    nullmat(matname)
    roweqnumb(M,s)
                                    the equation number of M associated with row equation s; missing
                                       if the row equation cannot be found
                                    the number of free parameters in rows of M
    rownfreeparms(M)
    rownumb(M,s)
                                    the row number of M associated with row name s; missing if the
```

row cannot be found the number of rows of M

rowsof(M)

sweep(M,i)	matrix M with i th row/column swept
trace(M)	the trace of matrix M
vec(M)	a column vector formed by listing the elements of M , starting with the first column and proceeding column by column
$\mathtt{vecdiag}(M)$	the row vector containing the diagonal of matrix M
$\operatorname{vech}(M)$	a column vector formed by listing the lower triangle elements of M
vecp(M)	a column vector formed by listing the upper triangle elements of ${\cal M}$

Programming functions

$autocode(x,n,x_0,x_1)$	partitions the interval from x_0 to x_1 into n equal-length intervals and returns the upper bound of the interval that contains x or the upper bound of the first or last interval if $x < x_0$ or $x > x_1$, respectively
byteorder()	1 if your computer stores numbers by using a hilo byte order and evaluates to 2 if your computer stores numbers by using a lohi byte order
c(name)	the value of the system or constant result c(name) (see [P] creturn)
_caller()	version of the program or session that invoked the currently running program; see [P] version
$chop(x, \epsilon)$	round(x) if abs(x - round(x)) < ϵ ; otherwise, x; or x if x is missing
clip(x,a,b)	x if $a < x < b$, b if $x \ge b$, a if $x \le a$, or missing if x is missing or if $a > b$; x if x is missing
cond(x,a,b[,c])	a if x is true and nonmissing, b if x is false, and c if x is missing; a if c is not specified and x evaluates to missing
e(name)	the value of stored result e(name); see [U] 18.8 Accessing results calculated by other programs
e(sample)	1 if the observation is in the estimation sample and 0 otherwise
epsdouble()	the machine precision of a double-precision number
epsfloat()	the machine precision of a floating-point number
${\tt fileexists}(f)$	1 if the file specified by f exists; otherwise, 0
fileread(f)	the contents of the file specified by f
filereaderror(s)	0 or positive integer, said value having the interpretation of a return code
filewrite(f,s[,r])	writes the string specified by s to the file specified by f and returns the number of bytes in the resulting file
float(x)	the value of x rounded to float precision
fmtwidth(fmtstr)	the output length of the %fmt contained in fmtstr; missing if fmtstr does not contain a valid %fmt
frval()	returns values of variables stored in other frames
_frval()	<pre>programmer's version of frval()</pre>
has_eprop(name)	1 if <i>name</i> appears as a word in e(properties); otherwise, 0

```
inlist(z,a,b,...)
                                  1 if z is a member of the remaining arguments; otherwise, 0
inrange(z,a,b)
                                  1 if it is known that a \le z \le b; otherwise, 0
irecode(x, x_1, \ldots, x_n)
                                  missing if x is missing or x_1, \ldots, x_n is not weakly increasing; 0
                                     if x \le x_1; 1 if x_1 < x \le x_2; 2 if x_2 < x \le x_3; ...; n if
                                     x > x_n
                                  restricts name interpretation to scalars and matrices; see scalar()
matrix(exp)
maxbyte()
                                  the largest value that can be stored in storage type byte
maxdouble()
                                  the largest value that can be stored in storage type double
maxfloat()
                                  the largest value that can be stored in storage type float
maxint()
                                  the largest value that can be stored in storage type int
maxlong()
                                  the largest value that can be stored in storage type long
mi(x_1, x_2, \ldots, x_n)
                                  a synonym for missing (x_1, x_2, \ldots, x_n)
                                  the smallest value that can be stored in storage type byte
minbyte()
mindouble()
                                  the smallest value that can be stored in storage type double
minfloat()
                                  the smallest value that can be stored in storage type float
minint()
                                  the smallest value that can be stored in storage type int
minlong()
                                  the smallest value that can be stored in storage type long
missing(x_1, x_2, \ldots, x_n)
                                  1 if any x_i evaluates to missing; otherwise, 0
r(name)
                                  the value of the stored result r(name); see [U] 18.8 Accessing
                                     results calculated by other programs
recode(x, x_1, \ldots, x_n)
                                  missing if x_1, x_2, \dots, x_n is not weakly increasing; x if x is missing;
                                     x_1 if x \le x_1; x_2 if x \le x_2, ...; otherwise, x_n if x > x_1, x_2,
                                     \dots, x_{n-1}. x_i \ge \dots is interpreted as x_i = +\infty
                                  1 if the first nonblank character of local macro '0' is a comma, or
replay()
                                     if '0' is empty
return(name)
                                  the value of the to-be-stored result r(name); see [P] return
                                  the value of stored result s(name); see [U] 18.8 Accessing results
s(name)
                                     calculated by other programs
scalar(exp)
                                  restricts name interpretation to scalars and matrices
smallestdouble()
                                  the smallest double-precision number greater than zero
```

Ra

ta(a,b) random variates, where a and b are the beta distribution shape parameters
nomial (n,p) random variates, where n is the number of trials and p is the success probability
auchy(a,b) random variates, where a is the location parameter and b is the scale parameter
, with df degrees of freedom, random variates
ponential random variates with scale b
$\operatorname{mma}(a,b)$ random variates, where a is the gamma shape parameter and b is the scale parameter

rhypergeometric(N, K, n)	hypergeometric random variates
rigaussian (m,a)	inverse Gaussian random variates with mean m and shape parameter a
rlaplace(m,b)	$\operatorname{Laplace}(m,b)$ random variates with mean m and scale parameter b
rlogistic()	logistic variates with mean 0 and standard deviation $\pi/\sqrt{3}$
rlogistic(s)	logistic variates with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$
${\tt rlogistic}(m,s)$	logistic variates with mean m , scale s , and standard deviation $s\pi/\sqrt{3}$
rnbinomial(n,p)	negative binomial random variates
rnormal()	standard normal (Gaussian) random variates, that is, variates from a normal distribution with a mean of 0 and a standard deviation of 1
rnormal(m)	normal $(m,1)$ (Gaussian) random variates, where m is the mean and the standard deviation is 1
rnormal(m,s)	normal (m,s) (Gaussian) random variates, where m is the mean and s is the standard deviation
${\tt rpoisson}(m)$	$\operatorname{Poisson}(m)$ random variates, where m is the distribution mean
$\mathtt{rt}(df)$	Student's t random variates, where df is the degrees of freedom
<pre>runiform()</pre>	uniformly distributed random variates over the interval $(0,1)$
runiform(a,b)	uniformly distributed random variates over the interval (a,b)
runiformint(a,b)	uniformly distributed random integer variates on the interval $[a, b]$
rweibull(a,b)	Weibull variates with shape a and scale b
rweibull(a,b,g)	Weibull variates with shape a , scale b , and location g
rweibullph(a,b)	Weibull (proportional hazards) variates with shape a and scale b
${\tt rweibullph}(a,b,g)$	Weibull (proportional hazards) variates with shape a , scale b , and location g

Selecting time-span functions

$tin(d_1, d_2)$	true if $d_1 \leq t \leq d_2$, where t is the time variable previously tsset
$twithin(d_1,d_2)$	true if $d_1 < t < d_2$, where t is the time variable previously tsse

Statistical functions

tatistical functions	
betaden(a,b,x)	the probability density of the beta distribution, where a and b are the shape parameters; 0 if $x<0$ or $x>1$
$\texttt{binomial}(n, k, \theta)$	the probability of observing $floor(k)$ or fewer successes in $floor(n)$ trials when the probability of a success on one trial is θ ; 0 if $k < 0$; or 1 if $k > n$
binomialp(n, k, p)	the probability of observing $floor(k)$ successes in $floor(n)$ trials when the probability of a success on one trial is p
$\texttt{binomialtail}(n,k,\theta)$	the probability of observing $floor(k)$ or more successes in $floor(n)$ trials when the probability of a success on one trial is θ ; 1 if $k < 0$; or 0 if $k > n$

```
the joint cumulative distribution \Phi(h, k, \rho) of bivariate normal with
binormal(h, k, \rho)
                                      correlation \rho
cauchy (a,b,x)
                                   the cumulative Cauchy distribution with location parameter a and
                                      scale parameter b
                                   the probability density of the Cauchy distribution with location
cauchyden(a,b,x)
                                      parameter a and scale parameter b
cauchytail(a,b,x)
                                   the reverse cumulative (upper tail or survivor) Cauchy distribution
                                      with location parameter a and scale parameter b
                                  the cumulative \chi^2 distribution with df degrees of freedom; 0 if
chi2(df,x)
                                  the probability density of the \chi^2 distribution with df degrees of
chi2den(df,x)
                                      freedom; 0 if x < 0
                                  the reverse cumulative (upper tail or survivor) \chi^2 distribution with
chi2tail(df,x)
                                      df degrees of freedom; 1 if x < 0
                                   \frac{\partial P(a,x)}{\partial x}, where P(a,x)=\mathrm{gammap}(a,x); 0 if x<0
dgammapda(a,x)
                                   \frac{\partial^2 P(a,x)}{\partial a^2}, where P(a,x)= gammap(a,x); 0 if x<0
dgammapdada(a,x)
                                   \frac{\partial^2 P(a,x)}{\partial a \partial x}, where P(a,x) = \mathrm{gammap(}a\,\mathrm{,}x\mathrm{)};\,\mathrm{0} if x<0
dgammapdadx(a,x)
                                   \frac{\partial P(a,x)}{\partial x}, where P(a,x)= gammap(a,x); 0 if x<0
dgammapdx(a,x)
                                   \frac{\partial^2 P(a,x)}{\partial x^2}, where P(a,x) = \text{gammap}(a,x); 0 if x < 0
dgammapdxdx(a,x)
                                   the cumulative multiple range distribution that is used in Dunnett's
dunnettprob(k, df, x)
                                      multiple-comparison method with k ranges and df degrees of
                                      freedom; 0 if x < 0
                                   the cumulative exponential distribution with scale b
exponential (b,x)
exponentialden(b, x)
                                   the probability density function of the exponential distribution with
                                      scale b
exponential tail(b,x)
                                   the reverse cumulative exponential distribution with scale b
                                  the cumulative F distribution with df_1 numerator and df_2 denomina-
F(df_1, df_2, f)
                                      tor degrees of freedom: F(df_1, df_2, f) = \int_0^f Fden(df_1, df_2, t)
                                      dt; 0 if f < 0
                                  the probability density function of the F distribution with df_1 nu-
Fden(df_1, df_2, f)
                                      merator and df_2 denominator degrees of freedom; 0 if f < 0
                                   the reverse cumulative (upper tail or survivor) F distribution with
Ftail(df_1, df_2, f)
                                      df_1 numerator and df_2 denominator degrees of freedom; 1 if
                                      f < 0
gammaden(a,b,g,x)
                                   the probability density function of the gamma distribution; 0 if
                                      x < g
                                   the cumulative gamma distribution with shape parameter a; 0 if
gammap(a,x)
                                   the reverse cumulative (upper tail or survivor) gamma distribution
gammaptail(a,x)
                                      with shape parameter a; 1 if x < 0
hypergeometric (N, K, n, k)
                                  the cumulative probability of the hypergeometric distribution
hypergeometric (N, K, n, k) the hypergeometric probability of k successes out of a sample of
                                      size n, from a population of size N containing K elements that
                                      have the attribute of interest
                                   the cumulative beta distribution with shape parameters a and b; 0
ibeta(a,b,x)
                                      if x < 0; or 1 if x > 1
```

```
ibetatail(a,b,x)
                               the reverse cumulative (upper tail or survivor) beta distribution with
                                  shape parameters a and b; 1 if x < 0; or 0 if x > 1
                               the cumulative inverse Gaussian distribution with mean m and shape
igaussian(m,a,x)
                                  parameter a; 0 if x < 0
                               the probability density of the inverse Gaussian distribution with
igaussianden(m,a,x)
                                  mean m and shape parameter a; 0 if x < 0
                               the reverse cumulative (upper tail or survivor) inverse Gaussian
igaussiantail(m,a,x)
                                  distribution with mean m and shape parameter a; 1 if x < 0
invbinomial(n,k,p)
                               the inverse of the cumulative binomial; that is, \theta (\theta = probability
                                  of success on one trial) such that the probability of observing
                                  floor(k) or fewer successes in floor(n) trials is p
                               the inverse of the right cumulative binomial; that is, \theta (\theta = probabil-
invbinomialtail(n, k, p)
                                  ity of success on one trial) such that the probability of observing
                                  floor(k) or more successes in floor(n) trials is p
invcauchy(a,b,p)
                               the inverse of cauchy(): if cauchy(a,b,x) = p, then
                                  invcauchy(a,b,p) = x
                               the inverse of cauchytail(): if cauchytail(a,b,x) = p, then
invcauchytail (a,b,p)
                                  invcauchytail(a,b,p) = x
                               the inverse of chi2(): if chi2(df, x) = p, then invchi2(df, p) =
invchi2(df,p)
                               the inverse of chi2tail(): if chi2tail(df,x) = p, then
invchi2tail(df, p)
                                  invchi2tail(df,p) = x
                               the inverse cumulative multiple range distribution that is used in
invdunnettprob(k, df, p)
                                  Dunnett's multiple-comparison method with k ranges and df
                                  degrees of freedom
                               the inverse cumulative exponential distribution with scale b: if
invexponential (b, p)
                                  exponential(b,x) = p, then invexponential(b,p) = x
invexponential tail(b, p)
                               the inverse reverse cumulative exponential distribution with scale b:
                                  if exponentialtail(b, x) = p, then
                                  invexponentialtail(b, p) = x
invF(df_1, df_2, p)
                               the inverse cumulative F distribution: if F(df_1, df_2, f) = p, then
                                  invF(df_1, df_2, p) = f
invFtail(df_1, df_2, p)
                               the inverse reverse cumulative (upper tail or survivor) {\cal F} distribution:
                                  if Ftail(df_1, df_2, f) = p, then invFtail(df_1, df_2, p) = f
                               the inverse cumulative gamma distribution: if gammap(a, x) = p,
invgammap(a, p)
                                  then invgammap(a, p) = x
                               the inverse reverse cumulative (upper tail or survivor) gamma distri-
invgammaptail(a,p)
                                  bution: if gammaptail(a, x) = p, then invgammaptail(a, p)
invibeta(a,b,p)
                               the inverse cumulative beta distribution: if ibeta(a,b,x) = p,
                                  then invibeta(a,b,p)=x
invibetatail(a,b,p)
                               the inverse reverse cumulative (upper tail or survivor) beta distribu-
                                  tion: if ibetatail(a,b,x) = p, then invibetatail(a,b,p)
                                  = x
invigaussian(m,a,p)
                               the inverse of igaussian(): if
                                  igaussian(m,a,x) = p, then invigaussian(m,a,p) = x
                               the inverse of igaussiantail(): if
invigaussiantail(m, a, p)
                                  igaussiantail(m,a,x)=p, then
                                  invigaussiantail(m,a,p)=x
```

```
the inverse of laplace(): if laplace(m,b,x) = p, then
invlaplace(m,b,p)
                                  invlaplace(m,b,p) = x
                               the inverse of laplacetail(): if laplacetail(m, b, x) = p,
invlaplacetail(m, b, p)
                                  then invlaplacetail(m, b, p) = x
                               the inverse cumulative logistic distribution: if logistic(x) = p,
invlogistic(p)
                                  then invlogistic(p) = x
                               the inverse cumulative logistic distribution: if logistic(s, x) = p,
invlogistic(s,p)
                                  then invlogistic(s,p) = x
                               the inverse cumulative logistic distribution: if logistic(m,s,x)
invlogistic(m,s,p)
                                  = p, then invlogistic(m, s, p) = x
                               the inverse reverse cumulative logistic distribution: if
invlogistictail(p)
                                  logistictail(x) = p, then invlogistictail(p) = x
                               the inverse reverse cumulative logistic distribution: if
invlogistictail(s,p)
                                  logistictail(s,x) = p, then invlogistictail(s,p) = x
invlogistictail(m, s, p)
                               the inverse reverse cumulative logistic distribution: if
                                  logistictail(m,s,x) = p, then
                                  invlogistictail(m,s,p) = x
                               the value of the negative binomial parameter, p, such that q =
invnbinomial (n, k, q)
                                  nbinomial(n,k,p)
invnbinomialtail(n, k, q)
                               the value of the negative binomial parameter, p, such that
                                  q = nbinomialtail(n, k, p)
                               the inverse cumulative noncentral \chi^2 distribution: if
invnchi2(df, np, p)
                                  nchi2(df, np, x) = p, then invnchi2(df, np, p) = x
                               the inverse reverse cumulative (upper tail or survivor) non-
invnchi2tail(df, np, p)
                                 central \chi^2 distribution: if nchi2tail(df, np, x) = p, then
                                  invnchi2tail(df, np, p) = x
invnF(df_1, df_2, np, p)
                               the inverse cumulative noncentral F distribution: if
                                  nF(df_1, df_2, np, f) = p, then invnF(df_1, df_2, np, p) = f
invnFtail(df_1, df_2, np, p)
                               the inverse reverse cumulative (upper tail or survivor) noncen-
                                  tral F distribution: if nFtail(df_1, df_2, np, f) = p, then
                                  invnFtail(df_1, df_2, np, p) = f
invnibeta(a,b,np,p)
                               the inverse cumulative noncentral beta distribution: if
                                  nibeta(a,b,np,x) = p, then invibeta(a,b,np,p) = x
                               the inverse cumulative standard normal distribution: if normal(z)
invnormal(p)
                                  = p, then invnormal(p) = z
invnt(df, np, p)
                               the inverse cumulative noncentral Student's t distribution: if
                                  nt(df, np, t) = p, then invnt(df, np, p) = t
                               the inverse reverse cumulative (upper tail or survivor) noncen-
invnttail(df, np, p)
                                  tral Student's t distribution: if nttail(df, np, t) = p, then
                                  invnttail(df, np, p) = t
                               the Poisson mean such that the cumulative Poisson distribution eval-
invpoisson(k,p)
                                  uated at k is p: if poisson(m, k) = p, then invpoisson(k, p)
                               the Poisson mean such that the reverse cumulative Poisson distri-
invpoissontail(k,q)
                                  bution evaluated at k is q: if poissontail(m,k) = q, then
                                  invpoissontail(k,q) = m
                               the inverse cumulative Student's t distribution: if t(df,t) = p,
invt(df,p)
                                  then invt(df, p) = t
```

```
the inverse reverse cumulative (upper tail or survivor) Student's
invttail(df, p)
                                  t distribution: if ttail(df, t) = p, then invttail(df, p) = t
invtukeyprob(k, df, p)
                               the inverse cumulative Tukey's Studentized range distribution with
                                  k ranges and df degrees of freedom
                               the inverse cumulative Weibull distribution with shape a and scale
invweibull(a,b,p)
                                  b: if weibull (a,b,x) = p, then invweibull (a,b,p) = x
invweibull(a,b,g,p)
                               the inverse cumulative Weibull distribution with shape a, scale b,
                                  and location g: if weibull(a,b,g,x) = p, then
                                  invweibull(a,b,g,p) = x
                               the inverse cumulative Weibull (proportional hazards) distribution
invweibullph(a,b,p)
                                  with shape a and scale b: if weibullph(a,b,x) = p, then
                                  invweibullph(a,b,p) = x
invweibullph(a,b,g,p)
                               the inverse cumulative Weibull (proportional hazards) distribution
                                  with shape a, scale b, and location g: if weibullph(a, b, g, x) =
                                  p, then invweibullph(a,b,g,p) = x
                               the inverse reverse cumulative Weibull (proportional hazards) distri-
invweibullphtail(a, b, p)
                                  bution with shape a and scale b: if weibullphtail(a,b,x) = p,
                                  then invweibullphtail(a,b,p) = x
invweibullphtail(a,b,g,p)
                               the inverse reverse cumulative Weibull (proportional hazards)
                                  distribution with shape a, scale b, and location g: if
                                  weibullphtail(a,b,g,x) = p, then
                                  invweibullphtail(a,b,g,p) = x
                               the inverse reverse cumulative Weibull distribution with shape a and
invweibulltail(a,b,p)
                                  scale b: if weibulltail(a,b,x) = p, then
                                  invweibulltail(a,b,p) = x
                               the inverse reverse cumulative Weibull distribution with shape a,
invweibulltail(a, b, g, p)
                                  scale b, and location g: if weibulltail(a,b,g,x) = p, then
                                  invweibulltail(a,b,g,p) = x
laplace(m,b,x)
                               the cumulative Laplace distribution with mean m and scale param-
laplaceden(m,b,x)
                               the probability density of the Laplace distribution with mean m and
                                  scale parameter b
                               the reverse cumulative (upper tail or survivor) Laplace distribution
laplacetail(m,b,x)
                                  with mean m and scale parameter b
                               the natural logarithm of the density of the Cauchy distribution with
lncauchyden(a,b,x)
                                  location parameter a and scale parameter b
                               the natural logarithm of the inverse gamma density, where a is the
lnigammaden(a,b,x)
                                  shape parameter and b is the scale parameter
lnigaussianden(m,a,x)
                               the natural logarithm of the inverse Gaussian density with mean m
                                  and shape parameter a
lniwishartden(df, V, X)
                               the natural logarithm of the density of the inverse Wishart distribu-
                                  tion; missing if df \leq n-1
lnlaplaceden(m,b,x)
                               the natural logarithm of the density of the Laplace distribution with
                                  mean m and scale parameter b
                               the natural logarithm of the multivariate normal density
lnmvnormalden(M, V, X)
lnnormal(z)
                               the natural logarithm of the cumulative standard normal distribution
lnnormalden(z)
                               the natural logarithm of the standard normal density, N(0,1)
```

```
lnnormalden(x, \sigma)
lnnormalden(x, \mu, \sigma)
lnwishartden(df, V, X)
logistic(x)
logistic(s,x)
logistic(m,s,x)
logisticden(x)
logisticden(s,x)
logisticden(m,s,x)
logistictail(x)
logistictail(s,x)
logistictail(m,s,x)
nbetaden(a,b,np,x)
nbinomial(n,k,p)
nbinomialp(n,k,p)
nbinomialtail(n,k,p)
nchi2(df, np, x)
nchi2den(df, np, x)
nchi2tail(df, np, x)
nF(df_1, df_2, np, f)
nFden(df_1, df_2, np, f)
nFtail(df_1, df_2, np, f)
nibeta(a,b,np,x)
normal(z)
```

the natural logarithm of the normal density with mean 0 and standard deviation σ the natural logarithm of the normal density with mean μ and standard deviation σ , $N(\mu, \sigma^2)$ the natural logarithm of the density of the Wishart distribution; missing if $df \leq n-1$ the cumulative logistic distribution with mean 0 and standard deviation $\pi/\sqrt{3}$ the cumulative logistic distribution with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$ the cumulative logistic distribution with mean m, scale s, and standard deviation $s\pi/\sqrt{3}$ the density of the logistic distribution with mean 0 and standard deviation $\pi/\sqrt{3}$ the density of the logistic distribution with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$ the density of the logistic distribution with mean m, scale s, and standard deviation $s\pi/\sqrt{3}$ the reverse cumulative logistic distribution with mean 0 and standard deviation $\pi/\sqrt{3}$ the reverse cumulative logistic distribution with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$ the reverse cumulative logistic distribution with mean m, scale s, and standard deviation $s\pi/\sqrt{3}$ the probability density function of the noncentral beta distribution; 0 if x < 0 or x > 1the cumulative probability of the negative binomial distribution the negative binomial probability the reverse cumulative probability of the negative binomial distribution the cumulative noncentral χ^2 distribution; 0 if x < 0

the probability density of the noncentral χ^2 distribution; 0 if x<0

the reverse cumulative (upper tail or survivor) noncentral χ^2 distri-

the cumulative noncentral F distribution with df_1 numerator and df_2 denominator degrees of freedom and noncentrality parameter

the probability density function of the noncentral F distribution with df_1 numerator and df_2 denominator degrees of freedom and

the reverse cumulative (upper tail or survivor) noncentral F distribution with df_1 numerator and df_2 denominator degrees of

the cumulative noncentral beta distribution; 0 if x < 0; or 1 if

freedom and noncentrality parameter np; 1 if f < 0

noncentrality parameter np; 0 if f < 0

the cumulative standard normal distribution

bution; 1 if x < 0

np; 0 if f < 0

```
normalden(z)
                               the standard normal density, N(0,1)
normalden(x, \sigma)
normalden(x, \mu, \sigma)
npnchi2(df,x,p)
npnF(df_1, df_2, f, p)
npnt(df,t,p)
nt(df, np, t)
ntden(df, np, t)
                                  rameter np
nttail(df, np, t)
                                  rameter np
poisson(m,k)
poissonp(m,k)
                                  as Poisson with mean m
poissontail(m,k)
t(df,t)
tden(df,t)
ttail(df,t)
                                  the probability T > t
tukeyprob(k, df, x)
weibull(a,b,x)
weibull(a,b,g,x)
                                  location q
weibullden(a,b,x)
                                  shape a and scale b
weibullden(a,b,q,x)
                                  shape a, scale b, and location q
weibullph(a,b,x)
                                  a and scale b
weibullph(a,b,g,x)
                                  a, scale b, and location q
weibullphden(a,b,x)
weibullphden(a,b,g,x)
                                  distribution with shape a, scale b, and location g
                               the reverse cumulative Weibull (proportional hazards) distribution
weibullphtail(a,b,x)
                                  with shape a and scale b
weibullphtail(a,b,q,x)
                               the reverse cumulative Weibull (proportional hazards) distribution
                                  with shape a, scale b, and location g
```

the normal density with mean 0 and standard deviation σ the normal density with mean μ and standard deviation σ , $N(\mu, \sigma^2)$ the noncentrality parameter, np, for noncentral χ^2 : if nchi2(df, np, x) = p, then npnchi2(df, x, p) = npthe noncentrality parameter, np, for the noncentral F: if $nF(df_1, df_2, np, f) = p$, then $npnF(df_1, df_2, f, p) = np$ the noncentrality parameter, np, for the noncentral Student's t distribution: if nt(df, np, t) = p, then npnt(df, t, p) = npthe cumulative noncentral Student's t distribution with df degrees of freedom and noncentrality parameter npthe probability density function of the noncentral Student's t distribution with df degrees of freedom and noncentrality pathe reverse cumulative (upper tail or survivor) noncentral Student's t distribution with df degrees of freedom and noncentrality pathe probability of observing floor(k) or fewer outcomes that are distributed as Poisson with mean m the probability of observing floor(k) outcomes that are distributed the probability of observing floor(k) or more outcomes that are distributed as Poisson with mean m the cumulative Student's t distribution with df degrees of freedom the probability density function of Student's t distribution the reverse cumulative (upper tail or survivor) Student's t distribution; the cumulative Tukey's Studentized range distribution with k ranges and df degrees of freedom; 0 if x < 0the cumulative Weibull distribution with shape a and scale b the cumulative Weibull distribution with shape a, scale b, and the probability density function of the Weibull distribution with the probability density function of the Weibull distribution with the cumulative Weibull (proportional hazards) distribution with shape the cumulative Weibull (proportional hazards) distribution with shape the probability density function of the Weibull (proportional hazards) distribution with shape a and scale bthe probability density function of the Weibull (proportional hazards)

String functions

```
abbrev(s,n)
                                 name s, abbreviated to a length of n
char(n)
                                 the character corresponding to ASCII or extended ASCII code n; ""
                                    if n is not in the domain
                                 the most closely related locale supported by ICU from loc if type
collatorlocale(loc, type)
                                    is 1; the actual locale where the collation data comes from if
                                    type is 2
collatorversion(loc)
                                 the version string of a collator based on locale loc
                                 the position in ASCII string s_1 of the first character of s_1 not found
indexnot(s_1, s_2)
                                    in ASCII string s_2, or 0 if all characters of s_1 are found in s_2
                                 the plural of s if n \neq \pm 1
plural(n,s)
plural(n,s_1,s_2)
                                 the plural of s_1, as modified by or replaced with s_2, if n \neq \pm 1
real(s)
                                 s converted to numeric or missing
regexcapture(n)
                                 subexpression n from a previous regexm() or regexmatch()
regexcapturenamed(grp)
                                 subexpression corresponding to matching group named grp in reg-
                                    ular expression from a previous regexm() or regexmatch()
                                    match
regexm(s, re)
                                 a match of a regular expression, which evaluates to 1 if regular
                                    expression re is satisfied by the ASCII string s; otherwise, 0
regexmatch(s,re[,noc[,std[,nlalt]]])
                                 a match of a regular expression, which evaluates to 1 if regular
                                    expression re is satisfied by the ASCII string s; otherwise, 0
regexr(s_1, re, s_2)
                                 replaces the first substring within ASCII string s_1 that matches re
                                    with ASCII string s_2 and returns the resulting string
regexreplace(s_1, re, s_2[, noc[, fmt[, std[, nlalt]]])
                                replaces the first substring within ASCII string s_1 that matches re
                                    with ASCII string s_2 and returns the resulting string
regexreplaceall(s_1, re, s_2[, noc[, fmt[, std[, nlalt]]])
                                replaces all substrings within ASCII string s_1 that match re with
                                    ASCII string s_2 and returns the resulting string
regexs(n)
                                 subexpression n from a previous regexm() or regexmatch()
                                    match, where 0 \le n < 10
soundex(s)
                                 the soundex code for a string, s
soundex_nara(s)
                                 the U.S. Census soundex code for a string, s
strcat(s_1, s_2)
                                 there is no strcat() function; instead the addition operator is used
                                    to concatenate strings
strdup(s_1,n)
                                 there is no strdup() function; instead the multiplication operator
                                    is used to create multiple copies of strings
string(n)
                                 a synonym for strofreal(n)
```

```
string(n,s)
                                 a synonym for strofreal(n,s)
stritrim(s)
                                 s with multiple, consecutive internal blanks (ASCII space character
                                    char(32)) collapsed to one blank
strlen(s)
                                 the number of characters in ASCII s or length in bytes
strlower(s)
                                 lowercase ASCII characters in string s
strltrim(s)
                                 s without leading blanks (ASCII space character char (32))
strmatch(s_1, s_2)
                                 1 if s_1 matches the pattern s_2; otherwise, 0
strofreal(n)
                                 n converted to a string
strofreal(n,s)
                                 n converted to a string using the specified display format
                                 the position in s_1 at which s_2 is first found, 0 if s_2 does not occur,
strpos(s_1, s_2)
                                    and 1 if s_2 is empty
strproper(s)
                                 a string with the first ASCII letter and any other letters immediately
                                    following characters that are not letters capitalized; all other
                                    ASCII letters converted to lowercase
strreverse(s)
                                 the reverse of ASCII string s
strrpos(s_1, s_2)
                                 the position in s_1 at which s_2 is last found, 0 if s_2 does not occur,
                                    and 1 if s_2 is empty
strrtrim(s)
                                 s without trailing blanks (ASCII space character char (32))
strtoname(s[,p])
                                 s translated into a Stata 13 compatible name
strtrim(s)
                                 s without leading and trailing blanks (ASCII space character
                                    char(32)); equivalent to strltrim(strrtrim(s))
strupper(s)
                                 uppercase ASCII characters in string s
subinstr(s_1, s_2, s_3, n)
                                 s_1, where the first n occurrences in s_1 of s_2 have been replaced
subinword(s_1, s_2, s_3, n)
                                 s_1, where the first n occurrences in s_1 of s_2 as a word have been
                                    replaced with s_3
substr(s, n_1, n_2)
                                 the substring of s, starting at n_1, for a length of n_2
tobytes(s[,n])
                                 escaped decimal or hex digit strings of up to 200 bytes of s
uchar(n)
                                 the Unicode character corresponding to Unicode code point n or
                                    an empty string if n is beyond the Unicode code-point range
udstrlen(s)
                                 the number of display columns needed to display the Unicode string
                                    s in the Stata Results window
udsubstr(s, n_1, n_2)
                                 the Unicode substring of s, starting at character n_1, for n_2 display
                                    columns
                                 1 if the first Unicode character in s is a Unicode decimal digit;
uisdigit(s)
                                    otherwise, 0
uisletter(s)
                                 1 if the first Unicode character in s is a Unicode letter; otherwise.
ustrcompare (s_1, s_2 \lceil, loc \rceil)
                                 compares two Unicode strings
ustrcompareex(s_1, s_2, loc, st, case, cslv, norm, num, alt, fr)
                                 compares two Unicode strings
ustrfix(s[,rep])
                                 replaces each invalid UTF-8 sequence with a Unicode character
ustrfrom(s,enc,mode)
                                 converts the string s in encoding enc to a UTF-8 encoded Unicode
ustrinvalidcnt(s)
                                 the number of invalid UTF-8 sequences in s
ustrleft(s,n)
                                 the first n Unicode characters of the Unicode string s
```

```
ustrlen(s)
                                the number of characters in the Unicode string s
ustrlower(s[,loc])
                                lowercase all characters of Unicode string s under the given locale
ustrltrim(s)
                                removes the leading Unicode whitespace characters and blanks from
                                   the Unicode string s
ustrnormalize(s, norm)
                                normalizes Unicode string s to one of the five normalization forms
                                    specified by norm
ustrpos(s_1, s_2[, n])
                                the position in s_1 at which s_2 is first found; otherwise, 0
ustrregexm(s, re[, noc])
                                performs a match of a regular expression and evaluates to 1 if regular
                                   expression re is satisfied by the Unicode string s; otherwise, 0
ustrregexra(s_1, re, s_2[, noc]) replaces all substrings within the Unicode string s_1 that match re
                                    with s_2 and returns the resulting string
ustrregexrf (s_1, re, s_2 \mid , noc)) replaces the first substring within the Unicode string s_1 that matches
                                    re with s_2 and returns the resulting string
ustrregexs(n)
                                subexpression n from a previous ustrregexm() match
ustrreverse(s)
                                the reverse of Unicode string s
ustrright(s,n)
                                the last n Unicode characters of the Unicode string s
ustrrpos(s_1, s_2[, n])
                                the position in s_1 at which s_2 is last found; otherwise, 0
ustrrtrim(s)
                                remove trailing Unicode whitespace characters and blanks from the
                                    Unicode string s
ustrsortkey(s[,loc])
                                generates a null-terminated byte array that can be used by the sort
                                   command to produce the same order as ustrcompare()
ustrsortkeyex(s, loc, st, case, cslv, norm, num, alt, fr)
                                generates a null-terminated byte array that can be used by the sort
                                   command to produce the same order as ustrcompare()
ustrtitle(s[,loc])
                                a string with the first characters of Unicode words titlecased and
                                    other characters lowercased
ustrto(s,enc,mode)
                                converts the Unicode string s in UTF-8 encoding to a string in
                                   encoding enc
ustrtohex(s[,n])
                                escaped hex digit string of s up to 200 Unicode characters
ustrtoname(s|,p|)
                                string s translated into a Stata name
ustrtrim(s)
                                removes leading and trailing Unicode whitespace characters and
                                   blanks from the Unicode string s
ustrunescape(s)
                                the Unicode string corresponding to the escaped sequences of s
ustrupper(s[,loc])
                                uppercase all characters in string s under the given locale loc
ustrword(s, n[, loc])
                                the nth Unicode word in the Unicode string s
ustrwordcount(s[,loc])
                                the number of nonempty Unicode words in the Unicode string s
usubinstr(s_1, s_2, s_3, n)
                                replaces the first n occurrences of the Unicode string s_2 with the
                                    Unicode string s_3 in s_1
usubstr(s, n_1, n_2)
                                the Unicode substring of s, starting at n_1, for a length of n_2
                                the nth word in s; missing ("") if n is missing
word(s,n)
```

$\verb wordbreaklocale (loc, type) $	the most closely related locale supported by ICU from loc if $type$ is 1, the actual locale where the word-boundary analysis data come from if $type$ is 2; or an empty string is returned for any
wordcount(s)	other $type$ the number of words in s

Trigonometric functions

acos(x)	the radian value of the arccosine of x
acosh(x)	the inverse hyperbolic cosine of x
asin(x)	the radian value of the arcsine of x
asinh(x)	the inverse hyperbolic sine of x
atan(x)	the radian value of the arctangent of x
atan2(y, x)	the radian value of the arctangent of y/x , where the signs of the parameters y and x are used to determine the quadrant of the answer
atanh(x)	the inverse hyperbolic tangent of x
cos(x)	the cosine of x , where x is in radians
cosh(x)	the hyperbolic cosine of x
sin(x)	the sine of x , where x is in radians
sinh(x)	the hyperbolic sine of x
tan(x)	the tangent of x , where x is in radians
tanh(x)	the hyperbolic tangent of x

Also see

```
[FN] Functions by name
[D] egen — Extensions to generate
[D] generate — Create or change contents of variable
[M-4] Intro — Categorical guide to Mata functions
[U] 13.3 Functions
```

Functions by name

```
abbrev(s,n)
                                  name s, abbreviated to a length of n
abs(x)
                                  the absolute value of x
                                  the radian value of the arccosine of x
acos(x)
acosh(x)
                                  the inverse hyperbolic cosine of x
age(e_{d DOB}, e_d[, s_{nl}])
                                  the age in integer years on e_d for date of birth e_{d \text{ DOB}} with s_{nl} the
                                      nonleap-year birthday for 29feb birthdates
age\_frac(e_{d_{DOB}}, e_d[, s_{nl}])
                                  the age in years, including the fractional part, on e_d for date of birth
                                      e_{d \, \text{DOB}} with s_{nl} the nonleap-year birthday for 29feb birthdates
                                  the radian value of the arcsine of x
asin(x)
asinh(x)
                                  the inverse hyperbolic sine of x
atan(x)
                                  the radian value of the arctangent of x
atan2(y, x)
                                  the radian value of the arctangent of y/x, where the signs of the
                                      parameters y and x are used to determine the quadrant of the
                                      answer
atanh(x)
                                  the inverse hyperbolic tangent of x
autocode (x, n, x_0, x_1)
                                  partitions the interval from x_0 to x_1 into n equal-length intervals
                                      and returns the upper bound of the interval that contains x or
                                      the upper bound of the first or last interval if x < x_0 or x > x_1,
                                     respectively
betaden(a,b,x)
                                  the probability density of the beta distribution, where a and b are
                                      the shape parameters; 0 if x < 0 or x > 1
                                  the probability of observing floor(k) or fewer successes in
binomial(n, k, \theta)
                                      floor(n) trials when the probability of a success on one trial
                                      is \theta; 0 if k < 0; or 1 if k > n
                                  the probability of observing floor(k) successes in floor(n) trials
binomialp(n,k,p)
                                      when the probability of a success on one trial is p
binomialtail(n, k, \theta)
                                  the probability of observing floor(k) or more successes in
                                      floor(n) trials when the probability of a success on one trial
                                      is \theta; 1 if k < 0; or 0 if k > n
binormal(h, k, \rho)
                                  the joint cumulative distribution \Phi(h, k, \rho) of bivariate normal with
                                     correlation \rho
birthday(e_{d \text{ DOB}}, Y[s, s_{nl}])
                                  the e_d date of the birthday in year Y for date of birth e_{d_{DOB}} with
                                      s_{nl} the nonleap-year birthday for 29feb birthdates
bofd("cal",e_d)
                                  the e_b business date corresponding to e_d
byteorder()
                                   1 if your computer stores numbers by using a hilo byte order and
                                     evaluates to 2 if your computer stores numbers by using a lohi
                                      byte order
                                  the value of the system or constant result c (name) (see [P] creturn)
c(name)
_caller()
                                  version of the program or session that invoked the currently running
                                      program; see [P] version
                                  the cumulative Cauchy distribution with location parameter a and
cauchy (a,b,x)
                                      scale parameter b
```

```
cauchyden (a,b,x)
                                  the probability density of the Cauchy distribution with location
                                     parameter a and scale parameter b
                                  the reverse cumulative (upper tail or survivor) Cauchy distribution
cauchytail(a,b,x)
                                     with location parameter a and scale parameter b
Cdhms(e_d,h,m,s)
                                  the e_{tC} datetime (ms. with leap seconds since 01jan1960
                                     00:00:00.000) corresponding to e_d, h, m, s
ceil(x)
                                  the unique integer n such that n-1 < x \le n; x (not ".") if x is
                                     missing, meaning that ceil(.a) = .a
                                  the character corresponding to ASCII or extended ASCII code n; ""
char(n)
                                     if n is not in the domain
                                  the cumulative \chi^2 distribution with d\!f degrees of freedom; 0 if
chi2(df,x)
                                     x < 0
                                  the probability density of the \chi^2 distribution with df degrees of
chi2den(df,x)
                                     freedom; 0 if x < 0
                                  the reverse cumulative (upper tail or survivor) \chi^2 distribution with
chi2tail(df,x)
                                     df degrees of freedom; 1 if x < 0
Chms (h, m, s)
                                  the e_{tC} datetime (ms. with leap seconds since 01jan1960
                                     00:00:00.000) corresponding to h, m, s on 01jan1960
                                  round(x) if abs (x - \text{round}(x)) < \epsilon; otherwise, x; or x if x is
chop(x, \epsilon)
                                     missing
                                  the Cholesky decomposition of the matrix: if R = \text{cholesky}(S),
cholesky(M)
                                     then RR^T = S
clip(x,a,b)
                                  x if a < x < b, b if x \ge b, a if x \le a, or missing if x is missing
                                     or if a > b; x if x is missing
Clock(s_1, s_2[, Y])
                                  the e_{tC} datetime (ms. with leap seconds since 01jan1960
                                     00:00:00.000) corresponding to s_1 based on s_2 and Y
\operatorname{clock}(s_1, s_2[, Y])
                                  the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding
                                     to s_1 based on s_2 and Y
                                  the e_{tC} datetime difference, rounded down to an integer, from
Clockdiff (e_{tC1}, e_{tC2}, s_u)
                                     e_{tC1} to e_{tC2} in s_u units of days, hours, minutes, seconds, or
                                     milliseconds
clockdiff(e_{tc1}, e_{tc2}, s_u)
                                  the e_{tc} datetime difference, rounded down to an integer, from e_{tc1} to
                                     e_{tc2} in s_u units of days, hours, minutes, seconds, or milliseconds
Clockdiff_frac(e_{tC1}, e_{tC2}, s_u)
                                  the e_{tC} datetime difference, including the fractional part, from
                                     e_{tC1} to e_{tC2} in s_u units of days, hours, minutes, seconds, or
                                     milliseconds
clockdiff_frac(e_{tc1}, e_{tc2}, s_u) the e_{tc} datetime difference, including the fractional part, from e_{tc1} to
                                     e_{tc2} in s_u units of days, hours, minutes, seconds, or milliseconds
Clockpart (e_{tC}, s_u)
                                  the integer year, month, day, hour, minute, second, or millisecond
                                     of e_{tC} with s_u specifying which time part
                                  the integer year, month, day, hour, minute, second, or millisecond
clockpart(e_{tc}, s_u)
                                     of e_{tc} with s_u specifying which time part
cloglog(x)
                                  the complementary \log - \log of x
Cmdyhms (M, D, Y, h, m, s)
                                  the e_{tC} datetime (ms. with leap seconds since 01jan1960
                                     00:00:00.000) corresponding to M, D, Y, h, m, s
                                  the e_{tC} datetime (ms. with leap seconds since 01jan1960
Cofc(e_{tc})
                                     00:00:00.000) of e_{tc} (ms. without leap seconds since 01jan1960
```

00:00:00.000)

```
cofC(e_{tC})
                                 the e_{tc} datetime (ms. without leap seconds since 01jan1960
                                    00:00:00.000) of e_{tC} (ms. with leap seconds since 01jan1960
                                    00:00:00.000)
Cofd(e_d)
                                 the e_{tC} datetime (ms. with leap seconds since 01jan1960
                                    00:00:00.000) of date e_d at time 00:00:00.000
                                 the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) of date e_d at
cofd(e_d)
                                    time 00:00:00.000
coleqnumb(M,s)
                                 the equation number of M associated with column equation s;
                                    missing if the column equation cannot be found
collatorlocale(loc, tupe)
                                 the most closely related locale supported by ICU from loc if type
                                    is 1: the actual locale where the collation data comes from if
                                    tupe is 2
collatorversion(loc)
                                 the version string of a collator based on locale loc
colnfreeparms(M)
                                 the number of free parameters in columns of M
colnumb(M,s)
                                 the column number of M associated with column name s; missing
                                    if the column cannot be found
colsof(M)
                                 the number of columns of M
comb(n,k)
                                 the combinatorial function n!/\{k!(n-k)!\}
cond(x,a,b[,c])
                                 a if x is true and nonmissing, b if x is false, and c if x is missing;
                                    a if c is not specified and x evaluates to missing
                                 the correlation matrix of the variance matrix
corr(M)
                                 the cosine of x, where x is in radians
cos(x)
cosh(x)
                                 the hyperbolic cosine of x
daily(s_1, s_2[, Y])
                                 a synonym for date(s_1, s_2[, Y])
date(s_1, s_2[, Y])
                                 the e_d date (days since 01jan1960) corresponding to s_1 based on
                                    s_2 and Y
datediff(e_{d1}, e_{d2}, s_u[, s_{nl}])
                                 the difference, rounded down to an integer, from e_{d1} to e_{d2} in
                                    s_u units of days, months, or years with s_{nl} the nonleap-year
                                    anniversary for e_{d1} on 29feb
\mathtt{datediff\_frac}(e_{d1}, e_{d2}, s_u[\ , s_{nl}\ ])
                                 the difference, including the fractional part, from e_{d1} to e_{d2} in
                                    s_u units of days, months, or years with s_{nl} the nonleap-year
                                    anniversary for e_{d1} on 29feb
datepart(e_d, s_u)
                                 the integer year, month, or day of e_d with s_u specifying year, month,
                                    or day
day(e_d)
                                 the numeric day of the month corresponding to e_d
daysinmonth(e_d)
                                 the number of days in the month of e_d
dayssincedow(e_d,d)
                                 a synonym for dayssinceweekday (e_d, d)
dayssinceweekday(e_d,d)
                                 the number of days until e_d since previous day-of-week d
daysuntildow(e_d,d)
                                 a synonym for daysuntilweekday (e_d, d)
daysuntilweekday(e_d,d)
                                 the number of days from e_d until next day-of-week d
det(M)
                                 the determinant of matrix M
                                 \frac{\partial P(a,x)}{\partial a}, where P(a,x)= gammap(a,x); 0 if x<0
dgammapda(a,x)
                                 \frac{\partial^2 P(a,x)}{\partial a^2}, where P(a,x) = \text{gammap}(a,x); 0 if x < 0
dgammapdada(a,x)
```

```
\frac{\partial^2 P(a,x)}{\partial a \partial x}, where P(a,x) = \text{gammap}(a,x); 0 if x < 0
dgammapdadx(a,x)
                                  \frac{\partial P(a,x)}{\partial x}, where P(a,x)= gammap(a,x); 0 if x<0
dgammapdx(a,x)
                                  \frac{\partial^2 P(a,x)}{\partial x^2}, where P(a,x) = \text{gammap}(a,x); 0 if x < 0
dgammapdxdx(a,x)
                                  the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding
dhms(e_d,h,m,s)
                                     to e_d, h, m, and s
diag(M)
                                  the square, diagonal matrix created from the row or column vector
                                  the number of zeros on the diagonal of M
diag0cnt(M)
digamma(x)
                                  the digamma() function, d \ln \Gamma(x)/dx
dmy(D,M,Y)
                                  the e_d date (days since 01jan1960) corresponding to D, M, Y
dofb(e_b, "cal")
                                  the e_d datetime corresponding to e_b
                                  the e_d date (days since 01jan1960) of datetime e_{tC} (ms. with leap
dofC(e_{tC})
                                     seconds since 01jan1960 00:00:00.000)
dofc(e_{tc})
                                  the e_d date (days since 01jan1960) of datetime e_{tc} (ms. since
                                     01jan1960 00:00:00.000)
dofh(e_h)
                                  the e_d date (days since 01jan1960) of the start of half-year e_h
dofm(e_m)
                                  the e_d date (days since 01jan1960) of the start of month e_m
dofq(e_q)
                                  the e_d date (days since 01jan1960) of the start of quarter e_q
dofw(e_w)
                                  the e_d date (days since 01jan1960) of the start of week e_w
dofy(e_u)
                                  the e_d date (days since 01jan1960) of 01jan in year e_q
dow(e_d)
                                  the numeric day of the week corresponding to date e_d; 0 = \text{Sunday},
                                     1 = Monday, \ldots, 6 = Saturday
dov(e_d)
                                  the numeric day of the year corresponding to date e_d
                                  the cumulative multiple range distribution that is used in Dunnett's
dunnettprob(k, df, x)
                                     multiple-comparison method with k ranges and df degrees of
                                     freedom: 0 if x < 0
e(name)
                                  the value of stored result e(name); see [U] 18.8 Accessing results
                                     calculated by other programs
el(s,i,j)
                                  s[floor(i),floor(j)], the i,j element of the matrix named s;
                                     missing if i or j are out of range or if matrix s does not exist
e(sample)
                                  1 if the observation is in the estimation sample and 0 otherwise
epsdouble()
                                  the machine precision of a double-precision number
                                  the machine precision of a floating-point number
epsfloat()
exp(x)
                                  the exponential function e^x
expm1(x)
                                  e^x - 1 with higher precision than \exp(x) - 1 for small values of
                                     |x|
exponential (b, x)
                                  the cumulative exponential distribution with scale b
                                  the probability density function of the exponential distribution with
exponentialden(b,x)
                                     scale b
exponential tail(b,x)
                                  the reverse cumulative exponential distribution with scale b
                                  the cumulative F distribution with df_1 numerator and df_2 denomina-
F(df_1, df_2, f)
                                     tor degrees of freedom: F(df_1, df_2, f) = \int_0^f Fden(df_1, df_2, t)
                                     dt; 0 if f < 0
Fden (df_1, df_2, f)
                                  the probability density function of the F distribution with df_1 nu-
                                     merator and df_2 denominator degrees of freedom; 0 if f < 0
```

```
1 if the file specified by f exists; otherwise, 0
fileexists(f)
fileread(f)
                                 the contents of the file specified by f
filereaderror(s)
                                 0 or positive integer, said value having the interpretation of a return
filewrite(f,s[,r])
                                 writes the string specified by s to the file specified by f and returns
                                    the number of bytes in the resulting file
                                 the e_d date of the first day of the month of e_d
firstdayofmonth(e_d)
                                 a synonym for firstweekdayofmonth (M, Y, d)
firstdowofmonth(M,Y,d)
firstweekdayofmonth(M,Y,d)
                                 the e_d date of the first day-of-week d in month M of year Y
float(x)
                                 the value of x rounded to float precision
floor(x)
                                 the unique integer n such that n \le x < n+1; x (not ".") if x is
                                    missing, meaning that floor(.a) = .a
                                 the output length of the \%fmt contained in fmtstr; missing if fmtstr
fmtwidth(fmtstr)
                                    does not contain a valid \( \frac{fmt}{} \)
frval()
                                 returns values of variables stored in other frames
_frval()
                                 programmer's version of frval()
Ftail(df_1, df_2, f)
                                 the reverse cumulative (upper tail or survivor) F distribution with
                                    df_1 numerator and df_2 denominator degrees of freedom; 1 if
                                    f < 0
                                 the probability density function of the gamma distribution; 0 if
gammaden(a,b,g,x)
                                    x < g
gammap(a,x)
                                 the cumulative gamma distribution with shape parameter a; 0 if
                                    x < 0
                                 the reverse cumulative (upper tail or survivor) gamma distribution
gammaptail(a,x)
                                    with shape parameter a; 1 if x < 0
get(systemname)
                                 a copy of Stata internal system matrix systemname
                                 a matrix whose i,\ j element is M[i,j]\cdot N[i,j] (if M and N are
hadamard(M,N)
                                    not the same size, this function reports a conformability error)
halfyear(e_d)
                                 the numeric half of the year corresponding to date e_d
halfyearly(s_1, s_2[,Y])
                                 the e_h half-yearly date (half-years since 1960h1) corresponding to
                                    s_1 based on s_2 and Y; Y specifies topyear; see date()
                                 1 if name appears as a word in e(properties); otherwise, 0
has_eprop(name)
hh(e_{tc})
                                 the hour corresponding to datetime e_{tc} (ms. since 01jan1960
                                    00:00:00.000)
hhC(e_{tC})
                                 the hour corresponding to datetime e_{tC} (ms. with leap seconds since
                                    01jan1960 00:00:00.000)
hms(h,m,s)
                                 the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding
                                    to h, m, s on 01jan1960
                                 the e_h half-yearly date (half years since 1960h1) containing date e_d
hofd(e_d)
                                 ms/3,600,000
hours(ms)
hypergeometric (N, K, n, k) the cumulative probability of the hypergeometric distribution
hypergeometric p(N, K, n, k) the hypergeometric probability of k successes out of a sample of
                                    size n, from a population of size N containing K elements that
                                    have the attribute of interest
I(n)
                                 an n \times n identity matrix if n is an integer; otherwise, a round (n) \times n
                                    round(n) identity matrix
```

```
the cumulative beta distribution with shape parameters a and b; 0
ibeta(a,b,x)
                                   if x < 0: or 1 if x > 1
ibetatail(a,b,x)
                                the reverse cumulative (upper tail or survivor) beta distribution with
                                   shape parameters a and b; 1 if x < 0; or 0 if x > 1
                                the cumulative inverse Gaussian distribution with mean m and shape
igaussian(m,a,x)
                                   parameter a; 0 if x \leq 0
igaussianden(m,a,x)
                                the probability density of the inverse Gaussian distribution with
                                   mean m and shape parameter a; 0 if x \le 0
                                the reverse cumulative (upper tail or survivor) inverse Gaussian
igaussiantail(m,a,x)
                                   distribution with mean m and shape parameter a; 1 if x \le 0
                                the position in ASCII string s_1 of the first character of s_1 not found
indexnot(s_1, s_2)
                                   in ASCII string s_2, or 0 if all characters of s_1 are found in s_2
                                1 if z is a member of the remaining arguments; otherwise, 0
inlist(z,a,b,...)
inrange(z,a,b)
                                1 if it is known that a \le z \le b; otherwise, 0
int(x)
                                the integer obtained by truncating x toward 0 (thus, int(5.2) = 5
                                   and int(-5.8) = -5); x (not ".") if x is missing, meaning
                                   that int(.a) = .a
                                the inverse of the matrix M
inv(M)
invbinomial(n, k, p)
                                the inverse of the cumulative binomial; that is, \theta (\theta = probability
                                   of success on one trial) such that the probability of observing
                                   floor(k) or fewer successes in floor(n) trials is p
                                the inverse of the right cumulative binomial; that is, \theta (\theta = probabil-
invbinomialtail (n, k, p)
                                   ity of success on one trial) such that the probability of observing
                                   floor(k) or more successes in floor(n) trials is p
                                the inverse of cauchy(): if cauchy(a,b,x) = p, then
inveauchy (a,b,p)
                                   invcauchy(a,b,p) = x
                                the inverse of cauchytail(): if cauchytail(a,b,x) = p, then
invcauchytail (a,b,p)
                                   invcauchytail(a,b,p) = x
invchi2(df,p)
                                the inverse of chi2(): if chi2(df, x) = p, then invchi2(df, p) =
                                the inverse of chi2tail(): if chi2tail(df, x) = p, then
invchi2tail(df, p)
                                   invchi2tail(df,p) = x
                                the inverse of the complementary log-log function of x
invcloglog(x)
                                the inverse cumulative multiple range distribution that is used in
invdunnettprob(k, df, p)
                                   Dunnett's multiple-comparison method with k ranges and df
                                   degrees of freedom
invexponential(b, p)
                                the inverse cumulative exponential distribution with scale b: if
                                   exponential(b,x) = p, then invexponential(b,p) = x
                                the inverse reverse cumulative exponential distribution with scale b:
invexponential tail(b, p)
                                   if exponentialtail(b, x) = p, then
                                   invexponentialtail(b, p) = x
invF(df_1, df_2, p)
                                the inverse cumulative F distribution: if F(df_1, df_2, f) = p, then
                                   invF(df_1, df_2, p) = f
invFtail(df_1, df_2, p)
                                the inverse reverse cumulative (upper tail or survivor) F distribution:
                                   if Ftail(df_1, df_2, f) = p, then invFtail(df_1, df_2, p) = f
                                the inverse cumulative gamma distribution: if gammap(a, x) = p,
invgammap(a, p)
                                   then invgammap(a, p) = x
```

```
the inverse reverse cumulative (upper tail or survivor) gamma distri-
invgammaptail(a, p)
                                 bution: if gammaptail(a, x) = p, then invgammaptail(a, p)
                               the inverse cumulative beta distribution: if ibeta(a,b,x) = p,
invibeta(a,b,p)
                                  then invibeta(a,b,p)=x
invibetatail(a,b,p)
                               the inverse reverse cumulative (upper tail or survivor) beta distribu-
                                 tion: if ibetatail(a,b,x) = p, then invibetatail(a,b,p)
invigaussian(m,a,p)
                               the inverse of igaussian(): if
                                  igaussian(m,a,x) = p, then invigaussian(m,a,p) = x
                               the inverse of igaussiantail(): if
invigaussiantail(m, a, p)
                                  igaussiantail(m,a,x)=p, then
                                  invigaussiantail(m, a, p) = x
                               the inverse of laplace(): if laplace(m,b,x) = p, then
invlaplace(m,b,p)
                                  invlaplace(m,b,p) = x
                               the inverse of laplacetail(): if laplacetail(m, b, x) = p,
invlaplacetail(m,b,p)
                                  then invlaplacetail(m, b, p) = x
invlogistic(p)
                               the inverse cumulative logistic distribution: if logistic(x) = p,
                                  then invlogistic(p) = x
invlogistic(s,p)
                               the inverse cumulative logistic distribution: if logistic(s, x) = p,
                                  then invlogistic(s, p) = x
invlogistic(m, s, p)
                               the inverse cumulative logistic distribution: if logistic(m,s,x)
                                  = p, then invlogistic(m, s, p) = x
                               the inverse reverse cumulative logistic distribution: if
invlogistictail(p)
                                  logistictail(x) = p, then invlogistictail(p) = x
invlogistictail(s,p)
                               the inverse cumulative logistic distribution: if logistic(s, x) = p,
                                  then invlogistic(s,p) = x
invlogistictail(m, s, p)
                               the inverse cumulative logistic distribution: if logistic(m, s, x)
                                  = p, then invlogistic(m, s, p) = x
invlogit(x)
                               the inverse of the logit function of x
                               the value of the negative binomial parameter, p, such that q =
invnbinomial (n, k, q)
                                 nbinomial(n,k,p)
invnbinomialtail(n, k, q)
                               the value of the negative binomial parameter, p, such that
                                  q = nbinomialtail(n, k, p)
                               the inverse cumulative noncentral \chi^2 distribution: if
invnchi2(df, np, p)
                                 nchi2(df, np, x) = p, then invnchi2(df, np, p) = x
                               the inverse reverse cumulative (upper tail or survivor) non-
invnchi2tail(df, np, p)
                                 central \chi^2 distribution: if nchi2tail(df, np, x) = p, then
                                  invnchi2tail(df, np, p) = x
invnF(df_1, df_2, np, p)
                               the inverse cumulative noncentral F distribution: if
                                 nF(df_1, df_2, np, f) = p, then invnF(df_1, df_2, np, p) = f
invnFtail(df_1, df_2, np, p)
                               the inverse reverse cumulative (upper tail or survivor) noncen-
                                  tral F distribution: if nFtail(df_1, df_2, np, f) = p, then
                                  invnFtail(df_1, df_2, np, p) = f
                               the inverse cumulative noncentral beta distribution: if
invnibeta(a,b,np,p)
                                 nibeta(a,b,np,x) = p, then invibeta(a,b,np,p) = x
                               the inverse cumulative standard normal distribution: if normal(z)
invnormal(p)
                                  = p, then invnormal(p) = z
```

```
invnt(df, np, p)
                               the inverse cumulative noncentral Student's t distribution; if
                                  \operatorname{nt}(df, np, t) = p, then \operatorname{invnt}(df, np, p) = t
                               the inverse reverse cumulative (upper tail or survivor) noncen-
invnttail(df, np, p)
                                   tral Student's t distribution: if nttail(df, np, t) = p, then
                                   invnttail(df, np, p) = t
                               the Poisson mean such that the cumulative Poisson distribution eval-
invpoisson(k, p)
                                   uated at k is p: if poisson(m,k) = p, then invpoisson(k,p)
                                   = m
                               the Poisson mean such that the reverse cumulative Poisson distri-
invpoissontail (k,q)
                                   bution evaluated at k is q: if poissontail (m,k) = q, then
                                   invpoissontail(k,q) = m
                               the inverse of M if M is positive definite
invsym(M)
invt(df, p)
                               the inverse cumulative Student's t distribution: if t(df,t) = p,
                                  then invt(df, p) = t
                               the inverse reverse cumulative (upper tail or survivor) Student's
invttail(df, p)
                                  t distribution: if ttail(df,t) = p, then invttail(df,p) = t
                               the inverse cumulative Tukey's Studentized range distribution with
invtukeyprob(k, df, p)
                                   k ranges and df degrees of freedom
                               a symmetric matrix formed by filling in the columns of the lower
invvech(M)
                                  triangle from a row or column vector
                               a symmetric matrix formed by filling in the columns of the upper
invvecp(M)
                                  triangle from a row or column vector
invweibull(a,b,p)
                               the inverse cumulative Weibull distribution with shape a and scale
                                   b: if weibull(a,b,x) = p, then invweibull(a,b,p) = x
                               the inverse cumulative Weibull distribution with shape a, scale b,
invweibull(a,b,g,p)
                                   and location g: if weibull (a,b,g,x) = p, then
                                   invweibull(a,b,g,p) = x
                               the inverse cumulative Weibull (proportional hazards) distribution
invweibullph(a,b,p)
                                   with shape a and scale b: if weibullph(a,b,x) = p, then
                                   invweibullph(a,b,p) = x
                               the inverse cumulative Weibull (proportional hazards) distribution
invweibullph(a,b,q,p)
                                   with shape a, scale b, and location q: if weibullph (a, b, q, x) =
                                  p, then invweibullph(a,b,q,p) = x
                               the inverse reverse cumulative Weibull (proportional hazards) distri-
invweibullphtail(a, b, p)
                                   bution with shape a and scale b: if weibullphtail (a,b,x)=p,
                                  then invweibullphtail(a,b,p) = x
invweibullphtail(a,b,g,p)
                               the inverse reverse cumulative Weibull (proportional hazards)
                                  distribution with shape a, scale b, and location g: if
                                   weibullphtail(a, b, g, x) = p, then
                                   invweibullphtail(a,b,g,p) = x
                               the inverse reverse cumulative Weibull distribution with shape a and
invweibulltail(a, b, p)
                                   scale b: if weibulltail(a,b,x) = p, then
                                   invweibulltail(a,b,p) = x
invweibulltail(a, b, g, p)
                               the inverse reverse cumulative Weibull distribution with shape a,
                                   scale b, and location g: if weibulltail(a,b,g,x) = p, then
                                   invweibulltail(a,b,q,p) = x
irecode(x, x_1, \ldots, x_n)
                               missing if x is missing or x_1, \ldots, x_n is not weakly increasing; 0
                                  if x \le x_1; 1 if x_1 < x \le x_2; 2 if x_2 < x \le x_3; ...; n if
                                  x > x_n
```

```
1 if e_{tC} is a leap second; otherwise, 0
isleapsecond(e_{tC})
isleapyear(Y)
                                1 if Y is a leap year; otherwise, 0
issymmetric(M)
                                1 if the matrix is symmetric; otherwise, 0
J(r,c,z)
                                the r \times c matrix containing elements z
laplace(m,b,x)
                                the cumulative Laplace distribution with mean m and scale param-
                                   eter b
                                the probability density of the Laplace distribution with mean m and
laplaceden(m,b,x)
                                   scale parameter b
laplacetail(m,b,x)
                                the reverse cumulative (upper tail or survivor) Laplace distribution
                                   with mean m and scale parameter b
lastdayofmonth(e_d)
                                the e_d date of the last day of the month of e_d
lastdowofmonth(M, Y, d)
                                a synonym for lastweekdayofmonth (M, Y, d)
lastweekdayofmonth(M, Y, d)
                                the e_d date of the last day-of-week d in month M of year Y
ln(x)
                                the natural logarithm, ln(x)
                                the natural logarithm of 1-x with higher precision than ln(1-x)
ln1m(x)
                                   for small values of |x|
ln1p(x)
                                the natural logarithm of 1+x with higher precision than ln(1+x)
                                   for small values of |x|
                                the natural logarithm of the density of the Cauchy distribution with
lncauchyden(a,b,x)
                                   location parameter a and scale parameter b
lnfactorial(n)
                                the natural log of n factorial = ln(n!)
                                ln\{\Gamma(x)\}
lngamma(x)
lnigammaden(a,b,x)
                                the natural logarithm of the inverse gamma density, where a is the
                                   shape parameter and b is the scale parameter
lnigaussianden(m,a,x)
                                the natural logarithm of the inverse Gaussian density with mean m
                                   and shape parameter a
lniwishartden(df, V, X)
                                the natural logarithm of the density of the inverse Wishart distribu-
                                   tion; missing if df < n-1
lnlaplaceden(m,b,x)
                                the natural logarithm of the density of the Laplace distribution with
                                   mean m and scale parameter b
lnmvnormalden(M, V, X)
                                the natural logarithm of the multivariate normal density
lnnormal(z)
                                the natural logarithm of the cumulative standard normal distribution
lnnormalden(z)
                                the natural logarithm of the standard normal density, N(0,1)
lnnormalden(x, \sigma)
                                the natural logarithm of the normal density with mean 0 and standard
                                   deviation \sigma
                                the natural logarithm of the normal density with mean \mu and standard
lnnormalden(x, \mu, \sigma)
                                   deviation \sigma, N(\mu, \sigma^2)
                                the natural logarithm of the density of the Wishart distribution;
lnwishartden(df, V, X)
                                   missing if df \leq n-1
                                a synonym for ln(x)
log(x)
log10(x)
                                the base-10 logarithm of x
log1m(x)
                                a synonym for ln1m(x)
                                a synonym for ln1p(x)
log1p(x)
```

```
logistic(x)
                                  the cumulative logistic distribution with mean 0 and standard devi-
                                     ation \pi/\sqrt{3}
logistic(s,x)
                                  the cumulative logistic distribution with mean 0, scale s, and standard
                                     deviation s\pi/\sqrt{3}
logistic(m,s,x)
                                 the cumulative logistic distribution with mean m, scale s, and
                                     standard deviation s\pi/\sqrt{3}
logisticden(x)
                                  the density of the logistic distribution with mean 0 and standard
                                     deviation \pi/\sqrt{3}
logisticden(s,x)
                                  the density of the logistic distribution with mean 0, scale s, and
                                     standard deviation s\pi/\sqrt{3}
logisticden(m,s,x)
                                  the density of the logistic distribution with mean m, scale s, and
                                     standard deviation s\pi/\sqrt{3}
logistictail(x)
                                  the reverse cumulative logistic distribution with mean 0 and standard
                                     deviation \pi/\sqrt{3}
                                  the reverse cumulative logistic distribution with mean 0, scale s,
logistictail(s,x)
                                     and standard deviation s\pi/\sqrt{3}
logistictail(m,s,x)
                                  the reverse cumulative logistic distribution with mean m, scale s,
                                     and standard deviation s\pi/\sqrt{3}
logit(x)
                                  the log of the odds ratio of x, logit(x) = \ln \{x/(1-x)\}\
matmissing(M)
                                  1 if any elements of the matrix are missing; otherwise, 0
matrix(exp)
                                  restricts name interpretation to scalars and matrices; see scalar()
matuniform(r,c)
                                  the r \times c matrices containing uniformly distributed pseudorandom
                                     numbers on the interval (0, 1)
\max(x_1, x_2, \ldots, x_n)
                                  the maximum value of x_1, x_2, \ldots, x_n
maxbyte()
                                  the largest value that can be stored in storage type byte
maxdouble()
                                  the largest value that can be stored in storage type double
maxfloat()
                                  the largest value that can be stored in storage type float
maxint()
                                  the largest value that can be stored in storage type int
maxlong()
                                  the largest value that can be stored in storage type long
mdy(M,D,Y)
                                  the e_d date (days since 01jan1960) corresponding to M, D, Y
mdyhms(M, D, Y, h, m, s)
                                  the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding
                                     to M, D, Y, h, m, s
mi(x_1, x_2, \ldots, x_n)
                                  a synonym for missing (x_1, x_2, \ldots, x_n)
\min(x_1, x_2, \ldots, x_n)
                                  the minimum value of x_1, x_2, \ldots, x_n
minbyte()
                                  the smallest value that can be stored in storage type byte
mindouble()
                                  the smallest value that can be stored in storage type double
minfloat()
                                  the smallest value that can be stored in storage type float
minint()
                                  the smallest value that can be stored in storage type int
minlong()
                                  the smallest value that can be stored in storage type long
                                  ms/60,000
minutes(ms)
missing(x_1, x_2, \ldots, x_n)
                                  1 if any x_i evaluates to missing; otherwise, 0
mm(e_{tc})
                                  the minute corresponding to datetime e_{tc} (ms. since 01jan1960
                                     00:00:00.000)
```

```
mmC(e_{tC})
                                  the minute corresponding to datetime e_{tC} (ms. with leap seconds
                                     since 01jan1960 00:00:00.000)
                                  the modulus of x with respect to y
mod(x,y)
mofd(e_d)
                                  the e_m monthly date (months since 1960m1) containing date e_d
month(e_d)
                                  the numeric month corresponding to date e_d
monthly(s_1, s_2[, Y])
                                  the e_m monthly date (months since 1960m1) corresponding to s_1
                                     based on s_2 and Y; Y specifies topyear; see date()
mreldif(X,Y)
                                  the relative difference of X and Y, where the relative difference is
                                     defined as \max_{i,j} \{ |x_{ij} - y_{ij}|/(|y_{ij}| + 1) \}
msofhours(h)
                                  h \times 3,600,000
msofminutes(m)
                                  m \times 60,000
msofseconds(s)
                                  s \times 1,000
nbetaden(a,b,np,x)
                                  the probability density function of the noncentral beta distribution;
                                     0 if x < 0 or x > 1
nbinomial(n,k,p)
                                  the cumulative probability of the negative binomial distribution
nbinomialp(n,k,p)
                                  the negative binomial probability
                                  the reverse cumulative probability of the negative binomial distri-
nbinomialtail(n,k,p)
                                  the cumulative noncentral \chi^2 distribution; 0 if x < 0
nchi2(df, np, x)
                                  the probability density of the noncentral \chi^2 distribution; 0 if x < 0
nchi2den(df, np, x)
                                  the reverse cumulative (upper tail or survivor) noncentral \chi^2 distri-
nchi2tail(df, np, x)
                                     bution; 1 if x < 0
nextbirthday(e_{d\,	ext{DOB}},e_{d}[,s_{nl}])
                                  the e_d date of the first birthday after e_d for date of birth e_{d \text{ DOB}}
                                     with s_{nl} the nonleap-year birthday for 29feb birthdates
                                  a synonym for nextweekday (e_d, d)
nextdow(e_d,d)
nextleapyear(Y)
                                  the first leap year after year Y
nextweekday(e_d,d)
                                  the e_d date of the first day-of-week d after e_d
nF(df_1, df_2, np, f)
                                  the cumulative noncentral F distribution with df_1 numerator and
                                     df_2 denominator degrees of freedom and noncentrality parameter
                                     np; 0 if f < 0
nFden(df_1, df_2, np, f)
                                  the probability density function of the noncentral F distribution
                                     with df_1 numerator and df_2 denominator degrees of freedom and
                                     noncentrality parameter np; 0 if f < 0
nFtail(df_1, df_2, np, f)
                                  the reverse cumulative (upper tail or survivor) noncentral F dis-
                                     tribution with df_1 numerator and df_2 denominator degrees of
                                     freedom and noncentrality parameter np; 1 if f < 0
nibeta(a,b,np,x)
                                  the cumulative noncentral beta distribution; 0 if x < 0; or 1 if
                                     x > 1
normal(z)
                                  the cumulative standard normal distribution
normalden(z)
                                  the standard normal density, N(0,1)
normalden(x, \sigma)
                                  the normal density with mean 0 and standard deviation \sigma
                                  the normal density with mean \mu and standard deviation \sigma, N(\mu, \sigma^2)
normalden(x, \mu, \sigma)
now()
                                  the current e_{tc} datetime
```

```
the noncentrality parameter, np, for noncentral \chi^2: if
npnchi2(df, x, p)
                                     nchi2(df, np, x) = p, then npnchi2(df, x, p) = np
npnF(df_1, df_2, f, p)
                                  the noncentrality parameter, np, for the noncentral F: if
                                     nF(df_1, df_2, np, f) = p, then npnF(df_1, df_2, f, p) = np
                                  the noncentrality parameter, np, for the noncentral Student's
npnt(df,t,p)
                                     t distribution: if nt(df, np, t) = p, then npnt(df, t, p) = np
nt(df, np, t)
                                  the cumulative noncentral Student's t distribution with df degrees
                                     of freedom and noncentrality parameter np
ntden(df, np, t)
                                  the probability density function of the noncentral Student's
                                     t distribution with df degrees of freedom and noncentrality pa-
                                     rameter np
nttail(df, np, t)
                                  the reverse cumulative (upper tail or survivor) noncentral Student's
                                     t distribution with df degrees of freedom and noncentrality pa-
                                     rameter np
nullmat(matname)
                                  use with the row-join (,) and column-join (\) operators
plural(n,s)
                                  the plural of s if n \neq \pm 1
plural(n, s_1, s_2)
                                  the plural of s_1, as modified by or replaced with s_2, if n \neq \pm 1
                                  the probability of observing floor(k) or fewer outcomes that are
poisson(m,k)
                                     distributed as Poisson with mean m
                                  the probability of observing floor (k) outcomes that are distributed
poissonp(m,k)
                                     as Poisson with mean m
                                  the probability of observing floor(k) or more outcomes that are
poissontail(m,k)
                                     distributed as Poisson with mean m
previousbirthday(e_{d \text{ DOB}}, e_d | ,s_{nl} |)
                                  the \vec{e_d} date of the birthday immediately before e_d for date of birth
                                     e_{d\,\mathrm{DOB}} with s_{nl} the nonleap-year birthday for 29feb birthdates
previousdow(e_d, d)
                                  a synonym for previousweekday (e_d, d)
previousleapyear(Y)
                                  the leap year immediately before year Y
previousweekday(e_d, d)
                                  the e_d date of the last day-of-week d before e_d
                                  the e_q quarterly date (quarters since 1960q1) containing date e_d
qofd(e_d)
quarter(e_d)
                                  the numeric quarter of the year corresponding to date e_d
quarterly(s_1, s_2[, Y])
                                 the e_q quarterly date (quarters since 1960q1) corresponding to s_1
                                     based on s_2 and Y; Y specifies topyear, see date()
r(name)
                                  the value of the stored result r(name); see [U] 18.8 Accessing
                                     results calculated by other programs
                                  beta(a,b) random variates, where a and b are the beta distribution
rbeta(a,b)
                                     shape parameters
rbinomial(n,p)
                                  binomial(n,p) random variates, where n is the number of trials and
                                     p is the success probability
                                 Cauchy(a,b) random variates, where a is the location parameter and
reauchy(a,b)
                                     b is the scale parameter
                                 \chi^2, with df degrees of freedom, random variates
rchi2(df)
recode(x, x_1, \ldots, x_n)
                                  missing if x_1, x_2, \ldots, x_n is not weakly increasing; x if x is missing;
                                     x_1 if x \le x_1; x_2 if x \le x_2, ...; otherwise, x_n if x > x_1, x_2,
                                     \dots, x_{n-1}. x_i \ge . is interpreted as x_i = +\infty
real(s)
                                  s converted to numeric or missing
```

```
regexcapture(n)
                                subexpression n from a previous regexm() or regexmatch()
                                   match
regexcapturenamed(qrp)
                                subexpression corresponding to matching group named grp in reg-
                                   ular expression from a previous regexm() or regexmatch()
                                   match
regexm(s, re)
                                a match of a regular expression, which evaluates to 1 if regular
                                   expression re is satisfied by the ASCII string s; otherwise, 0
regexmatch(s,re[,noc[,std[,nlalt]]])
                                a match of a regular expression, which evaluates to 1 if regular
                                   expression re is satisfied by the ASCII string s; otherwise, 0
regexr(s_1, re, s_2)
                                replaces the first substring within ASCII string s_1 that matches re
                                   with ASCII string s_2 and returns the resulting string
regexreplace(s_1, re, s_2[, noc[, fmt[, std[, nlalt]]])
                                replaces the first substring within ASCII string s_1 that matches re
                                   with ASCII string s_2 and returns the resulting string
regexreplaceall(s_1, re, s_2[, noc[, fmt[, std[, nlalt]]])
                                replaces all substrings within ASCII string s_1 that match re with
                                   ASCII string s_2 and returns the resulting string
                                subexpression n from a previous regexm() or regexmatch()
regexs(n)
                                   match, where 0 \le n < 10
                                the "relative" difference |x-y|/(|y|+1); 0 if both arguments are
reldif(x,y)
                                   the same type of extended missing value; missing if only one
                                   argument is missing or if the two arguments are two different
                                   types of missing
                                1 if the first nonblank character of local macro '0' is a comma, or
replay()
                                   if '0' is empty
return(name)
                                the value of the to-be-stored result r(name); see [P] return
rexponential(b)
                                exponential random variates with scale b
rgamma(a,b)
                                gamma(a,b) random variates, where a is the gamma shape parameter
                                   and b is the scale parameter
rhypergeometric (N, K, n)
                                hypergeometric random variates
rigaussian(m,a)
                                inverse Gaussian random variates with mean m and shape param-
                                   eter a
rlaplace(m,b)
                                Laplace(m,b) random variates with mean m and scale parameter b
                                logistic variates with mean 0 and standard deviation \pi/\sqrt{3}
rlogistic()
rlogistic(s)
                                logistic variates with mean 0, scale s, and standard deviation s\pi/\sqrt{3}
rlogistic(m,s)
                                logistic variates with mean m, scale s, and standard deviation
                                   s\pi/\sqrt{3}
                                negative binomial random variates
rnbinomial(n, p)
                                standard normal (Gaussian) random variates, that is, variates from
rnormal()
                                   a normal distribution with a mean of 0 and a standard deviation
                                   of 1
rnormal(m)
                                normal(m,1) (Gaussian) random variates, where m is the mean and
                                   the standard deviation is 1
rnormal(m,s)
                                normal(m,s) (Gaussian) random variates, where m is the mean and
                                   s is the standard deviation
```

```
round(x,y) or round(x)
                                x rounded in units of y or x rounded to the nearest integer if the
                                   argument y is omitted; x (not ".") if x is missing (meaning
                                   that round(.a) = .a and that round(.a, y) = .a if y is not
                                   missing) and if y is missing, then "." is returned
                                the equation number of M associated with row equation s; missing
rowegnumb (M,s)
                                   if the row equation cannot be found
rownfreeparms(M)
                                the number of free parameters in rows of M
rownumb(M,s)
                                the row number of M associated with row name s; missing if the
                                   row cannot be found
rowsof(M)
                                the number of rows of M
                                Poisson(m) random variates, where m is the distribution mean
rpoisson(m)
rt(df)
                                Student's t random variates, where df is the degrees of freedom
runiform()
                                uniformly distributed random variates over the interval (0,1)
runiform(a,b)
                                uniformly distributed random variates over the interval (a,b)
runiformint (a,b)
                                uniformly distributed random integer variates on the interval [a, b]
rweibull(a,b)
                                Weibull variates with shape a and scale b
                                Weibull variates with shape a, scale b, and location q
rweibull(a,b,q)
rweibullph(a,b)
                                Weibull (proportional hazards) variates with shape a and scale b
rweibullph(a,b,g)
                                Weibull (proportional hazards) variates with shape a, scale b, and
                                   location q
s(name)
                                the value of stored result s(name); see [U] 18.8 Accessing results
                                   calculated by other programs
scalar(exp)
                                restricts name interpretation to scalars and matrices
seconds(ms)
                                ms/1.000
                                the sign of x: -1 if x < 0, 0 if x = 0, 1 if x > 0, or missing if
sign(x)
                                   x is missing
sin(x)
                                the sine of x, where x is in radians
sinh(x)
                                the hyperbolic sine of x
smallestdouble()
                                the smallest double-precision number greater than zero
soundex(s)
                                the soundex code for a string, s
soundex_nara(s)
                                the U.S. Census soundex code for a string, s
sqrt(x)
                                the square root of x
ss(e_{tc})
                                the second corresponding to datetime e_{tc} (ms. since 01jan1960
                                   00:00:00.000)
ssC(e_{tC})
                                the second corresponding to datetime e_{tC} (ms. with leap seconds
                                   since 01jan1960 00:00:00.000)
                                there is no strcat() function; instead the addition operator is used
strcat(s_1, s_2)
                                   to concatenate strings
strdup(s_1, n)
                                there is no strdup() function; instead the multiplication operator
                                   is used to create multiple copies of strings
string(n)
                                a synonym for strofreal(n)
string(n,s)
                                a synonym for strofreal(n,s)
stritrim(s)
                                s with multiple, consecutive internal blanks (ASCII space character
                                   char(32)) collapsed to one blank
strlen(s)
                                the number of characters in ASCII s or length in bytes
```

```
strlower(s)
                                 lowercase ASCII characters in string s
strltrim(s)
                                 s without leading blanks (ASCII space character char(32))
strmatch(s_1, s_2)
                                 1 if s_1 matches the pattern s_2; otherwise, 0
strofreal(n)
                                 n converted to a string
strofreal(n,s)
                                 n converted to a string using the specified display format
strpos(s_1, s_2)
                                 the position in s_1 at which s_2 is first found, 0 if s_2 does not occur,
                                    and 1 if s_2 is empty
                                 a string with the first ASCII letter and any other letters immediately
strproper(s)
                                    following characters that are not letters capitalized; all other
                                    ASCII letters converted to lowercase
strreverse(s)
                                 the reverse of ASCII string s
strrpos(s_1, s_2)
                                 the position in s_1 at which s_2 is last found, 0 if s_2 does not occur,
                                    and 1 if s_2 is empty
strrtrim(s)
                                 s without trailing blanks (ASCII space character char (32))
strtoname(s[,p])
                                 s translated into a Stata 13 compatible name
strtrim(s)
                                 s without leading and trailing blanks (ASCII space character
                                    char(32)); equivalent to strltrim(strrtrim(s))
strupper(s)
                                 uppercase ASCII characters in string s
subinstr(s_1, s_2, s_3, n)
                                 s_1, where the first n occurrences in s_1 of s_2 have been replaced
subinword(s_1, s_2, s_3, n)
                                 s_1, where the first n occurrences in s_1 of s_2 as a word have been
                                    replaced with s_3
                                 the substring of s, starting at n_1, for a length of n_2
substr(s, n_1, n_2)
sum(x)
                                 the running sum of x, treating missing values as zero
sweep(M,i)
                                 matrix M with ith row/column swept
t(df,t)
                                 the cumulative Student's t distribution with df degrees of freedom
tan(x)
                                 the tangent of x, where x is in radians
tanh(x)
                                 the hyperbolic tangent of x
tC(l)
                                 convenience function to make typing dates and times in expressions
                                    easier
tc(l)
                                 convenience function to make typing dates and times in expressions
td(l)
                                 convenience function to make typing dates in expressions easier
tden(df,t)
                                 the probability density function of Student's t distribution
th(l)
                                 convenience function to make typing half-yearly dates in expressions
                                    easier
tin(d_1,d_2)
                                 true if d_1 \leq t \leq d_2, where t is the time variable previously tsset
t.m(l)
                                 convenience function to make typing monthly dates in expressions
tobytes(s[,n])
                                 escaped decimal or hex digit strings of up to 200 bytes of s
today()
                                 today's e_d date
tq(l)
                                 convenience function to make typing quarterly dates in expressions
                                    easier
                                 the trace of matrix M
trace(M)
                                 the second derivative of lngamma(x) = d^2 \ln \Gamma(x)/dx^2
trigamma(x)
```

```
trunc(x)
                                 a synonym for int(x)
                                 the reverse cumulative (upper tail or survivor) Student's t distribution;
ttail(df,t)
                                    the probability T>t
tukeyprob(k, df, x)
                                 the cumulative Tukey's Studentized range distribution with k ranges
                                    and df degrees of freedom; 0 if x < 0
tw(l)
                                 convenience function to make typing weekly dates in expressions
twithin (d_1, d_2)
                                 true if d_1 < t < d_2, where t is the time variable previously tsset
uchar(n)
                                 the Unicode character corresponding to Unicode code point n or
                                    an empty string if n is beyond the Unicode code-point range
udstrlen(s)
                                 the number of display columns needed to display the Unicode string
                                    s in the Stata Results window
udsubstr(s, n_1, n_2)
                                 the Unicode substring of s, starting at character n_1, for n_2 display
                                 1 if the first Unicode character in s is a Unicode decimal digit;
uisdigit(s)
                                    otherwise, 0
uisletter(s)
                                 1 if the first Unicode character in s is a Unicode letter; otherwise.
ustrcompare(s_1, s_2[, loc])
                                 compares two Unicode strings
ustrcompareex(s_1, s_2, loc, st, case, cslv, norm, num, alt, fr)
                                 compares two Unicode strings
ustrfix(s[,rep])
                                 replaces each invalid UTF-8 sequence with a Unicode character
ustrfrom(s,enc,mode)
                                 converts the string s in encoding enc to a UTF-8 encoded Unicode
                                    string
ustrinvalidcnt(s)
                                 the number of invalid UTF-8 sequences in s
ustrleft(s,n)
                                 the first n Unicode characters of the Unicode string s
ustrlen(s)
                                 the number of characters in the Unicode string s
ustrlower(s[,loc])
                                 lowercase all characters of Unicode string s under the given locale
ustrltrim(s)
                                 removes the leading Unicode whitespace characters and blanks from
                                    the Unicode string s
ustrnormalize(s, norm)
                                 normalizes Unicode string s to one of the five normalization forms
                                    specified by norm
ustrpos(s_1, s_2[, n])
                                 the position in s_1 at which s_2 is first found; otherwise, 0
ustrregexm(s, re[, noc])
                                 performs a match of a regular expression and evaluates to 1 if regular
                                    expression re is satisfied by the Unicode string s; otherwise, 0
ustrregexra(s_1, re, s_2[, noc]) replaces all substrings within the Unicode string s_1 that match re
                                    with s_2 and returns the resulting string
ustrregexrf (s_1, re, s_2 | , noc |) replaces the first substring within the Unicode string s_1 that matches
                                    re with s_2 and returns the resulting string
ustrregexs(n)
                                 subexpression n from a previous ustrregexm() match
ustrreverse(s)
                                 the reverse of Unicode string s
ustrright(s,n)
                                 the last n Unicode characters of the Unicode string s
ustrrpos(s_1, s_2[, n])
                                 the position in s_1 at which s_2 is last found; otherwise, 0
ustrrtrim(s)
                                 remove trailing Unicode whitespace characters and blanks from the
                                    Unicode string s
```

generates a null-terminated byte array that can be used by the sort

```
command to produce the same order as ustrcompare()
ustrsortkeyex(s, loc, st, case, cslv, norm, num, alt, fr)
                                generates a null-terminated byte array that can be used by the sort
                                   command to produce the same order as ustrcompare()
ustrtitle(s[,loc])
                                a string with the first characters of Unicode words titlecased and
                                   other characters lowercased
ustrto(s,enc,mode)
                                converts the Unicode string s in UTF-8 encoding to a string in
                                   encoding enc
ustrtohex(s[,n])
                                escaped hex digit string of s up to 200 Unicode characters
ustrtoname(s[,p])
                                string s translated into a Stata name
ustrtrim(s)
                                removes leading and trailing Unicode whitespace characters and
                                   blanks from the Unicode string s
ustrunescape(s)
                                the Unicode string corresponding to the escaped sequences of s
ustrupper(s[,loc])
                                uppercase all characters in string s under the given locale loc
ustrword(s, n[, loc])
                                the nth Unicode word in the Unicode string s
ustrwordcount(s[,loc])
                                the number of nonempty Unicode words in the Unicode string s
usubinstr(s_1, s_2, s_3, n)
                                replaces the first n occurrences of the Unicode string s_2 with the
                                   Unicode string s_3 in s_1
                                the Unicode substring of s, starting at n_1, for a length of n_2
usubstr(s, n_1, n_2)
vec(M)
                                a column vector formed by listing the elements of M, starting with
                                   the first column and proceeding column by column
                                the row vector containing the diagonal of matrix M
vecdiag(M)
vech(M)
                                a column vector formed by listing the lower triangle elements of
vecp(M)
                                a column vector formed by listing the upper triangle elements of
                                   M
week(e_d)
                                the numeric week of the year corresponding to date e_d, the %td
                                   encoded date (days since 01jan1960)
weekly(s_1, s_2[, Y])
                                the e_w weekly date (weeks since 1960w1) corresponding to s_1
                                   based on s_2 and Y; Y specifies topyear; see date()
weibull(a,b,x)
                                the cumulative Weibull distribution with shape a and scale b
weibull(a,b,q,x)
                                the cumulative Weibull distribution with shape a, scale b, and
                                   location q
                                the probability density function of the Weibull distribution with
weibullden(a,b,x)
                                   shape a and scale b
weibullden(a,b,g,x)
                                the probability density function of the Weibull distribution with
                                   shape a, scale b, and location g
weibullph(a,b,x)
                                the cumulative Weibull (proportional hazards) distribution with shape
                                   a and scale b
                                the cumulative Weibull (proportional hazards) distribution with shape
weibullph(a,b,g,x)
                                   a, scale b, and location q
                                the probability density function of the Weibull (proportional hazards)
weibullphden(a,b,x)
                                   distribution with shape a and scale b
                                the probability density function of the Weibull (proportional hazards)
weibullphden(a,b,g,x)
                                   distribution with shape a, scale b, and location g
```

ustrsortkey(s[,loc])

the reverse cumulative Weibull (proportional hazards) distribution with shape \boldsymbol{a} and scale \boldsymbol{b}
the reverse cumulative Weibull (proportional hazards) distribution with shape $a,$ scale $b,$ and location g
the reverse cumulative Weibull distribution with shape a and scale b
the reverse cumulative Weibull distribution with shape a , scale b , and location g
the e_w weekly date (weeks since 1960w1) containing date e_d
the n th word in s ; m issing ("") if n is missing
the most closely related locale supported by ICU from loc if $type$ is 1, the actual locale where the word-boundary analysis data come from if $type$ is 2; or an empty string is returned for any other $type$
the number of words in s
the numeric year corresponding to date e_d
the e_y yearly date (year) corresponding to s_1 based on s_2 and Y ; Y specifies <i>topyear</i> ; see date()
the e_h half-yearly date (half-years since 1960h1) corresponding to year Y , half-year H
the e_m monthly date (months since 1960m1) corresponding to year $Y, \ \mathrm{month} \ M$
the e_y yearly date (year) containing date e_d
the e_q quarterly date (quarters since 1960q1) corresponding to year $Y, {\rm quarter} Q$
the \boldsymbol{e}_w weekly date (weeks since 1960w1) corresponding to year $\boldsymbol{Y},$ week \boldsymbol{W}

Also see

```
[FN] Functions by category
```

- [D] egen Extensions to generate
- [D] generate Create or change contents of variable
- [M-4] Intro Categorical guide to Mata functions
- [U] 13.3 Functions

Date and time functions

Functions

Also see

Contents

 $Cofc(e_{tc})$

 $cofC(e_{tC})$

References

Helelelices Also see		
Contents		
$age(e_{d ext{DOB}}, e_{d}ig[, s_{nl}ig])$	the age in integer years on e_d for date of birth $e_{d{\tiny DOB}}$ with s_{nl} the nonleap-year birthday for 29feb birthdates	
$\texttt{age_frac}(e_{d\text{\tiny DOB}}, e_d\big[, s_{nl}\big])$	the age in years, including the fractional part, on e_d for date of birth $e_{d{\tiny {\rm DOB}}}$ with s_{nl} the nonleap-year birthday for 29feb birthdates	
$\mathtt{birthday}(e_{d exttt{DOB}}, Yig[, s_{nl}ig])$	the e_d date of the birthday in year Y for date of birth $e_{d {\tiny DOB}}$ with s_{nl} the nonleap-year birthday for 29feb birthdates	
$bofd("cal", e_d)$	the e_b business date corresponding to e_d	
$\mathtt{Cdhms}(e_d,h,m,s)$	the e_{tC} datetime (ms. with leap seconds since 01jan1960 00:00:00.000) corresponding to $e_d,\ h,\ m,\ s$	
$\mathtt{Chms}(h,m,s)$	the e_{tC} datetime (ms. with leap seconds since 01jan1960 00:00:00.000) corresponding to $h,\ m,\ s$ on 01jan1960	
${ t Clock}(s_1,s_2[,Y])$	the e_{tC} datetime (ms. with leap seconds since 01jan1960 00:00:00.000) corresponding to s_1 based on s_2 and Y	
${ t clock}(s_1,s_2[,Y])$	the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding to s_1 based on s_2 and ${\cal Y}$	
Clockdiff(e_{tC1} , e_{tC2} , s_u)	the e_{tC} datetime difference, rounded down to an integer, from e_{tC1} to e_{tC2} in s_u units of days, hours, minutes, seconds, or milliseconds	
${ t clockdiff}(e_{tc1},e_{tc2},s_u)$	the e_{tc} datetime difference, rounded down to an integer, from e_{tc1} to e_{tc2} in s_u units of days, hours, minutes, seconds, or milliseconds	
${ t Clockdiff_frac}(e_{tC1},e_{tC2},s_{tC2})$		
	the e_{tC} datetime difference, including the fractional part, from e_{tC1} to e_{tC2} in s_u units of days, hours, minutes, seconds, or milliseconds	
$\texttt{clockdiff_frac}(e_{tc1}, e_{tc2}, s_u)$		
	the e_{tc} datetime difference, including the fractional part, from e_{tc1} to e_{tc2} in s_u units of days, hours, minutes, seconds, or milliseconds	
$ ext{Clockpart}(e_{tC}, s_u)$	the integer year, month, day, hour, minute, second, or millisecond of e_{tC} with s_u specifying which time part	
$ ext{clockpart}(e_{tc}, s_u)$	the integer year, month, day, hour, minute, second, or millisecond of e_{tc} with s_u specifying which time part	
Cmdyhms(M, D, Y, h, m, s)	the e_{tC} datetime (ms. with leap seconds since 01jan1960 00:00:00:0000) corresponding to M,D,Y,h,m,s	

Remarks and examples

Methods and formulas

00:00:00.000)

00:00:00.000)

the e_{tC} datetime (ms. with leap seconds since 01jan1960

the e_{tc} datetime (ms. without leap seconds since 01jan1960

00:00:00.000) of e_{tc} (ms. without leap seconds since 01jan1960

00:00:00.000) of e_{tC} (ms. with leap seconds since 01jan1960

```
Cofd(e_d)
                                 the e_{tC} datetime (ms. with leap seconds since 01jan1960
                                    00:00:00.000) of date e_d at time 00:00:00.000
cofd(e_d)
                                 the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) of date e_d at
                                    time 00:00:00.000
daily(s_1, s_2[, Y])
                                 a synonym for date(s_1, s_2 \mid , Y \mid)
date(s_1, s_2[, Y])
                                 the e_d date (days since 01jan1960) corresponding to s_1 based on
                                     s_2 and Y
datediff(e_{d1}, e_{d2}, s_u[, s_{nl}])
                                 the difference, rounded down to an integer, from e_{d1} to e_{d2} in
                                     s_u units of days, months, or years with s_{nl} the nonleap-year
                                     anniversary for e_{d1} on 29feb
datediff\_frac(e_{d1}, e_{d2}, s_u | , s_{nl} |)
                                 the difference, including the fractional part, from e_{d1} to e_{d2} in
                                     s_u units of days, months, or years with s_{nl} the nonleap-year
                                     anniversary for e_{d1} on 29feb
datepart(e_d, s_u)
                                 the integer year, month, or day of e_d with s_u specifying year, month,
                                    or day
day(e_d)
                                 the numeric day of the month corresponding to e_d
daysinmonth(e_d)
                                 the number of days in the month of e_d
dayssincedow(e_d,d)
                                 a synonym for dayssinceweekday (e_d, d)
dayssinceweekday(e_d,d)
                                 the number of days until e_d since previous day-of-week d
                                  a synonym for daysuntilweekday (e_d, d)
daysuntildow (e_d, d)
daysuntilweekday(e_d, d)
                                 the number of days from e_d until next day-of-week d
                                 the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding
dhms (e_d, h, m, s)
                                    to e_d, h, m, and s
dmy(D,M,Y)
                                 the e_d date (days since 01jan1960) corresponding to D, M, Y
dofb(e_b, "cal")
                                 the e_d datetime corresponding to e_b
dofC(e_{tC})
                                 the e_d date (days since 01jan1960) of datetime e_{tC} (ms. with leap
                                     seconds since 01jan1960 00:00:00.000)
                                 the e_d date (days since 01jan1960) of datetime e_{tc} (ms. since
dofc(e_{tc})
                                    01jan1960 00:00:00.000)
dofh(e_h)
                                 the e_d date (days since 01jan1960) of the start of half-year e_h
dofm(e_m)
                                 the e_d date (days since 01jan1960) of the start of month e_m
dofq(e_a)
                                 the e_d date (days since 01jan1960) of the start of quarter e_q
dofw(e_w)
                                 the e_d date (days since 01jan1960) of the start of week e_w
dofy(e_u)
                                 the e_d date (days since 01jan1960) of 01jan in year e_q
dow(e_d)
                                 the numeric day of the week corresponding to date e_d; 0 = \text{Sunday},
                                     1 = Monday, \ldots, 6 = Saturday
                                 the numeric day of the year corresponding to date e_d
doy(e_d)
firstdayofmonth(e_d)
                                 the e_d date of the first day of the month of e_d
firstdowofmonth(M,Y,d)
                                 a synonym for firstweekdayofmonth (M, Y, d)
firstweekdayofmonth(M,Y,d)
                                 the e_d date of the first day-of-week d in month M of year Y
halfyear(e_d)
                                 the numeric half of the year corresponding to date e_d
halfyearly(s_1, s_2, Y)
                                 the e_h half-yearly date (half-years since 1960h1) corresponding to
                                    s_1 based on s_2 and Y; Y specifies topyear; see date()
```

```
hh(e_{tc})
                                  the hour corresponding to datetime e_{tc} (ms. since 01jan1960
                                     00:00:00.000)
hhC(e_{tC})
                                  the hour corresponding to datetime e_{tC} (ms. with leap seconds since
                                     01jan1960 00:00:00.000)
                                  the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding
hms(h,m,s)
                                     to h, m, s on 01jan1960
hofd(e_d)
                                  the e_h half-yearly date (half years since 1960h1) containing date e_d
hours(ms)
                                  ms/3,600,000
isleapsecond(e_{tC})
                                  1 if e_{tC} is a leap second; otherwise, 0
isleapyear(Y)
                                  1 if Y is a leap year; otherwise, 0
lastdayofmonth(e_d)
                                  the e_d date of the last day of the month of e_d
lastdowofmonth(M, Y, d)
                                  a synonym for lastweekdayofmonth (M, Y, d)
lastweekdayofmonth(M, Y, d)
                                  the e_d date of the last day-of-week d in month M of year Y
mdy(M,D,Y)
                                  the e_d date (days since 01jan1960) corresponding to M, D, Y
mdyhms(M, D, Y, h, m, s)
                                  the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding
                                     to M, D, Y, h, m, s
minutes(ms)
                                 ms/60,000
mm(e_{tc})
                                  the minute corresponding to datetime e_{tc} (ms. since 01jan1960
                                     00:00:00.000)
mmC(e_{tC})
                                  the minute corresponding to datetime e_{tC} (ms. with leap seconds
                                     since 01jan1960 00:00:00.000)
mofd(e_d)
                                  the e_m monthly date (months since 1960m1) containing date e_d
month(e_d)
                                  the numeric month corresponding to date e_d
monthly(s_1, s_2[, Y])
                                  the e_m monthly date (months since 1960m1) corresponding to s_1
                                     based on s_2 and Y; Y specifies topyear; see date()
                                  h \times 3,600,000
msofhours(h)
msofminutes(m)
                                 m \times 60,000
msofseconds(s)
                                  s \times 1,000
nextbirthday(e_{d \text{ DOB}}, e_d[, s_{nl}])
                                  the e_d date of the first birthday after e_d for date of birth e_{d \text{ DOB}}
                                     with s_{nl} the nonleap-year birthday for 29feb birthdates
nextdow(e_d,d)
                                  a synonym for nextweekday (e_d, d)
nextleapyear(Y)
                                  the first leap year after year Y
nextweekday(e_d,d)
                                  the e_d date of the first day-of-week d after e_d
now()
                                  the current e_{tc} datetime
previousbirthday(e_{d\,	ext{DOB}}, e_d | ,s_{nl} |)
                                  the e_d date of the birthday immediately before e_d for date of birth
                                     e_{d\,\mathrm{DOB}} with s_{nl} the nonleap-year birthday for 29feb birthdates
previousdow(e_d, d)
                                  a synonym for previousweekday (e_d, d)
previousleapyear(Y)
                                  the leap year immediately before year Y
previousweekday(e_d,d)
                                  the e_d date of the last day-of-week d before e_d
qofd(e_d)
                                  the e_q quarterly date (quarters since 1960q1) containing date e_d
quarter(e_d)
                                  the numeric quarter of the year corresponding to date e_d
```

quarterly($s_1, s_2[,Y]$)	the e_q quarterly date (quarters since 1960q1) corresponding to s_1 based on s_2 and $Y;Y$ specifies topyear, see date()
seconds(ms)	$ms/1,\!000$
$\mathtt{ss}(e_{tc})$	the second corresponding to datetime e_{tc} (ms. since 01jan1960 00:00:00.000)
$\mathtt{ssC}(e_{tC})$	the second corresponding to datetime e_{tC} (ms. with leap seconds since 01jan1960 00:00:00.000)
tC(l)	convenience function to make typing dates and times in expressions easier
tc(l)	convenience function to make typing dates and times in expressions easier
td(l)	convenience function to make typing dates in expressions easier
$\mathtt{th}(l)$	convenience function to make typing half-yearly dates in expressions easier
tm(l)	convenience function to make typing monthly dates in expressions easier
today()	today's e_d date
tq(l)	convenience function to make typing quarterly dates in expressions easier
tw(l)	convenience function to make typing weekly dates in expressions easier
$\mathtt{week}(e_d)$	the numeric week of the year corresponding to date e_d , the %td encoded date (days since 01jan1960)
$weekly(s_1, s_2[, Y])$	the e_w weekly date (weeks since 1960w1) corresponding to s_1 based on s_2 and Y ; Y specifies $topyear$; see date()
$\mathtt{wofd}(e_d)$	the e_w weekly date (weeks since 1960w1) containing date e_d
$\mathtt{year}(e_d)$	the numeric year corresponding to date e_d
$yearly(s_1, s_2[,Y])$	the e_y yearly date (year) corresponding to s_1 based on s_2 and Y ; Y specifies <i>topyear</i> ; see date()
yh(Y, H)	the e_h half-yearly date (half-years since 1960h1) corresponding to year Y , half-year H
ym(Y,M)	the e_m monthly date (months since 1960m1) corresponding to year Y , month M
$\mathtt{yofd}(e_d)$	the e_y yearly date (year) containing date e_d
yq(Y,Q)	the e_q quarterly date (quarters since 1960q1) corresponding to year $Y, {\rm quarter} Q$
yw(Y,W)	the e_w weekly date (weeks since 1960w1) corresponding to year Y , week W

Functions

Stata's date and time functions are described with examples in [U] 25 Working with dates and times, [D] Datetime, [D] Datetime durations, and [D] Datetime relative dates. What follows is a technical description. We use the following notation:

```
%tb business calendar date (days)
e_{b}
      %tc encoded datetime (ms. since 01jan1960 00:00:00.000)
e_{tc}
      %tC encoded datetime (ms. with leap seconds since 01jan1960 00:00:00.000)
e_{tC}
      %td encoded date (days since 01jan1960)
e_d
      %tw encoded weekly date (weeks since 1960w1)
e_{m}
      %tm encoded monthly date (months since 1960m1)
e_m
      %tq encoded quarterly date (quarters since 1960q1)
e_a
      %th encoded half-yearly date (half-years since 1960h1)
e_h
      %ty encoded yearly date (years)
e_y
M
      month, 1-12
D
      day of month, 1-31
Y
      year, 0100-9999
h
      hour, 0-23
      minute, 0-59
m
      second, 0-59 or 60 if leap seconds
s
      milliseconds
ms
W
      week number, 1-52
Q
      quarter number, 1-4
Η
      half-year number, 1 or 2
      numeric day of the week, 0 = \text{Sunday}, 1 = \text{Monday}, ..., 6 = \text{Saturday}
d
```

The date and time functions, where integer arguments are required, allow noninteger values and use the floor() of the value.

A Stata date-and-time variable is recorded as the number of milliseconds, days, weeks, etc., depending upon the units, from 01jan1960. Negative values indicate dates and times before 01jan1960. Allowable dates and times are those between 01jan0100 and 31dec9999, inclusive, but all functions are based on the Gregorian calendar, and values do not correspond to historical dates before Friday, 15oct1582.

```
age (e_{d \text{ DOB}}, e_d [ , s_{nl} ])
```

Description: the age in integer years on e_d for date of birth $e_{d \, \text{DOB}}$ with s_{nl} the nonleap-year birthday for 29feb birthdates

 s_{nl} specifies when someone born on 29feb becomes another year older in nonleap years. $s_{nl} = "01mar"$ (the default) means the birthday is taken to be 01mar. $s_{nl} = "28feb"$ means the birthday is taken to be 28feb. See *Methods and formulas*.

When $e_d < e_{d,DOB}$, the result is missing.

Domain $e_{d \text{ DOB}}$: e_d dates 01jan0101 to 31dec9998 (integers -678,985 to 2,936,184) Domain e_d : e_d dates 01jan0101 to 31dec9998 (integers -678,985 to 2,936,184)

Domain s_{nl} : strings "28feb", "feb28", "01mar", "1mar", "mar01", and "mar1" (case

insensitive)

Range: integers 0 to 9897 or missing

 $ext{age_frac}(e_{d\, ext{d}\, ext{DOB}},e_{d}ig\lceil,s_{nl}ig
ceil)$

Description: the age in years, including the fractional part, on e_d for date of birth $e_{d \text{ DOB}}$ with

 s_{nl} the nonleap-year birthday for 29feb birthdates

 s_{nl} specifies when someone born on 29feb becomes another year older in nonleap years. $s_{nl} =$ "01mar" (the default) means the birthday is taken to be 01mar. $s_{nl} =$ "28feb" means the birthday is taken to be 28feb. See *Methods and*

formulas.

When $e_d < e_{d \text{ DOB}}$, the result is missing.

Domain $e_{d \text{ DOB}}$: e_d dates 01jan0101 to 31dec9998 (integers -678,985 to 2,936,184) Domain e_d : e_d dates 01jan0101 to 31dec9998 (integers -678,985 to 2,936,184)

Domain s_{nl} : strings "28feb", "feb28", "01mar", "1mar", "mar01", and "mar1" (case

insensitive)

Range: reals 0 to 9897.997... or missing

 $ext{birthday}(e_{d_{ ext{ DOB}}},Y[ext{ ,}s_{nl}])$

Description: the e_d date of the birthday in year Y for date of birth $e_{d \text{ DOB}}$ with s_{nl} the

nonleap-year birthday for 29feb birthdates

 s_{nl} specifies when someone born on 29feb becomes another year older in nonleap years. $s_{nl} = "01mar"$ (the default) means the birthday is taken to be 01mar. $s_{nl} = "28feb"$ means the birthday is taken to be 28feb. See *Methods and*

formulas.

Domain $e_{d \text{ DOB}}$: e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Domain Y: integers 0100 to 9999 (but probably 1800 to 2100)

Domain s_{nl} : strings "28feb", "feb28", "01mar", "1mar", "mar01", and "mar1" (case

insensitive)

Range: e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) or missing

 $bofd("cal",e_d)$

Description: the e_b business date corresponding to e_d business calendar names and formats

Domain e_d : e_d as defined by business calendar named cal as defined by business calendar named cal

 $\texttt{Cdhms}(e_d,h,m,s)$

Description: the e_{tC} datetime (ms. with leap seconds since 01jan1960 00:00:00.000) corre-

sponding to e_d , h, m, s

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Domain h: integers 0 to 23 Domain m: integers 0 to 59 Domain s: reals 0.000 to 60.999

Range: e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999+number of leap seconds)

or missing

Chms (h, m, s)

Description: the e_{tC} datetime (ms. with leap seconds since 01jan1960 00:00:00.000) corre-

sponding to h, m, s on 01jan1960

Domain h: integers 0 to 23 Domain m: integers 0 to 59 Domain s: reals 0.000 to 60.999

Range: e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999+number of leap seconds)

or missing

 $Clock(s_1, s_2[, Y])$

Description: the e_{tC} datetime (ms. with leap seconds since 01jan1960 00:00:00.000) corre-

sponding to s_1 based on s_2 and Y

Function Clock() works the same as function clock() except that Clock() returns a leap second-adjusted t_C value rather than an unadjusted t_c value. Use

Clock() only if original time values have been adjusted for leap seconds.

Domain s_1 : strings Domain s_2 : strings

Domain Y: integers 1000 to 9998 (but probably 2001 to 2099)

Range: e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999+number of leap seconds)

or missing

 $clock(s_1, s_2 \mid , Y \mid)$

Description: the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding to s_1 based on s_2 and Y

> s_1 contains the date, time, or both, recorded as a string, in virtually any format. Months can be spelled out, abbreviated (to three characters), or indicated as numbers; years can include or exclude the century; blanks and punctuation are allowed.

> s_2 is any permutation of M, D, [#]Y, h, m, and s, with their order defining the order that month, day, year, hour, minute, and second occur (and whether they occur) in s_1 . ##, if specified, indicates the default century for two-digit years in s_1 . For instance, $s_2 = "MD19Y hm"$ would translate $s_1 = "11/15/91 \ 21:14"$ as 15nov1991 21:14. The space in "MD19Y hm" was not significant and the string would have translated just as well with "MD19Yhm".

> Y provides an alternate way of handling two-digit years. Y specifies the largest year that is to be returned when a two-digit year is encountered; see function date() below. If neither ## nor Y is specified, clock() returns missing when it encounters a two-digit year.

Domain s_1 : strings Domain s_2 : strings

Domain Y: integers 1000 to 9998 (but probably 2001 to 2099)

Range: e_{tc} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999) or missing

Clockdiff (e_{tC1}, e_{tC2}, s_u)

Description: the e_{tC} datetime difference, rounded down to an integer, from e_{tC1} to e_{tC2} in

 s_u units of days, hours, minutes, seconds, or milliseconds

Note that Clockdiff(e_{tC1} , e_{tC2} , s_u) = -Clockdiff(e_{tC2} , e_{tC1} , s_u).

Domain e_{tC1} : e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999+number of leap seconds)

Domain e_{tC2} : e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999+number of leap seconds) Domain s_u : strings "day" or "d" for day; "hour" or "h" for hour; "minute", "min", or

"m" for minute; "second", "sec", or "s" for second; and "millisecond" or

"ms" for millisecond (case insensitive)

Range: integers -312,413,759,999,999 - number of leap seconds to

312,413,759,999,999 + number of leap seconds or missing

 $clockdiff(e_{tc1}, e_{tc2}, s_u)$

Description: the e_{tc} datetime difference, rounded down to an integer, from e_{tc1} to e_{tc2} in s_u

units of days, hours, minutes, seconds, or milliseconds

Note that clockdiff $(e_{tc1}, e_{tc2}, s_u) = -\text{clockdiff}(e_{tc2}, e_{tc1}, s_u)$.

Domain e_{tc1} : e_{tc} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999)

Domain e_{tc2} : e_{tc} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999)

Domain s_u : strings "day" or "d" for day; "hour" or "h" for hour; "minute", "min", or

"m" for minute; "second", "sec", or "s" for second; and "millisecond" or

"ms" for millisecond (case insensitive)

Range: integers -312,413,759,999,999 to 312,413,759,999,999 or missing

 ${\tt Clockdiff_frac}(e_{tC1},e_{tC2},s_u)$

Description: the e_{tC} datetime difference, including the fractional part, from e_{tC1} to e_{tC2} in

 s_u units of days, hours, minutes, seconds, or milliseconds

Note that

 $\texttt{Clockdiff_frac}(e_{tC1}, e_{tC2}, s_u) = -\texttt{Clockdiff_frac}(e_{tC2}, e_{tC1}, s_u).$

Domain e_{tC1} : e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58.695.840,000,000 to 253,717,919,999,999+number of leap seconds)

Domain e_{tC2} : e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999+number of leap seconds)

Domain s_u : strings "day" or "d" for day; "hour" or "h" for hour; "minute", "min", or

"m" for minute; "second", "sec", or "s" for second; and "millisecond" or

"ms" for millisecond (case insensitive)

Range: reals -312,413,759,999,999 - number of leap seconds to 312,413,759,999,999 +

number of leap seconds or missing

$clockdiff_frac(e_{tc1}, e_{tc2}, s_u)$

Description: the e_{tc} datetime difference, including the fractional part, from e_{tc1} to e_{tc2} in s_u

units of days, hours, minutes, seconds, or milliseconds

Note that

 $\texttt{clockdiff_frac}(e_{tc1}, e_{tc2}, s_u) = -\texttt{clockdiff_frac}(e_{tc2}, e_{tc1}, s_u).$

Domain e_{tc1} : e_{tc} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999)

Domain e_{tc2} : e_{tc} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999)

Domain s_u : strings "day" or "d" for day; "hour" or "h" for hour; "minute", "min", or

"m" for minute; "second", "sec", or "s" for second; and "millisecond" or

"ms" for millisecond (case insensitive)

Range: reals -312,413,759,999,999 to 312,413,759,999,999 or missing

Clockpart (e_{tC}, s_u)

Description: the integer year, month, day, hour, minute, second, or millisecond of e_{tC} with

 s_u specifying which time part

Domain e_{tC} : e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

 $(integers - 58,695,840,000,000 \ to \ 253,717,919,999,999 + number \ of \ leap \ seconds)$

Domain s_u : strings "year" or "y" for year; "month" or "mon" for month; "day" or "d"

for day; "hour" or "h" for hour; "minute" or "min" for minute; "second", "sec", or "s" for second; and "millisecond" or "ms" for millisecond (case

insensitive)

Range: integers 0 to 9999 or missing

$clockpart(e_{tc}, s_u)$

Description: the integer year, month, day, hour, minute, second, or millisecond of e_{tc} with s_u

specifying which time part

Domain e_{tc} : e_{tc} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999)

Domain s_u : strings "year" or "y" for year; "month" or "mon" for month; "day" or "d"

for day; "hour" or "h" for hour; "minute" or "min" for minute; "second",

"sec", or "s" for second; and "millisecond" or "ms" for millisecond (case

insensitive)

Range: integers 0 to 9999 or missing

Cmdyhms (M, D, Y, h, m, s)

Description: the e_{tC} datetime (ms. with leap seconds since 01jan1960 00:00:00.000) corre-

sponding to M, D, Y, h, m, s

Domain M: integers 1 to 12 Domain D: integers 1 to 31

Domain *Y*: integers 0100 to 9999 (but probably 1800 to 2100)

Domain h: integers 0 to 23 Domain m: integers 0 to 59 Domain s: reals 0.000 to 60.999

Range: e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999+number of leap seconds)

or missing

 $Cofc(e_{tc})$

Description: the e_{tC} datetime (ms. with leap seconds since 01jan1960 00:00:00.000) of e_{tc}

(ms. without leap seconds since 01jan1960 00:00:00.000)

Domain e_{tc} : e_{tc} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999)

Range: e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999+number of leap seconds)

 $\mathtt{cofC}(e_{tC})$

Description: the e_{tc} datetime (ms. without leap seconds since 01jan1960 00:00:00.000) of e_{tC}

(ms. with leap seconds since 01jan1960 00:00:00.000)

Domain e_{tC} : e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999+number of leap seconds) Range e_{tc} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999)

 $\mathtt{Cofd}(e_d)$

Description: the e_{tC} datetime (ms. with leap seconds since 01jan1960 00:00:00.000) of date

 e_d at time 00:00:00.000

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) Range: e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999+number of leap seconds)

 $cofd(e_d)$

Description: the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) of date e_d at time

00:00:00.000

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) Range: e_{tc} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999)

 $daily(s_1, s_2[, Y])$

Description: a synonym for date $(s_1, s_2[, Y])$

 $\mathtt{date}(s_1, s_2[, Y])$

Description:

the e_d date (days since 01jan1960) corresponding to s_1 based on s_2 and Y

 s_1 contains the date, recorded as a string, in virtually any format. Months can be spelled out, abbreviated (to three characters), or indicated as numbers; years can include or exclude the century; blanks and punctuation are allowed.

 s_2 is any permutation of M, D, and [##]Y, with their order defining the order that month, day, and year occur in s_1 . ##, if specified, indicates the default century for two-digit years in s_1 . For instance, $s_2 =$ "MD19Y" would translate $s_1 =$ "11/15/91" as 15nov1991.

Y provides an alternate way of handling two-digit years. When a two-digit year is encountered, the largest year, *topyear*, that does not exceed Y is returned.

```
date("1/15/08","MDY",1999) = 15jan1908
date("1/15/08","MDY",2019) = 15jan2008
date("1/15/51","MDY",2000) = 15jan1951
date("1/15/50","MDY",2000) = 15jan1950
date("1/15/49","MDY",2000) = 15jan1949
date("1/15/01","MDY",2050) = 15jan2001
date("1/15/00","MDY",2050) = 15jan2000
```

If neither ## nor Y is specified, date() returns missing when it encounters a two-digit year. See Working with two-digit years in [D] Datetime conversion for more information.

Domain s_1 : strings Domain s_2 : strings

Domain Y: integers 1000 to 9998 (but probably 2001 to 2099)

Range: e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) or missing

 $\mathtt{datediff}(e_{d1}, e_{d2}, s_u[, s_{nl}])$

Description: the difference, rounded down to an integer, from e_{d1} to e_{d2} in s_u units of days, months, or years with s_{nl} the nonleap-year anniversary for e_{d1} on 29feb

 s_{nl} specifies the anniversary when e_{d1} is on 29feb. $s_{nl} = "01mar"$ (the default) means the anniversary is taken to be 01mar. $s_{nl} = "28feb"$ means the anniversary is taken to be 28feb. See *Methods and formulas*.

Note that datediff(e_{d1} , e_{d2} , s_u , s_{nl}) = -datediff(e_{d2} , e_{d1} , s_u , s_{nl}).

Domain e_{d1} : e_d dates 01jan0101 to 31dec9998 (integers -678,985 to 2,936,184) Domain e_{d2} : e_d dates 01jan0101 to 31dec9998 (integers -678,985 to 2,936,184)

Domain s_u : strings "day" or "d" for day; "month", "mon", or "m" for month; and "year"

or "y" for year (case insensitive)

Domain s_{nl} : strings "28feb", "feb28", "01mar", "1mar", "mar01", and "mar1" (case

insensitive)

Range: integers -3,615,169 to 3,615,169 or missing

 $\mathtt{datediff_frac}(e_{d1}, e_{d2}, s_u[, s_{nl}])$

Description: the difference, including the fractional part, from e_{d1} to e_{d2} in s_u units of days,

months, or years with s_{nl} the nonleap-year anniversary for e_{d1} on 29feb

 s_{nl} specifies the anniversary when e_{d1} is on 29feb. $s_{nl}=$ "01mar" (the default) means the anniversary is taken to be 01mar. $s_{nl}=$ "28feb" means the anniversary

is taken to be 28feb. See Methods and formulas. Note that datediff_frac(e_{d1} , e_{d2} , s_u , s_{nl}) = $-\text{datediff}_{\text{frac}}(e_{d2}, e_{d1}, s_u, s_{nl})$.

Domain e_{d1} : e_d dates 01jan0101 to 31dec9998 (integers -678,985 to 2,936,184) Domain e_{d2} : e_d dates 01jan0101 to 31dec9998 (integers -678,985 to 2,936,184)

Domain s_u : strings "day" or "d" for day; "month", "mon", or "m" for month; and "year"

or "y" for year (case insensitive)

Domain s_{nl} : strings "28feb", "feb28", "01mar", "1mar", "mar01", and "mar1" (case

insensitive)

Range: reals -3,615,169 to 3,615,169 or missing

 $datepart(e_d, s_u)$

Description: the integer year, month, or day of e_d with s_u specifying year, month, or day

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Domain s_u : strings "day" or "d" for day; "month", "mon", or "m" for month; and "year"

or "y" for year (case insensitive)

Range: integers 1 to 9999 or missing

 $\mathtt{day}(e_d)$

Description: the numeric day of the month corresponding to e_d

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Range: integers 1 to 31 or missing

 $\mathtt{daysinmonth}(e_d)$

Description: the number of days in the month of e_d

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Range: integers 28 to 31 or missing

 $exttt{dayssincedow}(e_d,d)$

Description: a synonym for dayssinceweekday (e_d, d)

 $exttt{dayssinceweekday}(e_d,d)$

Description: the number of days until e_d since previous day-of-week d

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Domain d: integers 0 to 6 (0=Sunday, 1=Monday, ..., 6=Saturday); alternatively, strings

with the first two or more letters of the day of week (case insensitive)

Range: integers 1 to 7 or missing

 $daysuntildow(e_d,d)$

Description: a synonym for daysuntilweekday (e_d, d)

daysuntilweekday(e_d ,d)

Description: the number of days from e_d until next day-of-week d

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Domain d: integers 0 to 6 (0=Sunday, 1=Monday, ..., 6=Saturday); alternatively, strings

with the first two or more letters of the day of week (case insensitive)

Range: integers 1 to 7 or missing

$dhms(e_d,h,m,s)$

Description: the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding to e_d , h, m,

and s

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Domain h: integers 0 to 23 Domain m: integers 0 to 59 Domain s: reals 0.000 to 59.999

Range: e_{tc} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999) or missing

dmy(D, M, Y)

Description: the e_d date (days since 01jan1960) corresponding to D, M, Y

Domain D: integers 1 to 31 Domain M: integers 1 to 12

Domain Y: integers 0100 to 9999 (but probably 1800 to 2100)

Range: e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) or missing

$dofb(e_b, "cal")$

Description: the e_d datetime corresponding to e_b

Domain e_b : e_b as defined by business calendar named cal

Domain *cal*: business calendar names and formats
Range: as defined by business calendar named *cal*

$dofC(e_{tC})$

Description: the e_d date (days since 01jan1960) of datetime e_{tC} (ms. with leap seconds since

01jan1960 00:00:00.000)

Domain e_{tC} : e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999+number of leap seconds)

Range: e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

$dofc(e_{tc})$

Description: the e_d date (days since 01jan1960) of datetime e_{tc} (ms. since 01jan1960

00:00:00.000)

Domain e_{tc} : e_{tc} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999)

Range: e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

 $dofh(e_h)$

Description: the e_d date (days since 01jan1960) of the start of half-year e_h

Domain e_h : e_h dates 0100h1 to 9999h2 (integers -3,720 to 16,079)

Range: e_d dates 01jan0100 to 01jul9999 (integers -679,350 to 2,936,366)

 $dofm(e_m)$

Description: the e_d date (days since 01jan1960) of the start of month e_m Domain e_m : e_m dates 0100m1 to 9999m12 (integers -22,320 to 96,479)

Range: e_d dates 01jan0100 to 01dec9999 (integers -679,350 to 2,936,519)

 $dofq(e_q)$

Description: the e_d date (days since 01jan1960) of the start of quarter e_q Domain e_q : e_q dates 0100q1 to 9999q4 (integers -7,440 to 32,159)

Range: e_d dates 01jan0100 to 01oct9999 (integers -679,350 to 2,936,458)

 $\mathtt{dofw}(e_w)$

Description: the e_d date (days since 01jan1960) of the start of week e_w Domain e_w : e_w dates 0100w1 to 9999w52 (integers -96,720 to 418,079)

Range: e_d dates 01jan0100 to 24dec9999 (integers -679,350 to 2,936,542)

 $\mathtt{dofy}(e_y)$

Description: the e_d date (days since 01jan1960) of 01jan in year e_y

Domain e_y : e_y dates 0100 to 9999 (integers 0100 to 9999)

Range: $e_d^{''}$ dates 01jan0100 to 01jan9999 (integers -679,350 to 2,936,185)

 $\mathtt{dow}(e_d)$

Description: the numeric day of the week corresponding to date e_d ; 0 = Sunday, 1 = Monday,

 \dots , 6 = Saturday

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Range: integers 0 to 6 or missing

 $doy(e_d)$

Description: the numeric day of the year corresponding to date e_d

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Range: integers 1 to 366 or missing

 $firstdayofmonth(e_d)$

Description: the e_d date of the first day of the month of e_d

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Range: e_d dates 01jan0100 to 01dec9999 (integers -679,350 to 2,936,519) or missing

firstdowofmonth(M,Y,d)

Description: a synonym for firstweekdayofmonth(M, Y, d)

firstweekdayofmonth(M,Y,d)

Description: the e_d date of the first day-of-week d in month M of year Y

Domain M: integers 1 to 12

Domain *Y*: integers 0100 to 9999 (but probably 1800 to 2100)

Domain d: integers 0 to 6 (0=Sunday, 1=Monday, ..., 6=Saturday); alternatively, strings

with the first two or more letters of the day of week (case insensitive)

Range: e_d dates 01jan0100 to 07dec9999 (integers -679,350 to 2,936,525) or missing

$halfyear(e_d)$

Description: the numeric half of the year corresponding to date e_d

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Range: integers 1, 2, or missing

halfyearly($s_1, s_2[, Y]$)

Description: the e_h half-yearly date (half-years since 1960h1) corresponding to s_1 based on

 s_2 and Y; Y specifies topyear; see date()

Domain s_1 : strings

Domain s_2 : strings "HY" and "YH"; Y may be prefixed with ## Domain Y: integers 1000 to 9998 (but probably 2001 to 2099)

Range: e_h dates 0100h1 to 9999h2 (integers -3,720 to 16,079) or missing

$hh(e_{tc})$

Description: the hour corresponding to datetime e_{tc} (ms. since 01jan1960 00:00:00.000)

Domain e_{tc} : e_{tc} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999)

Range: integers 0 through 23 or missing

$hhC(e_{tC})$

Description: the hour corresponding to datetime e_{tC} (ms. with leap seconds since 01jan1960

00:00:00.000)

Domain e_{tC} : e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999+number of leap seconds)

Range: integers 0 through 23 or missing

hms(h,m,s)

Description: the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding to h, m, s

on 01jan1960

Domain h: integers 0 to 23 Domain m: integers 0 to 59 Domain s: reals 0.000 to 59.999

Range: datetimes 01jan1960 00:00:00.000 to 01jan1960 23:59:59.999 (integers 0 to

86,399,999 or *missing*)

 $hofd(e_d)$

Description: the e_h half-yearly date (half years since 1960h1) containing date e_d Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Range: e_h dates 0100h1 to 9999h2 (integers -3,720 to 16,079)

hours(ms)

Description: ms/3,600,000Domain ms: real; milliseconds Range: real or missing

 $isleapsecond(e_{tC})$

Description: 1 if e_{tC} is a leap second; otherwise, 0

Domain e_{tC} : e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999+number of leap seconds)

Range: 0, 1, or missing

isleapyear(Y)

Description: 1 if Y is a leap year; otherwise, 0

Domain *Y*: integers 0100 to 9999 (but probably 1800 to 2100)

Range: 0, 1, or missing

 ${ t last day of month}(e_d)$

Description: the e_d date of the last day of the month of e_d

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Range: e_d dates 31jan0100 to 31dec9999 (integers -679,320 to 2,936,549) or missing

lastdowofmonth(M, Y, d)

Description: a synonym for lastweekdayofmonth (M, Y, d)

lastweekdayofmonth (M, Y, d)

Description: the e_d date of the last day-of-week d in month M of year Y

Domain M: integers 1 to 12

Domain Y: integers 0100 to 9999 (but probably 1800 to 2100)

Domain d: integers 0 to 6 (0=Sunday, 1=Monday, ..., 6=Saturday); alternatively, strings

with the first two or more letters of the day of week (case insensitive)

Range: e_d dates 25jan0100 to 31dec9999 (integers -679,326 to 2,936,549) or missing

mdy(M,D,Y)

Description: the e_d date (days since 01jan1960) corresponding to M, D, Y

Domain M: integers 1 to 12 Domain D: integers 1 to 31

Domain *Y*: integers 0100 to 9999 (but probably 1800 to 2100)

Range: e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) or missing

mdyhms(M,D,Y,h,m,s)

Description: the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding to M, D, Y,

h, m, s

Domain M: integers 1 to 12 Domain D: integers 1 to 31

Domain Y: integers 0100 to 9999 (but probably 1800 to 2100)

Domain h: integers 0 to 23 Domain m: integers 0 to 59 Domain s: reals 0.000 to 59.999

Range: e_{tc} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999) or missing

minutes(ms)

Description: ms/60,000Domain ms: real; milliseconds Range: real or missing

 $mm(e_{tc})$

Description: the minute corresponding to datetime e_{tc} (ms. since 01jan1960 00:00:00.000)

Domain e_{tc} : e_{tc} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999)

Range: integers 0 through 59 or missing

 $\mathtt{mmC}(e_{tC})$

Description: the minute corresponding to datetime e_{tC} (ms. with leap seconds since 01jan1960

(000.00:00.000)

Domain e_{tC} : e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58.695.840.000.000 to 253.717.919.999.999 + number of leap seconds)

Range: integers 0 through 59 or missing

 $mofd(e_d)$

Description: the e_m monthly date (months since 1960m1) containing date e_d Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Range: e_m dates 0100m1 to 9999m12 (integers -22,320 to 96,479)

 $\mathtt{month}(e_d)$

Description: the numeric month corresponding to date e_d

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Range: integers 1 to 12 or missing

monthly($s_1, s_2[, Y]$)

Description: the e_m monthly date (months since 1960m1) corresponding to s_1 based on s_2

and Y; Y specifies topyear; see date()

Domain s_1 : strings

Domain s_2 : strings "MY" and "YM"; Y may be prefixed with ## Domain Y: integers 1000 to 9998 (but probably 2001 to 2099)

Range: e_m dates 0100m1 to 9999m12 (integers -22,320 to 96,479) or missing

msofhours(h)

Description: $h \times 3,600,000$ Domain h: real; hours

Range: real or *missing*; milliseconds

msofminutes(m)

Description: $m \times 60,000$ Domain m: real; minutes

Range: real or *missing*; milliseconds

msofseconds(s)

Description: $s \times 1,000$ Domain s: real; seconds

Range: real or *missing*; milliseconds

nextbirthday($e_{d\, ext{d}\, ext{DOB}}$, $e_{d}[$, s_{nl}])

Description: the e_d date of the first birthday after e_d for date of birth $e_{d \text{ DOB}}$ with s_{nl} the

nonleap-year birthday for 29feb birthdates

 s_{nl} specifies when someone born on 29feb becomes another year older in nonleap years. $s_{nl}=$ "01mar" (the default) means the birthday is taken to be 01mar. $s_{nl}=$ "28feb" means the birthday is taken to be 28feb. See *Methods and*

formulas.

Domain $e_{d \text{ DOB}}$: e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Domain s_{nl} : strings "28feb", "feb28", "01mar", "1mar", "mar01", and "mar1" (case

insensitive)

Range: e_d dates 01jan0101 to 31dec9999 (integers -678,985 to 2,936,549) or missing

$nextdow(e_d,d)$

Description: a synonym for nextweekday (e_d, d)

nextleapyear(Y)

Description: the first leap year after year Y

Domain Y: integers 0100 to 9999 (but probably 1800 to 2100)

Range: integers 1584 to 9996 or missing

$nextweekday(e_d,d)$

Description: the e_d date of the first day-of-week d after e_d

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Domain d: integers 0 to 6 (0=Sunday, 1=Monday, ..., 6=Saturday); alternatively, strings

with the first two or more letters of the day of week (case insensitive)

Range: e_d dates 02jan0100 to 31dec9999 (integers -679,349 to 2,936,549) or missing

now()

Description: the current e_{tc} datetime

Range: e_{tc} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999)

$exttt{previousbirthday}(e_{d_{ exttt{DOB}}}$, $e_dig[$, $s_{nl}ig]$)

Description: the e_d date of the birthday immediately before e_d for date of birth $e_{d,DOB}$ with

 s_{nl} the nonleap-year birthday for 29feb birthdates

 s_{nl} specifies when someone born on 29feb becomes another year older in nonleap years. $s_{nl}=$ "01mar" (the default) means the birthday is taken to be 01mar. $s_{nl}=$ "28feb" means the birthday is taken to be 28feb. See *Methods and*

formulas.

Domain $e_{d \text{ DOB}}$: e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Domain s_{nl} : strings "28feb", "feb28", "01mar", "1mar", "mar01", and "mar1" (case

insensitive)

Range: e_d dates 01jan0100 to 31dec9998 (integers -679,350 to 2,936,184) or missing

$previousdow(e_d,d)$

Description: a synonym for previousweekday (e_d, d)

previousleapyear(Y)

Description: the leap year immediately before year Y

Domain Y: integers 0100 to 9999 (but probably 1800 to 2100)

Range: integers 1584 to 9996 or missing

previousweekday (e_d,d)

Description: the e_d date of the last day-of-week d before e_d

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Domain d: integers 0 to 6 (0=Sunday, 1=Monday, ..., 6=Saturday); alternatively, strings

with the first two or more letters of the day of week (case insensitive)

Range: e_d dates 01jan0100 to 30dec9999 (integers -679,350 to 2,936,548) or missing

$qofd(e_d)$

Description: the e_q quarterly date (quarters since 1960q1) containing date e_d Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Range: e_q dates 0100q1 to 9999q4 (integers -7,440 to 32,159)

 $quarter(e_d)$

Description: the numeric quarter of the year corresponding to date e_d

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Range: integers 1 to 4 or missing

quarterly($s_1, s_2[,Y]$)

Description: the e_q quarterly date (quarters since 1960q1) corresponding to s_1 based on s_2

and Y; Y specifies topyear; see date()

Domain s_1 : strings

Domain s_2 : strings "QY" and "YQ"; Y may be prefixed with ## integers 1000 to 9998 (but probably 2001 to 2099)

Range: e_q dates 0100q1 to 9999q4 (integers -7,440 to 32,159) or missing

seconds(ms)

Description: ms/1,000

Domain ms: real; milliseconds Range: real or missing

 $ss(e_{tc})$

Description: the second corresponding to datetime e_{tc} (ms. since 01jan1960 00:00:00.000)

Domain e_{tc} : e_{tc} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999)

Range: real 0.000 through 59.999 or missing

 $ssC(e_{tC})$

Description: the second corresponding to datetime e_{tC} (ms. with leap seconds since 01jan1960

00:00:00.000)

Domain e_{tC} : e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999+number of leap seconds)

Range: real 0.000 through 60.999 or missing

tC(l)

Description: convenience function to make typing dates and times in expressions easier

Same as tc(), except returns leap second-adjusted values; for example, typing tc(29nov2007 9:15) is equivalent to typing 1511946900000, whereas

tC(29nov2007 9:15) is 1511946923000.

Domain *l*: datetime literal strings 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

Range: e_{tC} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999+number of leap seconds)

tc(l)

Description: convenience function to make typing dates and times in expressions easier

For example, typing tc(2jan1960 13:42) is equivalent to typing 135720000; the date but not the time may be omitted, and then 01jan1960 is assumed; the seconds portion of the time may be omitted and is assumed to be 0.000;

tc(11:02) is equivalent to typing 39720000.

Domain l: datetime literal strings 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

 e_{tc} datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999

(integers -58,695,840,000,000 to 253,717,919,999,999)

td(l)

Range:

Description: convenience function to make typing dates in expressions easier

For example, typing td(2jan1960) is equivalent to typing 1.

Domain l: date literal strings 01jan0100 to 31dec9999

Range: e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

th(l)

Description: convenience function to make typing half-yearly dates in expressions easier

For example, typing th(1960h2) is equivalent to typing 1.

Domain *l*: half-year literal strings 0100h1 to 9999h2

Range: e_h dates 0100h1 to 9999h2 (integers -3,720 to 16,079)

tm(l)

Description: convenience function to make typing monthly dates in expressions easier

For example, typing tm(1960m2) is equivalent to typing 1.

Domain *l*: month literal strings 0100m1 to 9999m12

Range: e_m dates 0100m1 to 9999m12 (integers -22,320 to 96,479)

today()

Description: today's e_d date

Range: e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

tq(l)

Description: convenience function to make typing quarterly dates in expressions easier

For example, typing tq(1960q2) is equivalent to typing 1.

Domain *l*: quarter literal strings 0100q1 to 9999q4

Range: e_q dates 0100q1 to 9999q4 (integers -7,440 to 32,159)

tw(l)

Description: convenience function to make typing weekly dates in expressions easier

For example, typing tw(1960w2) is equivalent to typing 1.

Domain l: week literal strings 0100w1 to 9999w52

Range: e_w dates 0100w1 to 9999w52 (integers -96,720 to 418,079)

 $week(e_d)$

Description: the numeric week of the year corresponding to date e_d , the "td encoded date

(days since 01jan1960)

Note: The first week of a year is the first 7-day period of the year. e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Domain e_d : e_d dates 01jan0100 to 31dec Range integers 1 to 52 or *missing*

weekly($s_1, s_2[,Y]$)

Description: the e_w weekly date (weeks since 1960w1) corresponding to s_1 based on s_2 and

Y; Y specifies topyear; see date()

Domain s_1 : strings

Domain s_2 : strings "WY" and "YW"; Y may be prefixed with ## Domain Y: integers 1000 to 9998 (but probably 2001 to 2099)

Range: e_w dates 0100w1 to 9999w52 (integers -96,720 to 418,079) or missing

 $\mathtt{wofd}(e_d)$

Description: the e_w weekly date (weeks since 1960w1) containing date e_d Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) e_w dates 0100w1 to 9999w52 (integers -96,720 to 418,079)

 $year(e_d)$

Description: the numeric year corresponding to date e_d

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Range: integers 0100 to 9999 (but probably 1800 to 2100)

 $\mathtt{yearly}(s_1, s_2[, Y])$

Description: The e_y yearly date (year) corresponding to s_1 based on s_2 and Y; Y specifies

topyear; see date()

Domain s_1 : strings

Domain s_2 : string "Y"; Y may be prefixed with ##

Domain Y: integers 1000 to 9998 (but probably 2001 to 2099)

Range: e_y dates 0100 to 9999 (integers 0100 to 9999) or missing

yh(Y, H)

Description: the e_h half-yearly date (half-years since 1960h1) corresponding to year Y, half-

year H

Domain Y: integers 1000 to 9999 (but probably 1800 to 2100)

Domain H: integers 1, 2

Range: e_h dates 1000h1 to 9999h2 (integers -1,920 to 16,079)

ym(Y, M)

Description: the e_m monthly date (months since 1960m1) corresponding to year Y, month M

Domain Y: integers 1000 to 9999 (but probably 1800 to 2100)

Domain M: integers 1 to 12

Range: e_m dates 1000m1 to 9999m12 (integers -11,520 to 96,479)

 $yofd(e_d)$

Description: the e_y yearly date (year) containing date e_d

Domain e_d : e_d dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

Range: e_y dates 0100 to 9999 (integers 0100 to 9999)

yq(Y,Q)

Description: the e_q quarterly date (quarters since 1960q1) corresponding to year Y, quarter Q

Domain Y: integers 1000 to 9999 (but probably 1800 to 2100)

Domain Q: integers 1 to 4

Range: e_q dates 1000q1 to 9999q4 (integers -3,840 to 32,159)

yw(Y,W)

Description: the e_w weekly date (weeks since 1960w1) corresponding to year Y, week W

Domain *Y*: integers 1000 to 9999 (but probably 1800 to 2100)

Domain W: integers 1 to 52

Range: e_w dates 1000w1 to 9999w52 (integers -49,920 to 418,079)

Remarks and examples

Stata's date and time functions are described with examples in [U] 25 Working with dates and times, [D] Datetime, [D] Datetime durations, and [D] Datetime relative dates.

Video example

How to create a date variable from a date stored as a string

Methods and formulas

The functions age() and age_frac() are based on datediff() and datediff_frac(), respectively,

 $\mathtt{age}(e_{d\, ext{DOB}},e_d,s_{nl}) = \mathtt{datediff}(e_{d\, ext{DOB}},e_d,\mathtt{"year"},s_{nl})$

$$age_frac(e_{dDOB}, e_d, s_{nl}) = datediff_frac(e_{dDOB}, e_d, "year", s_{nl})$$

when $e_d \ge e_{d \text{ DOB}}$. When $e_d < e_{d \text{ DOB}}$, age() and age_frac() return missing (.).

datediff(e_{d1} , e_{d2} , "year", s_{nl}) returns an integer that is the number of years between e_{d1} and e_{d2} . Assume $e_{d2} \ge e_{d1}$. If the month and day of e_{d2} are the same or after the month and day of e_{d1} , it returns year(e_{d2}) - year(e_{d1}). If the month and day of e_{d2} are before the month and day of e_{d1} , it returns year(e_{d2}) - year(e_{d1}) - 1.

If $e_{d2} < e_{d1}$, the result is calculated using

$$datediff(e_{d1}, e_{d2}, "year", s_{nl}) = -datediff(e_{d2}, e_{d1}, "year", s_{nl})$$

This formula also holds for units of "month" and "day" and for datediff_frac().

datediff $(e_{d1}, e_{d2}, "year", s_{nl})$ has an optional fourth argument, s_{nl} , that applies only to a starting date e_{d1} on 29feb when the ending date e_{d2} is not in a leap year. There are two possible values for s_{nl} : either "01mar" (with equivalents "1mar", "mar01", "mar1") or "28feb" ("feb28"). When "01mar" is specified and e_{d1} is on 29feb, datediff() increases by one in nonleap years when e_{d2} goes to 01mar. When "28feb" is specified and e_{d1} is on 29feb, it increases by one in nonleap years when e_{d2} goes to 28feb.

In other words, s_{nl} sets the anniversary date (or birthday) in nonleap years for starting dates (or dates of birth) on 29feb. When the fourth argument is omitted, it is as if "01mar" was specified.

Regardless of the value of s_{nl} , when e_{d1} is on 29feb, datediff(..., "year",...) increases by one in leap years when e_{d2} goes to 29feb.

datediff_frac(e_{d1} , e_{d2} ,"year", s_{nl}) is defined similarly. datediff_frac(...,"year",...) is exactly an integer and equal to datediff(...,"year",...) for days e_{d2} on which datediff() increases by one from the day previous to e_{d2} .

The fractional part of datediff_frac(e_{d1} , e_{d2} ,"year", s_{nl}) is calculated by first counting the number of days, d_1 , from the closest date prior to e_{d2} that has an exact integer value of datediff_frac(...,"year",...) to e_{d2} . Then number of the days, d_2 , from e_{d2} to the closest following date that has an exact integer value of datediff_frac() is determined. The fractional part is $d_1/(d_1+d_2)$, and d_1+d_2 is either 365 or 366.

For examples, see example 1 and example 3 in [D] **Datetime durations**.

datediff(e_{d1} , e_{d2} , "month", s_{nl}) and datediff_frac(e_{d1} , e_{d2} , "month", s_{nl}) follow the corresponding definitions with "year". datediff(..., "month",...) increases to an integer multiple of 12 when datediff(..., "year",...) increases by one from the day previous to e_{d2} . datediff_frac(..., "month",...) is exactly 12 times datediff_frac(..., "year",...) when datediff_frac(..., "year",...) is an integer.

datediff(e_{d1} , e_{d2} , "month", s_{nl}) increases by one from the day previous to e_{d2} when day(e_{d2}) = day(e_{d1}). If there is no day(e_{d1}) in the month, then it increases by one on the first day of the next month. For example, if e_{d1} is on 30aug, then datediff(..., "month",...) increases by one when e_{d2} goes to 30sep. If e_{d1} is on 31aug, then datediff(..., "month",...) increases by one when e_{d2} goes to 01oct.

The optional fourth argument, s_{nl} , again sets the date, either "01mar" or "28feb", when datediff(..., "month",...) increases by one when e_{d1} is on 29feb.

datediff_frac(..., "month",...) is defined like datediff_frac(..., "year",...). Days on which datediff_frac(..., "month",...) is an exact integer are determined, and the fractional part for other days is determined by interpolating between these days. The denominator of the fractional part is 28, 29, 30, or 31.

See example 2 of datediff() and datediff_frac() for months in [D] Datetime durations.

datediff(e_{d1} , e_{d2} , "day", s_{nl}) and datediff_frac(e_{d1} , e_{d2} , "day", s_{nl}) have no such complications. Both are equal to $e_{d2}-e_{d1}$ and are always integers. The optional fourth argument has no bearing on the calculation and is ignored.

clockdiff(e_{tc1}, e_{tc2}, s_u) and clockdiff_frac(e_{tc1}, e_{tc2}, s_u) take the difference $e_{tc2} - e_{tc1}$, which is in milliseconds, and converts the difference to the units specified by s_u , days ($24 \times 60 \times 60 \times 1000$ milliseconds), hours ($60 \times 60 \times 1000$ milliseconds), minutes (60×1000 milliseconds), or seconds (1000 milliseconds). clockdiff() rounds the result down to an integer, whereas clockdiff_frac() retains the fractional part of the difference.

Clockdiff(e_{tC1}, e_{tC2}, s_u) and Clockdiff_frac(e_{tC1}, e_{tC2}, s_u) are similar to clockdiff() and clockdiff_frac() except they are used with datetime/C values (times with leap seconds) rather than datetime/c values (times without leap seconds). In almost all cases, Clockdiff() and Clockdiff_frac() give the same results as clockdiff() and clockdiff_frac() with the datetime/C values converted to datetime/c values. They only differ when either or both of times e_{tC1} and e_{tC2} are close to a leap second and the units are days, hours, or minutes. By "close", we mean within a day, hour, or minute of the leap second, respectively, for the chosen unit, and less than or equal to the leap second.

Stata system file leapseconds.maint lists the dates on which leap seconds occurred. To view the file, type

. viewsource leapseconds.maint

For times close to leap seconds or times that are leap seconds, Clockdiff() and Clockdiff_frac() base their calculations on there being a minute consisting of 61 seconds, an hour of $60 \times 60 + 1 = 3,601$ seconds, and a day of $24 \times 60 \times 60 + 1 = 86,401$ seconds before the leap second (and including the leap second).

For example, 31dec2016 23:59:60 is a leap second, so the time difference between 31dec2016 23:59:00 and 01jan2017 00:00:00 is a minute that consists of 61 seconds. The time difference between $e_{tC1}=$ 31dec2016 23:59:00 and $e_{tC2}=$ 31dec2016 23:59:59 is 59 seconds. So Clockdiff_frac(e_{tC1} , e_{tC2} , "minute") = 59/61=0.9672 minute.

For times further away from the leap second, say, $e_{tC1} = 31 \text{dec}2016\ 23:58:00$ and $e_{tC2} = 01 \text{jan}2017\ 00:02:01$, having a leap second between these times has no effect on the result. In this case, Clockdiff_frac(e_{tC1} , e_{tC2} , "minute") = 4+1/60=4.0167 minutes. 01jan2017 00:02:00 is considered the "anniversary" minute of 31dec2016 23:58:00, so the difference between these times is exactly 4 minutes. Increasing the ending time by a second gives the result 4+1/60 minutes. This is, of course, the same result produced by clockdiff_frac(..., "minute") with the datetime/C values converted to datetime/c.

For units of days or hours, the logic of the calculation is similar. For units of seconds or milliseconds, the results are straightforward. The arguments e_{tC1} and e_{tC2} are numbers of milliseconds, so

Clockdiff_frac(
$$e_{tC1}$$
, e_{tC2} , "millisecond") = $e_{tC2} - e_{tC1}$

and

Clockdiff_frac(
$$e_{tC1}$$
, e_{tC2} , "second") = $(e_{tC2} - e_{tC1})/1000$

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Also see

- [FN] Functions by category
- [D] **Datetime** Date and time values and variables
- [D] **Datetime durations** Obtaining and working with durations
- [D] Datetime relative dates Obtaining dates and date information from other dates
- [D] egen Extensions to generate
- [D] **generate** Create or change contents of variable
- [M-5] **date**() Date and time manipulation
- [U] 13.3 Functions
- [U] 25 Working with dates and times

Mathematical functions

Contents Functions Video example References Also see

Contents

```
abs(x)
                                 the absolute value of x
ceil(x)
                                 the unique integer n such that n-1 < x \le n; x (not ".") if x is
                                    missing, meaning that ceil(.a) = .a
cloglog(x)
                                 the complementary log-log of x
comb(n,k)
                                 the combinatorial function n!/\{k!(n-k)!\}
digamma(x)
                                 the digamma() function, d \ln \Gamma(x)/dx
exp(x)
                                 the exponential function e^x
expm1(x)
                                 e^x - 1 with higher precision than \exp(x) - 1 for small values of
                                   |x|
floor(x)
                                 the unique integer n such that n \le x < n+1; x (not ".") if x is
                                    missing, meaning that floor(.a) = .a
int(x)
                                 the integer obtained by truncating x toward 0 (thus, int (5.2) = 5
                                    and int(-5.8) = -5); x (not ".") if x is missing, meaning
                                    that int(.a) = .a
                                 the inverse of the complementary log-log function of x
invcloglog(x)
invlogit(x)
                                 the inverse of the logit function of x
ln(x)
                                 the natural logarithm, ln(x)
ln1m(x)
                                 the natural logarithm of 1-x with higher precision than ln(1-x)
                                    for small values of |x|
ln1p(x)
                                 the natural logarithm of 1+x with higher precision than ln(1+x)
                                    for small values of |x|
lnfactorial(n)
                                 the natural log of n factorial = ln(n!)
lngamma(x)
                                ln{\Gamma(x)}
log(x)
                                 a synonym for ln(x)
log10(x)
                                 the base-10 logarithm of x
log1m(x)
                                 a synonym for ln1m(x)
log1p(x)
                                 a synonym for ln1p(x)
logit(x)
                                 the log of the odds ratio of x, logit(x) = \ln \{x/(1-x)\}\
\max(x_1, x_2, \ldots, x_n)
                                 the maximum value of x_1, x_2, \ldots, x_n
\min(x_1, x_2, \ldots, x_n)
                                 the minimum value of x_1, x_2, \ldots, x_n
mod(x,y)
                                 the modulus of x with respect to y
reldif(x,y)
                                 the "relative" difference |x-y|/(|y|+1); 0 if both arguments are
                                    the same type of extended missing value; missing if only one
                                    argument is missing or if the two arguments are two different
                                    types of missing
```

round(x,y) or round(x)x rounded in units of y or x rounded to the nearest integer if the argument y is omitted; x (not ".") if x is missing (meaning that round(.a) = .a and that round(.a, y) = .a if y is not missing) and if y is missing, then "." is returned the sign of x: -1 if x < 0, 0 if x = 0, 1 if x > 0, or missing if sign(x)x is missing sqrt(x)the square root of x sum(x)the running sum of x, treating missing values as zero the second derivative of $lngamma(x) = d^2 ln\Gamma(x)/dx^2$ trigamma(x)trunc(x)a synonym for int(x)**Functions** abs(x)Description: the absolute value of xDomain: -8e+307 to 8e+307Range: 0 to 8e+307

ceil(x)

Description: the unique integer n such that $n-1 < x \le n$; x (not ".") if x is missing, meaning

that ceil(.a) = .a

Also see floor(x), int(x), and round(x).

Domain: -8e+307 to 8e+307

Range: integers in -8e+307 to 8e+307

cloglog(x)

Description: the complementary log-log of x

 $cloglog(x) = ln\{-ln(1-x)\}\$

Domain: 0 to 1

Range: -8e+307 to 8e+307

comb(n,k)

Description: the combinatorial function $n!/\{k!(n-k)!\}$

Domain n: integers 1 to 1e+305 Domain k: integers 0 to n

Range: 0 to 8e+307 or missing

digamma(x)

Description: the digamma() function, $d \ln \Gamma(x)/dx$

This is the derivative of lngamma(x). The digamma(x) function is sometimes called

the psi function, $\psi(x)$.

Domain: -1e+15 to 8e+307

Range: -8e+307 to 8e+307 or missing

exp(x)

Description: the exponential function e^x

This function is the inverse of ln(x). To compute $e^x - 1$ with high precision for

small values of |x|, use expm1(x).

Domain: -8e+307 to 709 Range: 0 to 8e+307

expm1(x)

Description: $e^x - 1$ with higher precision than $\exp(x) - 1$ for small values of |x|

Domain: -8e+307 to 709 Range: -1 to 8e+307

floor(x)

Description: the unique integer n such that $n \le x < n+1$; x (not ".") if x is missing, meaning

that floor(.a) = .a

Also see ceil(x), int(x), and round(x).

Domain: -8e+307 to 8e+307

Range: integers in -8e+307 to 8e+307

int(x)

Description: the integer obtained by truncating x toward 0 (thus, int (5.2) = 5 and int (-5.8) =

-5); x (not ".") if x is missing, meaning that int(.a) = .a

One way to obtain the closest integer to x is int(x+sign(x)/2), which simplifies to int(x+0.5) for $x \ge 0$. However, use of the round() function is preferred. Also

see round(x), ceil(x), and floor(x).

Domain: -8e+307 to 8e+307

Range: integers in -8e+307 to 8e+307

invcloglog(x)

Description: the inverse of the complementary log-log function of x

 $invcloglog(x) = 1 - exp{-exp(x)}$

Domain: -8e+307 to 8e+307Range: 0 to 1 or *missing*

invlogit(x)

Description: the inverse of the logit function of x

 $invlogit(x) = exp(x)/\{1 + exp(x)\}$

Domain: -8e+307 to 8e+307 Range: 0 to 1 or *missing*

ln(x)

Description: the natural logarithm, ln(x)

This function is the inverse of exp(x). The logarithm of x in base b can be calculated

via $\log_b(x) = \log_a(x)/\log_a(b)$. Hence,

 $\begin{aligned} \log_5(x) &= \ln(x) / \ln(5) = \log(x) / \log(5) = \log(10(x) / \log(10(5)) \\ \log_2(x) &= \ln(x) / \ln(2) = \log(x) / \log(2) = \log(10(x) / \log(10(2)) \end{aligned}$

You can calculate $\log_b(x)$ by using the formula that best suits your needs. To compute $\ln(1-x)$ and $\ln(1+x)$ with high precision for small values of |x|, use $\ln \ln(x)$

and ln1p(x), respectively.

Domain: 1e–323 to 8e+307 Range: -744 to 709

ln1m(x)

Description: the natural logarithm of 1-x with higher precision than ln(1-x) for small values

of |x|

Domain: -8e+307 to 1-c (epsdouble)

Range: -37 to 709

ln1p(x)

Description: the natural logarithm of 1+x with higher precision than ln(1+x) for small values

of |x|

Domain: -1 + c(epsdouble) to 8e+307

Range: -37 to 709

lnfactorial(n)

Description: the natural log of n factorial = ln(n!)

To calculate n!, use round(exp(lnfactorial(n)),1) to ensure that the result is an integer. Logs of factorials are generally more useful than the factorials themselves

because of overflow problems.

Domain: integers 0 to 1e+305

Range: 0 to 8e+307

lngamma(x)

Description: $ln{\Gamma(x)}$

Here the gamma function, $\Gamma(x)$, is defined by $\Gamma(x) = \int_0^\infty t^{x-1} e^{-t} dt$. For integer values of x > 0, this is $\ln((x-1)!)$

values of x > 0, this is ln((x-1)!).

 $\operatorname{Ingamma}(x)$ for x < 0 returns a number such that $\exp(\operatorname{Ingamma}(x))$ is equal to the absolute value of the gamma function, $\Gamma(x)$. That is, $\operatorname{Ingamma}(x)$ always returns

a real (not complex) result.

Domain: -2,147,483,648 to 1e+305 (excluding negative integers)

Range: -8e+307 to 8e+307

log(x)

Description: a synonym for ln(x)

```
Description: the base-10 logarithm of x
   Domain:
               1e-323 to 8e+307
   Range:
               -323 to 308
log1m(x)
   Description: a synonym for ln1m(x)
log1p(x)
   Description: a synonym for ln1p(x)
logit(x)
   Description: the log of the odds ratio of x, logit(x) = \ln \{x/(1-x)\}\
   Domain:
               0 to 1 (exclusive)
               -8e+307 to 8e+307 or missing
   Range:
\max(x_1, x_2, \ldots, x_n)
   Description: the maximum value of x_1, x_2, \ldots, x_n
               Unless all arguments are missing, missing values are ignored.
               \max(2,10,..,7) = 10
               \max(.,.,.) = .
   Domain x_1: -8e+307 to 8e+307 or missing
   Domain x_2: -8e+307 to 8e+307 or missing
   Domain x_n: -8e+307 to 8e+307 or missing
               -8e+307 to 8e+307 or missing
   Range:
\min(x_1, x_2, \ldots, x_n)
   Description: the minimum value of x_1, x_2, \ldots, x_n
               Unless all arguments are missing, missing values are ignored.
               min(2,10,.,7) = 2
               min(.,.,.) = .
   Domain x_1: -8e+307 to 8e+307 or missing
   Domain x_2: -8e+307 to 8e+307 or missing
   Domain x_n: -8e+307 to 8e+307 or missing
               -8e+307 to 8e+307 or missing
   Range:
```

log10(x)

mod(x,y)

Description: the modulus of x with respect to y

mod(x,y) = x - y floor(x/y)

mod(x,0) = .

Domain x: -8e+307 to 8e+307

Domain *y*: 0 to 8e+307 Range: 0 to 8e+307

reldif(x,y)

Description: the "relative" difference |x-y|/(|y|+1); 0 if both arguments are the same type

of extended missing value; missing if only one argument is missing or if the two

arguments are two different types of missing

Domain x: -8e+307 to 8e+307 or missing Domain y: -8e+307 to 8e+307 or missing

Range: 0 to 8e+307 or missing

round(x,y) or round(x)

Description: x rounded in units of y or x rounded to the nearest integer if the argument y is omitted; x (not ".") if x is missing (meaning that round(.a) = .a and that round(.a, y) = .a if y is not missing) and if y is missing, then "." is returned

For y=1, or with y omitted, this amounts to the closest integer to x; round (5.2,1) is 5, as is round (4.8,1); round (-5.2,1) is -5, as is round (-4.8,1). The rounding definition is generalized for $y \neq 1$. With y=0.01, for instance, x is rounded to two decimal places; round (sqrt(2),.01) is 1.41. y may also be larger than 1; round (28,5) is 30, which is 28 rounded to the closest multiple of 5. For y=0, the function is defined as returning x unmodified.

For values of x exactly at midpoints, where it may not be clear whether to round up or down, x is always rounded up to the larger value. For example, round (4.5) is 5 and round (-4.5) is -4. Note that rounding a number is based on the floating-point number representation of the number instead of the number itself. So round () is sensitive to representation errors and precision limits. For example, 0.15 has no exact floating-point number representation. Therefore, round (0.15,0.1) is 0.1 instead of 0.2. See [U] 13.12 Precision and problems therein for details.

Also see int(x), ceil(x), and floor(x).

Domain x: -8e+307 to 8e+307Domain y: -8e+307 to 8e+307Range: -8e+307 to 8e+307

sign(x)

Description: the sign of x: -1 if x < 0, 0 if x = 0, 1 if x > 0, or missing if x is missing

Domain: -8e+307 to 8e+307 or missing

Range: -1, 0, 1 or missing

sqrt(x)

Description: the square root of x

Domain: 0 to 8e+307 Range: 0 to 1e+154

sum(x)

Description: the running sum of x, treating missing values as zero

For example, following the command generate y=sum(x), the jth observation on y contains the sum of the first through jth observations on x. See [D] **egen** for an alternative sum function, total(), that produces a constant equal to the overall sum.

Domain: all real numbers or missing

Range: -8e+307 to 8e+307 (excluding *missing*)

trigamma(x)

Description: the second derivative of $lngamma(x) = d^2 ln\Gamma(x)/dx^2$

The trigamma() function is the derivative of digamma(x).

Domain: -1e+15 to 8e+307Range: 0 to 8e+307 or missing

trunc(x)

Description: a synonym for int(x)

Video example

How to round a continuous variable

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Also see

- [FN] Functions by category
- [D] egen Extensions to generate
- [D] generate Create or change contents of variable
- [M-4] Intro Categorical guide to Mata functions
- [U] 13.3 Functions

Matrix functions

Contents Functions Reference Also see

Contents

$\operatorname{cholesky}(M)$	the Cholesky decomposition of the matrix: if $R = \text{cholesky}(S)$, then $RR^T = S$
$\mathtt{coleqnumb}(M,s)$	the equation number of M associated with column equation s ; missing if the column equation cannot be found
$\mathtt{colnfreeparms}(M)$	the number of free parameters in columns of M
$\mathtt{colnumb}(M,s)$	the column number of M associated with column name s ; missing if the column cannot be found
${\tt colsof}(M)$	the number of columns of M
$\mathtt{corr}(M)$	the correlation matrix of the variance matrix
$\det(M)$	the determinant of matrix M
$\mathtt{diag}(M)$	the square, diagonal matrix created from the row or column vector
${\tt diag0cnt}(M)$	the number of zeros on the diagonal of M
el(s,i,j)	s[floor(i),floor(j)], the i,j element of the matrix named s ; missing if i or j are out of range or if matrix s does not exist
<pre>get(systemname)</pre>	a copy of Stata internal system matrix systemname
${\tt hadamard}(M,N)$	a matrix whose i , j element is $M[i,j] \cdot N[i,j]$ (if M and N are not the same size, this function reports a conformability error)
I(n)	an $n \times n$ identity matrix if n is an integer; otherwise, a round(n) \times round(n) identity matrix
$\mathtt{inv}(M)$	the inverse of the matrix M
$\mathtt{invsym}(M)$	the inverse of M if M is positive definite
$\mathtt{invvech}(M)$	a symmetric matrix formed by filling in the columns of the lower triangle from a row or column vector
invvecp(M)	a symmetric matrix formed by filling in the columns of the upper triangle from a row or column vector
${ t issymmetric}(M)$	1 if the matrix is symmetric; otherwise, 0
J(r,c,z)	the $r \times c$ matrix containing elements z
$\mathtt{matmissing}(M)$	1 if any elements of the matrix are missing; otherwise, 0
$\mathtt{matuniform}(r,c)$	the $r \times c$ matrices containing uniformly distributed pseudorandom numbers on the interval $(0,1)$
mreldif(X,Y)	the relative difference of X and Y , where the relative difference is defined as $\max_{i,j}\{ x_{ij}-y_{ij} /(y_{ij} +1)\}$
<pre>nullmat(matname)</pre>	use with the row-join (,) and column-join (\) operators
${\tt roweqnumb}(M,s)$	the equation number of M associated with row equation $s;$ missing if the row equation cannot be found
${\tt rownfreeparms}(M)$	the number of free parameters in rows of M
$\mathtt{rownumb}(M,s)$	the row number of M associated with row name s ; missing if the row cannot be found

${ t rowsof}(M)$	the number of rows of M
${\tt sweep}(M,i)$	matrix M with i th row/column swept
trace(M)	the trace of matrix M
vec(M)	a column vector formed by listing the elements of M , starting with the first column and proceeding column by column
$\mathtt{vecdiag}(M)$	the row vector containing the diagonal of matrix M
$\operatorname{\mathtt{vech}}(M)$	a column vector formed by listing the lower triangle elements of M
vecp(M)	a column vector formed by listing the upper triangle elements of

Functions

We divide the basic matrix functions into two groups, according to whether they return a matrix or a scalar:

Matrix functions returning a matrix Matrix functions returning a scalar

Matrix functions returning a matrix

In addition to the functions listed below, see [P] matrix svd for singular value decomposition, [P] matrix symeigen for eigenvalues and eigenvectors of symmetric matrices, and [P] matrix eigenvalues for eigenvalues of nonsymmetric matrices.

cholesky(M)

Description: the Cholesky decomposition of the matrix: if R = cholesky(S), then $RR^T = S$

 \mathbb{R}^T indicates the transpose of \mathbb{R} . Row and column names are obtained from M.

Domain: $n \times n$, positive-definite, symmetric matrices

Range: $n \times n$ lower-triangular matrices

corr(M)

Description: the correlation matrix of the variance matrix

Row and column names are obtained from M.

Domain: $n \times n$ symmetric variance matrices Range: $n \times n$ symmetric correlation matrices

diag(M)

Description: the square, diagonal matrix created from the row or column vector

Row and column names are obtained from the column names of M if M is a row

vector or from the row names of M if M is a column vector. $1\times n$ and $n\times 1$ vectors

Domain: $1 \times n$ and $n \times 1$ vectors Range: $n \times n$ diagonal matrices

get(systemname)

Description: a copy of Stata internal system matrix systemname

This function is included for backward compatibility with previous versions of Stata.

Domain: existing names of system matrices

Range: matrices

hadamard(M,N)

Description: a matrix whose i, j element is $M[i, j] \cdot N[i, j]$ (if M and N are not the same size,

this function reports a conformability error)

Domain M: $m \times n$ matrices Domain N: $m \times n$ matrices Range: $m \times n$ matrices

I(n)

Description: an $n \times n$ identity matrix if n is an integer; otherwise, a round(n) \times round(n)

identity matrix

Domain: real scalars 1 to c(max_matdim)

Range: identity matrices

inv(M)

Description: the inverse of the matrix M

If M is singular, this will result in an error.

The function invsym() should be used in preference to inv() because invsym() is more accurate. The row names of the result are obtained from the column names of M, and the column names of the result are obtained from the row names of M.

Domain: $n \times n$ nonsingular matrices

Range: $n \times n$ matrices

invsym(M)

Description: the inverse of M if M is positive definite

If M is not positive definite, rows will be inverted until the diagonal terms are zero or negative; the rows and columns corresponding to these terms will be set to 0, producing a g2 inverse. The row names of the result are obtained from the column names of M, and the column names of the result are obtained from the row names

of M.

Domain: $n \times n$ symmetric matrices Range: $n \times n$ symmetric matrices

invvech(M)

Description: a symmetric matrix formed by filling in the columns of the lower triangle from a

row or column vector

Domain: $n(n+1)/2 \times 1$ and $1 \times n(n+1)/2$ vectors

Range: $n \times n$ matrices

invvecp(M)

Description: a symmetric matrix formed by filling in the columns of the upper triangle from a

row or column vector

Domain: $n(n+1)/2 \times 1$ and $1 \times n(n+1)/2$ vectors

Range: $n \times n$ matrices

J(r,c,z)

Description: the $r \times c$ matrix containing elements z Domain r: integer scalars 1 to c(max_matdim)

Domain c: integer scalars 1 to c(max_matdim)

Domain z: scalars -8e+307 to 8e+307

Range: $r \times c$ matrices

matuniform(r,c)

Description: the $r \times c$ matrices containing uniformly distributed pseudorandom numbers on the

interval (0,1)

Domain r: integer scalars 1 to c(max_matdim)
Domain c: integer scalars 1 to c(max_matdim)

Range: $r \times c$ matrices

nullmat(matname)

Description: use with the row-join (,) and column-join (\) operators

Consider the following code fragment, which is an attempt to create the vector (1, 2, 3, 4):

The above program will not work because, the first time through the loop, v will not yet exist, and thus forming (v, 'i') makes no sense. nullmat() relaxes that restriction:

```
forvalues i = 1/4 {
    mat v = (nullmat(v), 'i')
}
```

The nullmat() function informs Stata that if v does not exist, the function row-join is to be generalized. Joining nothing with 'i' results in ('i'). Thus the first time through the loop, v = (1) is formed. The second time through, v does exist, so v = (1, 2) is formed, and so on.

nullmat() can be used only with the , and \ operators.

Domain: matrix names, existing and nonexisting

Range: matrices including null if matname does not exist

sweep(M,i)

Description: matrix M with ith row/column swept

The row and column names of the resultant matrix are obtained from M, except that the nth row and column names are interchanged. If B = sweep(A, k), then

$$B_{kk} = \frac{1}{A_{kk}}$$

$$B_{ik} = -\frac{A_{ik}}{A_{kk}}, \quad i \neq k$$

$$B_{kj} = \frac{A_{kj}}{A_{kk}}, \quad j \neq k$$

$$B_{ij} = A_{ij} - \frac{A_{ik}A_{kj}}{A_{kk}}, \quad i \neq k, j \neq k$$

Domain M: $n \times n$ matrices Domain i: integer scalars 1 to nRange: $n \times n$ matrices

vec(M)

Description: a column vector formed by listing the elements of M, starting with the first column

and proceeding column by column

Domain: matrices

Range: column vectors ($n \times 1$ matrices)

vecdiag(M)

Description: the row vector containing the diagonal of matrix M

vecdiag() is the opposite of diag(). The row name is set to r1; the column names

are obtained from the column names of M.

Domain: $n \times n$ matrices Range: $1 \times n$ vectors

vech(M)

Description: a column vector formed by listing the lower triangle elements of M

Domain: $n \times n$ matrices

Range: $n(n+1)/2 \times 1$ vectors

vecp(M)

Description: a column vector formed by listing the upper triangle elements of M

Domain: $n \times n$ matrices

Range: $n(n+1)/2 \times 1$ vectors

Matrix functions returning a scalar

coleqnumb(M,s)

Description: the equation number of M associated with column equation s; missing if the column

equation cannot be found

Domain M: matrices Domain s: strings

Range: integer scalars 1 to c(max_matdim) or missing

colnfreeparms(M)

Description: the number of free parameters in columns of M

Domain: matrices

Range: integer scalars 0 to c(max_matdim)

colnumb(M,s)

Description: the column number of M associated with column name s; missing if the column

cannot be found

Domain M: matrices
Domain s: strings

Range: integer scalars 1 to c(max_matdim) or missing

colsof(M)

Description: the number of columns of M

Domain: matrices

Range: integer scalars 1 to c(max_matdim)

det(M)

Description: the determinant of matrix MDomain: $n \times n$ (square) matrices Range: scalars -8e+307 to 8e+307

diag0cnt(M)

Description: the number of zeros on the diagonal of M

Domain: $n \times n$ (square) matrices Range: integer scalars 0 to n

el(s,i,j)

Description: s[floor(i), floor(j)], the i, j element of the matrix named s; missing if i or j

are out of range or if matrix s does not exist

Domain s: strings containing matrix name Domain i: scalars 1 to c(max_matdim) Domain j: scalars 1 to c(max_matdim)

Range: scalars -8e+307 to 8e+307 or missing

issymmetric(M)

Description: 1 if the matrix is symmetric; otherwise, 0

Domain M: matrices

Range: integers 0 and 1

matmissing(M)

Description: 1 if any elements of the matrix are missing; otherwise, 0

Domain M: matrices

Range: integers 0 and 1

mreldif(X,Y)

Description: the relative difference of X and Y, where the relative difference is defined as

 $\max_{i,j} \{ |x_{ij} - y_{ij}|/(|y_{ij}| + 1) \}$

Domain X: matrices

Domain Y: matrices with same number of rows and columns as X

Range: scalars -8e+307 to 8e+307

roweqnumb(M,s)

Description: the equation number of M associated with row equation s; missing if the row equation

cannot be found

Domain M: matrices Domain s: strings

Range: integer scalars 1 to c(max_matdim) or missing

rownfreeparms(M)

Description: the number of free parameters in rows of M

Domain: matrices

Range: integer scalars 0 to c(max_matdim)

rownumb(M,s)

Description: the row number of M associated with row name s; missing if the row cannot be

found

Domain M: matrices Domain s: strings

Range: integer scalars 1 to c(max_matdim) or missing

rowsof(M)

Description: the number of rows of M

Domain: matrices

Range: integer scalars 1 to c(max_matdim)

trace(M)

Description: the trace of matrix MDomain: $n \times n$ (square) matrices Range: scalars -8e+307 to 8e+307

Jacques Salomon Hadamard (1865-1963) was born in Versailles, France. He had a tumultuous childhood, eating elephant meat to survive and enduring the premature deaths of two younger sisters. Hadamard taught while working on his doctorate, which he obtained in 1892 from École Normale Supérieure. His dissertation is recognized as the first examination of singularities. Hadamard published a paper on the Riemann zeta function, for which he was awarded the Grand Prix des Sciences Mathématiques in 1892. Shortly after, he became a professor at the University of Bordeaux and made many significant contributions over the course of four years. For example, in 1893 he published a paper on determinant inequalities, giving rise to Hadamard matrices. Then in 1896, he used complex analysis to prove the prime number theorem, and he was awarded the Bordin Prize by the Academy of Sciences for his work on dynamic trajectories. In the following years, he published books on two-dimensional and three-dimensional geometry, as well as an influential paper on functional analysis. He was elected to presidency of the French Mathematical Society in 1906 and as chair of mechanics at the Collège de France in 1909. Faced with the tragic deaths of two of his sons during World War I, Hadamard buried himself in his work. He continued to publish outstanding work in new areas, including probability theory, education, and psychology. In 1956, he was awarded the CNRS Gold Medal for his many contributions.

Reference

Mazýa, V. G., and T. O. Shaposhnikova. 1998. *Jacques Hadamard, A Universal mathematician*. Providence, RI: American Mathematical Society.

Also see

- [FN] Functions by category
- [D] **egen** Extensions to generate
- [D] generate Create or change contents of variable
- [M-4] **Intro** Categorical guide to Mata functions
- [U] 13.3 Functions
- [U] 14.8 Matrix functions

Programming functions

Contents Functions References Also see

Contents

$autocode(x,n,x_0,x_1)$	partitions the interval from x_0 to x_1 into n equal-length intervals and returns the upper bound of the interval that contains x or the upper bound of the first or last interval if $x < x_0$ or $x > x_1$, respectively
byteorder()	1 if your computer stores numbers by using a hilo byte order and evaluates to 2 if your computer stores numbers by using a lohi byte order
c(name)	the value of the system or constant result c(name) (see [P] creturn)
_caller()	version of the program or session that invoked the currently running program; see [P] version
$chop(x, \epsilon)$	round(x) if $abs(x - round(x)) < \epsilon$; otherwise, x; or x if x is missing
clip(x,a,b)	x if $a < x < b$, b if $x \ge b$, a if $x \le a$, or missing if x is missing or if $a > b$; x if x is missing
cond(x,a,b[,c])	a if x is true and nonmissing, b if x is false, and c if x is missing; a if c is not specified and x evaluates to missing
e(name)	the value of stored result e(name); see [U] 18.8 Accessing results calculated by other programs
e(sample)	1 if the observation is in the estimation sample and 0 otherwise
epsdouble()	the machine precision of a double-precision number
epsfloat()	the machine precision of a floating-point number
${\tt fileexists}(f)$	1 if the file specified by f exists; otherwise, 0
fileread(f)	the contents of the file specified by f
filereaderror(s)	0 or positive integer, said value having the interpretation of a return code
filewrite(f,s[,r])	writes the string specified by s to the file specified by f and returns the number of bytes in the resulting file
float(x)	the value of x rounded to float precision
<pre>fmtwidth(fmtstr)</pre>	the output length of the \%fmt contained in fmtstr; missing if fmtstr does not contain a valid \%fmt
frval()	returns values of variables stored in other frames
_frval()	programmer's version of frval()
has_eprop(name)	1 if name appears as a word in e(properties); otherwise, 0
inlist(z,a,b,)	1 if z is a member of the remaining arguments; otherwise, 0
inrange(z,a,b)	1 if it is known that $a \le z \le b$; otherwise, 0
$irecode(x, x_1, \ldots, x_n)$	missing if x is missing or x_1,\ldots,x_n is not weakly increasing; 0 if $x \leq x_1$; 1 if $x_1 < x \leq x_2$; 2 if $x_2 < x \leq x_3$;; n if $x > x_n$

```
matrix(exp)
maxbyte()
maxdouble()
maxfloat()
maxint()
maxlong()
\min(x_1, x_2, \ldots, x_n)
minbyte()
mindouble()
minfloat()
minint()
minlong()
missing(x_1, x_2, \ldots, x_n)
r(name)
recode(x, x_1, \ldots, x_n)
replay()
return(name)
s(name)
scalar(exp)
smallestdouble()
```

```
restricts name interpretation to scalars and matrices; see scalar()
the largest value that can be stored in storage type byte
the largest value that can be stored in storage type double
the largest value that can be stored in storage type float
the largest value that can be stored in storage type int
the largest value that can be stored in storage type long
a synonym for missing (x_1, x_2, \ldots, x_n)
the smallest value that can be stored in storage type byte
the smallest value that can be stored in storage type double
the smallest value that can be stored in storage type float
the smallest value that can be stored in storage type int
the smallest value that can be stored in storage type long
1 if any x_i evaluates to missing; otherwise, 0
the value of the stored result r(name); see [U] 18.8 Accessing
   results calculated by other programs
missing if x_1, x_2, \dots, x_n is not weakly increasing; x if x is missing;
   x_1 if x \leq x_1; x_2 if x \leq x_2, ...; otherwise, x_n if x > x_1, x_2,
   \dots, x_{n-1}. x_i \ge 1 is interpreted as x_i = +\infty
1 if the first nonblank character of local macro '0' is a comma, or
   if '0' is empty
the value of the to-be-stored result r(name); see [P] return
the value of stored result s (name); see [U] 18.8 Accessing results
   calculated by other programs
restricts name interpretation to scalars and matrices
the smallest double-precision number greater than zero
```

Functions

 $autocode(x,n,x_0,x_1)$

Description:

partitions the interval from x_0 to x_1 into n equal-length intervals and returns the upper bound of the interval that contains x or the upper bound of the first or last interval if $x < x_0$ or $x > x_1$, respectively

This function is an automated version of recode(). See [U] 26 Working with categorical data and factor variables for an example.

```
The algorithm for autocode() is  \text{if } (n \geq . \mid x_0 \geq . \mid x_1 \geq . \mid n \leq 0 \mid x_0 \geq x_1) \\ \text{then return } \underset{\text{missing}}{\text{missing}} \\ \text{if } x \geq ., \text{ then return } x \\ \text{otherwise} \\ \text{for } i = 1 \text{ to } n-1 \\ xmap = x_0 + i * (x_1 - x_0)/n
```

if $x \le xmap$ then return xmap end otherwise return x_1

return

Domain x: -8e+307 to 8e+307Domain n: integers 1 to 10,000 Domain x_0 : -8e+307 to 8e+307Domain x_1 : x_0 to 8e+307Range: x_0 to x_1

byteorder()

Description:

1 if your computer stores numbers by using a hilo byte order and evaluates to 2 if your computer stores numbers by using a lohi byte order

Consider the number 1 written as a 2-byte integer. On some computers (called hilo), it is written as "00 01", and on other computers (called lohi), it is written as "01 00" (with the least significant byte written first). There are similar issues for 4-byte integers, 4-byte floats, and 8-byte floats. Stata automatically handles byte-order differences for Stata-created files. Users need not be concerned about this issue. Programmers producing custom binary files can use byteorder() to

determine the native byte ordering; see [P] file.

Range: 1 and 2

c(name)

Description: the value of the system or constant result c(name) (see [P] creturn)

Referencing c(name) will return an error if the result does not exist.

Domain: names

Range: real values, strings, or missing

_caller()

Description: version of the program or session that invoked the currently running program;

see [P] version

This is a function for use by programmers.

Range: 1 to 18.0 (or 1 to 18.5 for StataNow)

 $chop(x, \epsilon)$

Description: round(x) if $abs(x - round(x)) < \epsilon$; otherwise, x; or x if x is missing

Domain x: -8e+307 to 8e+307Domain ϵ : -8e+307 to 8e+307Range: -8e+307 to 8e+307

clip(x,a,b)

Description: x if a < x < b, b if $x \ge b$, a if $x \le a$, or missing if x is missing or if a > b; $x \le a$

if x is missing

If a or b is missing, this is interpreted as $a = -\infty$ or $b = +\infty$, respectively.

Domain *x*: -8e+307 to 8e+307 Domain *a*: -8e+307 to 8e+307 Domain *b*: -8e+307 to 8e+307 Range: -8e+307 to 8e+307

cond(x,a,b[,c])

Description: a if x is true and nonmissing, b if x is false, and c if x is missing; a if c is not

specified and x evaluates to missing

Note that expressions such as x > 2 will never evaluate to missing.

cond(x>2,50,70) returns 50 if x>2 (includes $x \ge .$) cond(x>2,50,70) returns 70 if x<2

If you need a case for missing values in the above examples, try

cond(missing(x), ., cond(x>2,50,70)) returns . if x is missing, returns 50 if x > 2, and returns 70 if x < 2

If the first argument is a scalar that may contain a missing value or a variable containing missing values, the fourth argument has an effect.

cond(wage,1,0,.) returns 1 if wage is not zero and not missing

cond(wage,1,0,.) returns 0 if wage is zero
cond(wage,1,0,.) returns . if wage is missing

Caution: If the first argument to cond() is a logical expression, that is,

cond(x>2,50,70,.), the fourth argument is never reached.

Domain x: -8e+307 to 8e+307 or missing; $0 \Rightarrow false$, otherwise interpreted as true

Domain a: numbers and strings

Domain b: numbers if a is a number; strings if a is a string Domain c: numbers if a is a number; strings if a is a string

Range: a, b, and c

e(name)

Description: the value of stored result e(name); see [U] 18.8 Accessing results calculated by

other programs

e(name) = scalar missing if the stored result does not exist
 e(name) = specified matrix if the stored result is a matrix
 e(name) = scalar numeric value if the stored result is a scalar

Domain: names

Range: strings, scalars, matrices, or missing

e(sample)

Description: 1 if the observation is in the estimation sample and 0 otherwise

Range: 0 and 1

epsdouble()

Description: the machine precision of a double-precision number

If d < epsdouble() and (double) x = 1, then x + d = (double) 1. This function

takes no arguments, but the parentheses must be included.

Range: a double-precision number close to 0

epsfloat()

Description: the machine precision of a floating-point number

If d < epsfloat() and (float) x = 1, then x + d = (float) 1. This function takes

no arguments, but the parentheses must be included.

Range: a floating-point number close to 0

fileexists(f)

Description: 1 if the file specified by f exists; otherwise, 0

If the file exists but is not readable, fileexists() will still return 1, because it

does exist. If the "file" is a directory, fileexists() will return 0.

Domain: filenames

Range: 0 and 1

fileread(f)

Description: the contents of the file specified by f

If the file does not exist or an I/O error occurs while reading the file, then

"fileread() error #" is returned, where # is a standard Stata error return code.

Domain: filenames Range: strings

filereaderror(s)

Description: 0 or positive integer, said value having the interpretation of a return code

It is used like this

- . generate strL s = fileread(filename) if fileexists(filename)
- . assert filereaderror(s)==0

or this

- . generate strL s = fileread(filename) if fileexists(filename)
- . generate rc = filereaderror(s)

That is, filereaderror(s) is used on the result returned by fileread(filename) to determine whether an I/O error occurred.

In the example, we only fileread() files that fileexists(). That is not required. If the file does not exist, that will be detected by filereaderror() as an error. The way we showed the example, we did not want to read missing files as errors. If we wanted to treat missing files as errors, we would have coded

- . generate strL s = fileread(filename)
- . assert filereaderror(s)==0

or

- . generate strL s = fileread(filename)
- . generate rc = filereaderror(s)

Domain: strings Range: integers

filewrite(f,s[,r])

Description:

writes the string specified by s to the file specified by f and returns the number of bytes in the resulting file

If the optional argument r is specified as 1, the file specified by f will be replaced if it exists. If r is specified as 2, the file specified by f will be appended to if it exists. Any other values of r are treated as if r were not specified; that is, f will only be written to if it does not already exist.

When the file f is freshly created or is replaced, the value returned by filewrite() is the number of bytes written to the file, strlen(s). If r is specified as 2, and thus filewrite() is appending to an existing file, the value returned is the total number of bytes in the resulting file; that is, the value is the sum of the number of the bytes in the file as it existed before filewrite() was called and the number of bytes newly written to it, strlen(s).

If the file exists and r is not specified as 1 or 2, or an error occurs while writing to the file, then a negative number (#) is returned, where abs(#) is a standard Stata error return code.

Domain f: filenames
Domain s: strings

Domain r: integers 1 or 2

Range: integers

float(x)

Description: the value of x rounded to float precision

Although you may store your numeric variables as byte, int, long, float, or double, Stata converts all numbers to double before performing any calculations. Consequently, difficulties can arise in comparing numbers that have no finite binary representation.

For example, if the variable x is stored as a float and contains the value 1.1 (a repeating "decimal" in binary), the expression x==1.1 will evaluate to false because the literal 1.1 is the double representation of 1.1, which is different from the float representation stored in x. (They differ by 2.384×10^{-8} .) The expression x==float(1.1) will evaluate to true because the float() function converts the literal 1.1 to its float representation before it is compared with x. (See [U] 13.12 Precision and problems therein for more information.)

Domain: -1e+38 to 1e+38 Range: -1e+38 to 1e+38

fmtwidth(fmtstr)

Description: the output length of the \(\frac{1}{2} fmt \) contained in \(fmtstr \); \(missing \) if \(fmtstr \) does not contain

a valid %fmt

For example, fmtwidth("%9.2f") returns 9 and fmtwidth("%tc") returns 18.

Range: strings

frval(lvar, var)

Description: returns values of variables stored in other frames

The frame functions frval() and _frval() access values of variables in frames outside the current frame. If you do not know what a frame is, see [D] frames intro.

The two functions do the same thing, but frval() is easier to use, and it is safer. _frval() is a programmer's function.

lvar is the name of a variable created by frlink that links the current frame to another frame.

var is the name of a variable in the other frame.

Returned is the value of *var* from the observation in the other frame that matches the observation in the current frame.

Example 1: The current frame contains data on persons. Among the variables in the current frame is countyid containing the county in which each person lives.

Frame frounty contains data on counties. In these data, variable countyid also records the county's ID, and the other variables record county characteristics.

In the current frame, you have previously created variable linkcnty that links the current frame to frounty. You did this by typing

. frlink m:1 countyid, frame(frcounty) generate(linkcnty)

Thus, you can now type

. generate rel_income = income / frval(linkcnty, median_income)

income is an existing variable in the current frame. median_income is an existing variable in frcounty. rel_income will be a new variable in the current frame, containing the income of each person divided by the median income of the county in which they live.

Example 2: It is usual to name frames after dataset names and to name link variables after frame names. Here is an example of this, following the names used above:

. use persons, clear

. frame create county

. frame county: use county

. frlink m:1 countyid, frame(county)

. generate rel_income = income / frval(county, median_income)

Domain *lvar*:

the name of a variable created by frlink that links the current frame to another

frame

Domain *var*:

any variable (string or numeric) in the frame to which lvar links; varname

abbreviation is allowed

Range:

range of *var*, plus missing value (missing value is defined as . when *var* contains numeric data and "" when *var* contains string data; missing value is returned for observations in the current frame that are unmatched in the other frame)

frval(lvar, var, unm)

Description: the frval() function described above but with a third argument unm

frval() returns the value of *var* from the observation in the frame linked using *lvar* that matches the observation in the current frame and the value in *unm* if there is no matching observation.

For example, type

. generate median_inc = frval(county, median_income, .a)

to create new variable median_inc in the current frame, containing median_income from the other frame, or .a when there is no matched observation in the other frame.

Domain lvar: the name of a variable created by frlink that links the current frame to another

Domain var:

any variable (string or numeric) in the frame to which *lvar* links; varname

abbreviation is allowed

Domain *unm*: any numeric value if var is numeric; any string value when var is string

Range: range of var, plus unm

_frval(frm, var, i)

Description: programmer's version of frval()

It is useful for those wishing to write their own frlink and create special (or at least different) effects.

_frval() returns values of variables stored in other frames. It returns var's ith observation (var[i]) from the frame frm; see [D] **frames intro**.

If i is outside the valid range of observations for the frame, $_frval()$ returns missing.

For example, you have two datasets in memory. The current frame is named default and contains 57 observations. The other dataset, we will assume, is stored in frame xdata. It contains different variables but on the same 57 observations. The two datasets are in the same order so that observation 1 in default corresponds to observation 1 in xdata, observation 2 to observation 2, and so on. You can type

. generate hrlywage = income / _frval(xdata, hrswrked, _n)

This will divide values of income stored in default by values of hrswrked stored in xdata.

The first thing to notice is that _frval()'s first two arguments are not expressions. You just type the name of the frame and the name of the variable without embedding them in quotes. We specified xdata for the frame name and and hrswrked for the variable name.

The second thing to notice is that the third argument is an expression. To emphasize that, let's change the example. Assume that xdata contains 58 instead of 57 observations. Assume that observation 1 in default corresponds to observation 2 in xdata, observation 2 corresponds to observation 3, and so on. There is no observation in default that corresponds to observation 1 in xdata. In this case, you type

. generate hrlywage = income / _frval(xdata, hrswrked, _n+1)

These examples are artificial. You will normally use <u>frval()</u> by creating a variable in default that contains the corresponding observation numbers in xdata. If the variable were called xobsno, then in the first example, xobsno would contain 1, 2, ..., 57.

In the second example, xobsno would contain 2, 3, ..., 58.

In another example, xobsno might contain 9, 6, ..., 32, which is to say, the numbers 2, 3, ..., 58, but permuted to reflect the datasets' jumbled order.

In yet another example, xobsno might contain 9, 6, 9, ..., 32, which is to say, observation 1 and 3 in default both correspond to observation 9 in xdata. xdata in this example might record geographic location and in default, persons in observations 1 and 3 live in the same locale.

And in a final example, xobsno might contain all the above and missing values (.). The missing values would indicate observations in default that have no corresponding observation in xdata. If observations 7 and 11 contained missing, that means there would be no observations in xdata corresponding to observations 7 and 11 in default. (_frval() has a second syntax that allows you to specify the value returned when there are no corresponding observations; see below.)

Regardless of the complexity of the example, the value of xobsno in observation j is the corresponding observation number i in xdata. Regardless of complexity, to create new variable hrlywage in default, you would type

. generate hrlywage = income / _frval(xdata, hrswrked, xobsno)

That leaves only the question of how to generate xobsno in all the above situations, and it is easy to do. See [D] frlink.

There are two more things to know.

First, variables across frames are distinct. If the variable we have been calling income in default were named x, and the variable hrswrked in xdata were also named x, you would type

. generate hrlywage = x / _frval(xdata, x, xobsno)

Second, although we have demonstrated the use of _frval() with numeric variables, it works with string variables too. If *var* is a string variable name, _frval() returns a string result.

Domain *frm*:

any existing framename

Domain *var*:

any existing variable name in frm; varname abbreviation is allowed

Domain i:

any numeric values including missing values even though the nonmissing values should be integers in the range 1 to frm's _N; nonintegers will be interpreted as the corresponding integer obtained by truncation, and values outside the range will

be treated as if they were missing value

Range:

range of var in frm plus missing value; numeric missing value (.) when var is

numeric, and string missing value ("") when var is string

```
_frval(frm, var, i, v)
```

Description:

the $_{frval}()$ function described above but with a fourth argument v

_frval() returns values of variables stored in other frames. It returns var's ith observation (var[i]) from the frame frm.

When v is specified, $_frval()$ returns v if var[i] is missing or if i is outside the valid range of observations.

. generate hwage = income / _frval(xdata, hrswrked, xobsno, .z)

. generate hwage = income / _frval(xdata, hrswrked, xobsno, avg)

In the first case, .z is returned for observations in which xobsno contains values that are out of range. In the second case, the value recorded in variable avg is returned.

Domain *frm*:

any existing framename

Domain var:

any existing variable name in frm; varname abbreviation is allowed

Domain i:

any numeric values including missing values even though the nonmissing values should be integers in the range 1 to frm's _N; nonintegers will be interpreted as the corresponding integer obtained by truncation, and values outside the range will

be treated as if they were missing value

Domain v:

any numeric value when var is numeric; any string value when var is string (can

be a constant or vary observation by observation)

Range:

range of var in frm plus v

has_eprop(name)

Description: 1 if name appears as a word in e(properties); otherwise, 0

Domain: names Range: 0 or 1

inlist(z,a,b,...)

Description: 1 if z is a member of the remaining arguments; otherwise, 0

All arguments must be reals or all must be strings. The number of arguments is

between 2 and 250 for reals and between 2 and 10 for strings.

Domain: all reals or all strings

Range: 0 or 1

inrange(z,a,b)

Description: 1 if it is known that $a \le z \le b$; otherwise, 0

The following ordered rules apply:

 $z \geq$. returns 0.

 $a \geq$. and b = . returns 1.

 $a \ge$. returns 1 if $z \le b$; otherwise, it returns 0. $b \ge$. returns 1 if $a \le z$; otherwise, it returns 0.

Otherwise, 1 is returned if $a \le z \le b$.

If the arguments are strings, "." is interpreted as "".

Domain: all reals or all strings

Range: 0 or 1

$irecode(x, x_1, x_2, x_3, \ldots, x_n)$

Description: missing if x is missing or x_1, \ldots, x_n is not weakly increasing; 0 if $x \le x_1$; 1 if

 $x_1 < x \le x_2$; 2 if $x_2 < x \le x_3$; ...; n if $x > x_n$

Also see autocode() and recode() for other styles of recode functions.

irecode(3, -10, -5, -3, -3, 0, 15, .) = 5

Domain x: -8e+307 to 8e+307

Domain x_i : -8e+307 to 8e+307Range: -8e+307 to 8e+307

matrix(*exp*)

Description: restricts name interpretation to scalars and matrices; see scalar()

Domain: any valid expression Range: evaluation of *exp*

maxbyte()

Description: the largest value that can be stored in storage type byte

This function takes no arguments, but the parentheses must be included.

Range: one integer number

maxdouble()

Description: the largest value that can be stored in storage type double

This function takes no arguments, but the parentheses must be included.

Range: one double-precision number

maxfloat()

Description: the largest value that can be stored in storage type float

This function takes no arguments, but the parentheses must be included.

Range: one floating-point number

maxint()

Description: the largest value that can be stored in storage type int

This function takes no arguments, but the parentheses must be included.

Range: one integer number

maxlong()

Description: the largest value that can be stored in storage type long

This function takes no arguments, but the parentheses must be included.

Range: one integer number

 $\min(x_1, x_2, \ldots, x_n)$

Description: a synonym for missing $(x_1, x_2, ..., x_n)$

minbyte()

Description: the smallest value that can be stored in storage type byte

This function takes no arguments, but the parentheses must be included.

Range: one integer number

mindouble()

Description: the smallest value that can be stored in storage type double

This function takes no arguments, but the parentheses must be included.

Range: one double-precision number

minfloat()

Description: the smallest value that can be stored in storage type float

This function takes no arguments, but the parentheses must be included.

Range: one floating-point number

minint()

Description: the smallest value that can be stored in storage type int

This function takes no arguments, but the parentheses must be included.

Range: one integer number

minlong()

Description: the smallest value that can be stored in storage type long

This function takes no arguments, but the parentheses must be included.

Range: one integer number

missing(x_1, x_2, \ldots, x_n)

Description: 1 if any x_i evaluates to missing; otherwise, 0

Stata has two concepts of missing values: a numeric missing value (., a, b, ..., z) and a string missing value (""). missing() returns 1 (meaning true) if any expression x_i evaluates to missing. If x is numeric, missing(x) is equivalent to

 $x \ge ...$ If x is string, missing(x) is equivalent to x = -...

Domain x_i : any string or numeric expression

Range: 0 and 1

r(name)

Description: the value of the stored result r(name); see [U] 18.8 Accessing results calculated

by other programs

r(name) = scalar missing if the stored result does not exist r(name) = specified matrix if the stored result is a matrix

r(name) = scalar numeric value if the stored result is a scalar that can be

interpreted as a number

Domain: names

Range: strings, scalars, matrices, or missing

 $recode(x, x_1, x_2, \ldots, x_n)$

Description: missing if x_1, x_2, \dots, x_n is not weakly increasing; x if x is missing; x_1 if $x \le x_1$;

 x_2 if $x \leq x_2, \ldots$; otherwise, x_n if $x > x_1, x_2, \ldots, x_{n-1}, x_i \geq 1$ is interpreted

as $x_i = +\infty$

Also see autocode() and irecode() for other styles of recode functions.

Domain x: -8e+307 to 8e+307 or missing

Domain x_1 : -8e+307 to 8e+307

Domain x_2 : x_1 to 8e+307

. . .

Domain x_n : x_{n-1} to 8e+307

Range: $x_1, x_2, ..., x_n$ or missing

replay()

Description: 1 if the first nonblank character of local macro '0' is a comma, or if '0' is empty

This is a function for use by programmers writing estimation commands; see

P ereturn.

Range: integers 0 and 1, meaning false and true, respectively

return(name)

Description: the value of the to-be-stored result r(name); see [P] return

return(name) = scalar missing if the stored result does not exist return(name) = specified matrix if the stored result is a matrix return(name) = scalar numeric value if the stored result is a scalar

Domain: names

Range: strings, scalars, matrices, or missing

s(name)

Description: the value of stored result s (name); see [U] 18.8 Accessing results calculated by

other programs

s(name) = . if the stored result does not exist

Domain: names

Range: strings or missing

scalar(exp)

Description: restricts name interpretation to scalars and matrices

Names in expressions can refer to names of variables in the dataset, names of matrices, or names of scalars. Matrices and scalars can have the same names as variables in the dataset. If names conflict, Stata assumes that you are referring to

the name of the variable in the dataset.

matrix() and scalar() explicitly state that you are referring to matrices and scalars. matrix() and scalar() are the same function; scalars and matrices may not have the same names and so cannot be confused. Typing scalar(x) makes it clear that you are referring to the scalar or matrix named x and not the variable

named x, should there happen to be a variable of that name.

Domain: any valid expression

Range: evaluation of *exp*

smallestdouble()

Description: the smallest double-precision number greater than zero

If 0 < d < smallestdouble(), then d does not have full double precision; these are called the denormalized numbers. This function takes no arguments, but the

parentheses must be included.

Range: a double-precision number close to 0

References

Kantor, D., and N. J. Cox. 2005. Depending on conditions: A tutorial on the cond() function. Stata Journal 5: 413–420.

Rising, W. R. 2010. Stata tip 86: The missing() function. Stata Journal 10: 303-304.

Also see

[FN] Functions by category

[D] **egen** — Extensions to generate

[D] generate — Create or change contents of variable

[M-4] **Programming** — Programming functions

[U] 13.3 Functions

Title

Random-number functions

Contents	Functions	Remarks and examples	Methods and formulas
Acknowledgments	References	Also see	

Contents

rbeta(a,b)	beta(a,b) random variates, where a and b are the beta distribution shape parameters
rbinomial(n,p)	binomial (n,p) random variates, where n is the number of trials and p is the success probability
reauchy(a,b)	Cauchy (a,b) random variates, where a is the location parameter and b is the scale parameter
$\mathtt{rchi2}(d\!f)$	χ^2 , with df degrees of freedom, random variates
rexponential(b)	exponential random variates with scale b
rgamma(a,b)	$\mbox{gamma}(a,b) \mbox{ random variates, where } a \mbox{ is the gamma shape parameter} \\ \mbox{and } b \mbox{ is the scale parameter} \\$
$ ext{rhypergeometric}(N,K,n)$	hypergeometric random variates
rigaussian(m,a)	inverse Gaussian random variates with mean m and shape parameter \boldsymbol{a}
${ t rlaplace}(m,b)$	$\operatorname{Laplace}(m,b)$ random variates with mean m and scale parameter b
rlogistic()	logistic variates with mean 0 and standard deviation $\pi/\sqrt{3}$
rlogistic(s)	logistic variates with mean 0, scale s , and standard deviation $s\pi/\sqrt{3}$
${\tt rlogistic}(m,s)$	logistic variates with mean m , scale s , and standard deviation $s\pi/\sqrt{3}$
rnbinomial(n,p)	negative binomial random variates
rnormal()	standard normal (Gaussian) random variates, that is, variates from a normal distribution with a mean of 0 and a standard deviation of 1
rnormal(m)	$\operatorname{normal}(m,1)$ (Gaussian) random variates, where m is the mean and the standard deviation is 1
rnormal(m,s)	$\operatorname{normal}(m,s)$ (Gaussian) random variates, where m is the mean and s is the standard deviation
${\tt rpoisson}(m)$	$\operatorname{Poisson}(m)$ random variates, where m is the distribution mean
$\mathtt{rt}(df)$	Student's t random variates, where df is the degrees of freedom
runiform()	uniformly distributed random variates over the interval $(0,1)$
runiform(a,b)	uniformly distributed random variates over the interval $\left(a,b\right)$
runiformint(a,b)	uniformly distributed random integer variates on the interval $\left[a,b\right]$

rweibull(a,b)	Weibull variates with shape a and scale b
rweibull(a,b,g)	Weibull variates with shape a , scale b , and location g
rweibullph(a,b)	Weibull (proportional hazards) variates with shape \boldsymbol{a} and scale \boldsymbol{b}
rweibullph(a,b,g)	Weibull (proportional hazards) variates with shape a , scale b , and location g

Functions

The term "pseudorandom number" is used to emphasize that the numbers are generated by formulas and are thus not truly random. From now on, we will drop the "pseudo" and just say random numbers.

For information on setting the random-number seed, see [R] set seed.

```
runiform()
  Description: uniformly distributed random variates over the interval (0,1)
              runiform() can be seeded with the set seed command; see [R] set seed.
  Range:
              c(epsdouble) to 1 - c(epsdouble)
runiform(a,b)
  Description: uniformly distributed random variates over the interval (a, b)
  Domain a:
              c(mindouble) to c(maxdouble)
  Domain b:
              c(mindouble) to c(maxdouble)
  Range:
              a + c(epsdouble) to b - c(epsdouble)
runiformint (a,b)
```

Description: uniformly distributed random integer variates on the interval [a, b]

If a or b is nonintegral, runiformint(a,b) returns runiformint(floor(a), floor(b)).

 -2^{53} to 2^{53} (may be nonintegral) Domain a: -2^{53} to 2^{53} (may be nonintegral) Domain *b*: -2^{53} to 2^{53} Range:

```
rbeta(a,b)
```

Description: beta(a,b) random variates, where a and b are the beta distribution shape parameters

Besides using the standard methodology for generating random variates from a given distribution, rbeta() uses the specialized algorithms of Johnk (Gentle 2003), Atkinson and Whittaker (1970, 1976), Devroye (1986), and Schmeiser and Babu (1980).

Domain a: 0.05 to 1e+50.15 to 1e+5 Domain b: Range: 0 to 1 (exclusive)

rbinomial(n,p)

Description: binomial(n,p) random variates, where n is the number of trials and p is the success

probability

Besides using the standard methodology for generating random variates from a given distribution, rbinomial() uses the specialized algorithms of Kachitvichyanukul (1982), Kachitvichyanukul and Schmeiser (1988), and Kemp (1986).

Domain n: 1 to 1e+11 Domain p: 1e-8 to 1-1e-8

Range: 0 to n

rcauchy(a,b)

Description: Cauchy(a,b) random variates, where a is the location parameter and b is the scale

parameter

Domain a: -1e+300 to 1e+300Domain b: 1e-100 to 1e+300

Range: c(mindouble) to c(maxdouble)

rchi2(df)

Description: χ^2 , with df degrees of freedom, random variates

Domain df: 2e–4 to 2e+8

Range: 0 to c(maxdouble)

rexponential(b)

Description: exponential random variates with scale b

Domain *b*: 1e–323 to 8e+307 Range: 1e–323 to 8e+307

rgamma(a,b)

Description: gamma(a,b) random variates, where a is the gamma shape parameter and b is the

scale parameter

Methods for generating gamma variates are taken from Ahrens and Dieter (1974),

Best (1983), and Schmeiser and Lal (1980).

Domain a: 1e-4 to 1e+8

Domain b: c(smallestdouble) to c(maxdouble)

Range: 0 to c(maxdouble)

rhypergeometric (N, K, n)

Description: hypergeometric random variates

The distribution parameters are integer valued, where N is the population size, K is the number of elements in the population that have the attribute of interest, and n is the sample size.

Besides using the standard methodology for generating random variates from a given distribution, rhypergeometric() uses the specialized algorithms of Kachitvichyanukul (1982) and Kachitvichyanukul and Schmeiser (1985).

Domain N: 2 to 1e+6 Domain K: 1 to N-1Domain n: 1 to N-1

Range: $\max(0, n - N + K)$ to $\min(K, n)$

rigaussian(m,a)

Description: inverse Gaussian random variates with mean m and shape parameter a

rigaussian() is based on a method proposed by Michael, Schucany, and

Haas (1976).

Domain m: 1e-10 to 1000 Domain a: 0.001 to 1e+10 Range: 0 to c(maxdouble)

rlaplace(m,b)

Description: Laplace(m,b) random variates with mean m and scale parameter b

Domain m: -1e+300 to 1e+300Domain b: 1e-300 to 1e+300

Range: c(mindouble) to c(maxdouble)

rlogistic()

Description: logistic variates with mean 0 and standard deviation $\pi/\sqrt{3}$

The variates x are generated by x = invlogistic(0,1,u), where u is a random

uniform(0,1) variate.

Range: c(mindouble) to c(maxdouble)

rlogistic(s)

Description: logistic variates with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$

The variates x are generated by x = invlogistic(0, s, u), where u is a random

uniform(0,1) variate.

Domain s: 0 to c(maxdouble)

Range: c(mindouble) to c(maxdouble)

rlogistic(m,s)

Description: logistic variates with mean m, scale s, and standard deviation $s\pi/\sqrt{3}$

The variates x are generated by x = invlogistic(m, s, u), where u is a random

uniform(0.1) variate.

Domain m: c(mindouble) to c(maxdouble)

Domain s: 0 to c(maxdouble)

Range: c(mindouble) to c(maxdouble)

rnbinomial(n, p)

Description: negative binomial random variates

If n is integer valued, rnbinomial() returns the number of failures before the nth success, where the probability of success on a single trial is p. n can also be nonintegral.

Domain n: 1e-4 to 1e+5 Domain p: 1e-4 to 1-1e-4

Range: 0 to $2^{53} - 1$

rnormal()

Description: standard normal (Gaussian) random variates, that is, variates from a normal distribution

with a mean of 0 and a standard deviation of 1

Range: c(mindouble) to c(maxdouble)

rnormal(m)

Description: normal(m,1) (Gaussian) random variates, where m is the mean and the standard

deviation is 1

Domain m: c(mindouble) to c(maxdouble) Range: c(mindouble) to c(maxdouble)

rnormal(m,s)

Description: normal(m,s) (Gaussian) random variates, where m is the mean and s is the standard

deviation

The methods for generating normal (Gaussian) random variates are taken from Knuth (1998, 122–128); Marsaglia, MacLaren, and Bray (1964); and Walker (1977).

Domain m: c(mindouble) to c(maxdouble)

Domain s: 0 to c(maxdouble)

Range: c(mindouble) to c(maxdouble)

rpoisson(m)

Description: Poisson(m) random variates, where m is the distribution mean

Poisson variates are generated using the probability integral transform methods of Kemp and Kemp (1990, 1991) and the method of Kachitvichyanukul (1982).

Domain m: 1e–6 to 1e+11 Range: 0 to $2^{53} - 1$

rt(df)

Description: Student's t random variates, where df is the degrees of freedom

Student's t variates are generated using the method of Kinderman and Monahan (1977, 1980).

Domain df: 1 to $2^{53} - 1$

Range: c(mindouble) to c(maxdouble)

rweibull(a,b)

Description: Weibull variates with shape a and scale b

The variates x are generated by x = invweibulltail(a,b,0,u), where u is a random uniform(0,1) variate.

Domain *a*: 0.01 to 1e+6 Domain *b*: 1e-323 to 8e+307 Range: 1e-323 to 8e+307 Description: Weibull variates with shape a, scale b, and location q

The variates x are generated by x = invweibulltail(a,b,g,u), where u is a

random uniform(0,1) variate.

Domain *a*: 0.01 to 1e+6 Domain *b*: 1e-323 to 8e+307 Domain *q*: -8e+307 to 8e+307

Range: g + c(epsdouble) to 8e+307

rweibullph(a,b)

Description: Weibull (proportional hazards) variates with shape a and scale b

The variates x are generated by x = invweibullphtail(a,b,0,u), where u is a

random uniform(0,1) variate.

Domain *a*: 0.01 to 1e+6 Domain *b*: 1e–323 to 8e+307 Range: 1e–323 to 8e+307

rweibullph(a,b,g)

Description: Weibull (proportional hazards) variates with shape a, scale b, and location g

The variates x are generated by x = invweibullphtail(a,b,g,u), where u is a

random uniform(0,1) variate.

Domain *a*: 0.01 to 1e+6 Domain *b*: 1e–323 to 8e+307 Domain *q*: –8e+307 to 8e+307

Range: q + c(epsdouble) to 8e+307

Remarks and examples

It is ironic that the first thing to note about random numbers is how to make them reproducible. Before using a random-number function, type

```
set seed #
```

where # is any integer between 0 and $2^{31} - 1$, inclusive, to draw the same sequence of random numbers. It does not matter which integer you choose as your seed; they are all equally good. See [R] set seed.

runiform() is the basis for all the other random-number functions because all the other random-number functions transform uniform (0,1) random numbers to the specified distribution.

runiform() implements the 64-bit Mersenne Twister (mt64), the stream 64-bit Mersenne Twister (mt64s), and the 32-bit "keep it simple stupid" (kiss32) random-number generators (RNGs) for generating uniform (0,1) random numbers. runiform() uses the mt64 RNG by default.

runiform() uses the kiss32 RNG only when the user version is less than 14 or when the RNG has been set to kiss32; see [P] version for details about setting the user version. We recommend that you do not change the default RNG, but see [R] set rng for details.

□ Technical note

Although we recommend that you use runiform(), we made generator-specific versions of runiform() available for advanced users who want to hardcode their generator choice. The function runiform_mt64() always uses the mt64 RNG to generate uniform (0,1) random numbers, the function runiform_mt64s() always uses the mt64s RNG to generate uniform (0,1) random numbers, the function runiform_kiss32() always uses the kiss32 RNG to generate uniform (0,1) random numbers. In fact, generator-specific versions are available for all the implemented distributions. For example, rnormal_mt64(), rnormal_mt64s, and rnormal_kiss32() use transforms of mt64, mt64s, and kiss32 uniform variates, respectively, to generate standard normal variates.

□ Technical note

Both the mt64 and the kiss32 RNGs produce uniform variates that pass many tests for randomness. Many researchers prefer the mt64 to the kiss32 RNG because the mt64 generator has a longer period and a finer resolution and requires a higher dimension before patterns appear; see Matsumoto and Nishimura (1998).

The mt64 RNG has a period of $2^{19937} - 1$ and a resolution of 2^{-53} ; see Matsumoto and Nishimura (1998). Each stream of the mt64s RNG contains 2¹²⁸ random numbers, and mt64s has a resolution of 2^{-53} ; see Haramoto et al. (2008). The kiss32 RNG has a period of about 2^{126} and a resolution of 2^{-32} ; see *Methods and formulas* below.

Technical note

This technical note explains how to restart a RNG from its current spot.

The current spot in the sequence of a RNG is part of the state of a RNG. If you tell me the state of a RNG, I know where it is in its sequence, and I can compute the next random number. The state of a RNG is a complicated object that requires more space than the integers used to seed a generator. For instance, an mt64 state is a 5011-digit, base-16 number preceded by three letters.

If you want to restart a RNG from where it left off, you should store the current state in a macro and then set the state of the RNG when you want to restart it. For example, suppose we set a seed and draw some random numbers.

```
. set obs 3
Number of observations (_N) was 0, now 3.
```

- . set seed 12345
- . generate x = runiform()
- . list x

	х
1.	.3576297
2.	.4004426
3.	.6893833

. local rngstate "'c(rngstate)'"

We draw some more random numbers.

```
. replace x = runiform()
(3 real changes made)
```

. list x

	х
1.	.5597356
2.	.5744513
3.	.2076905

Now, we set the state of the RNG to where it was and draw those same random numbers again.

```
. set rngstate 'rngstate'
```

```
. replace x = runiform()
(0 real changes made)
```

. list x



Methods and formulas

All the nonuniform generators are based on the uniform mt64, mt64s, and kiss32 RNGs.

The mt64 RNG is well documented in Matsumoto and Nishimura (1998) and on their website http://www.math.sci.hiroshima-u.ac.jp/~m-mat/MT/emt.html. The mt64 RNG implements the 64-bit version discussed at http://www.math.sci.hiroshima-u.ac.jp/~m-mat/MT/emt64.html. The mt64s RNG is based on a method proposed by Haramoto et al. (2008). The default seed of all three RNGs is 123456789.

kiss32 generator

The kiss32 uniform RNG implemented in runiform() is based on George Marsaglia's (G. Marsaglia, 1994, pers. comm.) 32-bit pseudorandom-integer generator kiss32. The integer kiss32 RNG is composed of two 32-bit pseudorandom-integer generators and two 16-bit integer generators (combined to make one 32-bit integer generator). The four generators are defined by the recursions

$$x_n = 69069 x_{n-1} + 1234567 \mod 2^{32} \tag{1}$$

$$y_n = y_{n-1}(I + L^{13})(I + R^{17})(I + L^5)$$
(2)

$$z_n = 65184(z_{n-1} \bmod 2^{16}) + \operatorname{int}(z_{n-1}/2^{16})$$
(3)

$$w_n = 63663(w_{n-1} \bmod 2^{16}) + \operatorname{int}(w_{n-1}/2^{16}) \tag{4}$$

In (2), the 32-bit word y_n is viewed as a 1×32 binary vector; L is the 32×32 matrix that produces a left shift of one (L has 1s on the first left subdiagonal, 0s elsewhere); and R is L transpose, affecting a right shift by one. In (3) and (4), int(x) is the integer part of x.

The integer kiss32 RNG produces the 32-bit random integer

$$R_n = x_n + y_n + z_n + 2^{16} w_n \mod 2^{32}$$

The kiss32 uniform RNG implemented in runiform() takes the output from the integer kiss32 RNG and divides it by 2^{32} to produce a real number on the interval (0,1). (Zeros are discarded, and the first nonzero result is returned.)

The recursion (5)–(8) have, respectively, the periods

$$2^{32}$$
 (5)

$$2^{32} - 1$$
 (6)

$$(65184 \cdot 2^{16} - 2)/2 \approx 2^{31} \tag{7}$$

$$(63663 \cdot 2^{16} - 2)/2 \approx 2^{31} \tag{8}$$

Thus the overall period for the integer kiss32 RNG is

$$2^{32} \cdot (2^{32} - 1) \cdot (65184 \cdot 2^{15} - 1) \cdot (63663 \cdot 2^{15} - 1) \approx 2^{126}$$

When Stata first comes up, it initializes the four recursions in kiss32 by using the seeds

$$x_0 = 123456789$$

$$y_0 = 521288629$$

$$z_0 = 362436069$$

$$w_0 = 2262615$$

Successive calls to the kiss32 uniform RNG implemented in runiform() then produce the sequence

$$\frac{R_1}{2^{32}}$$
, $\frac{R_2}{2^{32}}$, $\frac{R_3}{2^{32}}$, ...

Hence, the kiss32 uniform RNG implemented in runiform() gives the same sequence of random numbers in every Stata session (measured from the start of the session) unless you reinitialize the seed. The full seed is the set of four numbers (x,y,z,w), but you can reinitialize the seed by simply issuing the command

. set seed #

where # is any integer between 0 and $2^{31} - 1$, inclusive. When this command is issued, the initial value x_0 is set equal to #, and the other three recursions are restarted at the seeds y_0 , z_0 , and w_0 given above. The first 100 random numbers are discarded, and successive calls to the kiss32 uniform RNG implemented in runiform() give the sequence

$$\frac{R'_{101}}{2^{32}}$$
, $\frac{R'_{102}}{2^{32}}$, $\frac{R'_{103}}{2^{32}}$, ...

However, if the command

. set seed 123456789

is given, the first 100 random numbers are not discarded, and you get the same sequence of random numbers that the kiss32 RNG produces when Stata restarts; also see [R] set seed.

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Also see

- [FN] Functions by category
- [D] **egen** Extensions to generate
- [D] **generate** Create or change contents of variable
- [R] set rng Set which random-number generator (RNG) to use
- [R] set rngstream Specify the stream for the stream random-number generator
- [R] **set seed** Specify random-number seed and state
- [M-5] **runiform**() Uniform and nonuniform pseudorandom variates
- [U] 13.3 Functions

Selecting time-span functions

Contents Functions Also see

Contents

```
true if d_1 \le t \le d_2, where t is the time variable previously tsset twithin(d_1, d_2) true if d_1 \le t \le d_2, where t is the time variable previously tsset
```

Functions

 $tin(d_1,d_2)$

Description: true if $d_1 \le t \le d_2$, where t is the time variable previously tsset

You must have previously tsset the data to use tin(); see [TS] **tsset**. When you tsset the data, you specify a time variable, t, and the format on t states how it is recorded. You type d_1 and d_2 according to that format.

If t has a %tc format, you could type tin(5jan1992 11:15, 14apr2002 12:25).

If t has a %td format, you could type tin(5jan1992, 14apr2002).

If t has a %tw format, you could type tin(1985w1, 2002w15).

If t has a %tm format, you could type tin(1985m1, 2002m4).

If t has a %tq format, you could type tin(1985q1, 2002q2).

If t has a %th format, you could type tin(1985h1, 2002h1).

If t has a %ty format, you could type tin(1985, 2002).

If t has a %tb format, you could type tin(5jan1992, 14apr2002). This will work as expected even if the arguments of tin() are not business days.

Otherwise, t is just a set of integers, and you could type tin(12, 38).

The details of the t format do not matter. If your t is formatted tdmm/dd/yy so that 5jan1992 displays as t1/5/92, you would still type the date in day-month-year order: t1/5jan1992, 14apr2002).

Domain d_1 : date or time literals or strings recorded in units of t previously tsset or blank to

indicate no minimum date

Domain d_2 : date or time literals or strings recorded in units of t previously tsset or blank to

indicate no maximum date

Range: 0 and 1, $1 \Rightarrow true$

$twithin(d_1,d_2)$

Description: true if $d_1 < t < d_2$, where t is the time variable previously tsset

See tin() above; twithin() is similar, except the range is exclusive.

Domain d_1 : date or time literals or strings recorded in units of t previously tsset or blank to

indicate no minimum date

Domain d_2 : date or time literals or strings recorded in units of t previously tsset or blank to

indicate no maximum date

Range: 0 and 1, $1 \Rightarrow true$

Also see

- [FN] Functions by category
- [D] egen Extensions to generate
- [D] **generate** Create or change contents of variable
- [U] 13.3 Functions

Statistical functions

Contents

betaden(a,b,x)	the probability density of the beta distribution, where a and b are the shape parameters; 0 if $x < 0$ or $x > 1$
$\texttt{binomial}(n,k,\theta)$	the probability of observing $floor(k)$ or fewer successes in $floor(n)$ trials when the probability of a success on one trial is θ ; 0 if $k < 0$; or 1 if $k > n$
binomialp(n,k,p)	the probability of observing $floor(k)$ successes in $floor(n)$ trials when the probability of a success on one trial is p
$\texttt{binomialtail}(n, k, \theta)$	the probability of observing $floor(k)$ or more successes in $floor(n)$ trials when the probability of a success on one trial is θ ; 1 if $k < 0$; or 0 if $k > n$
$\mathtt{binormal}(h,k,\rho)$	the joint cumulative distribution $\Phi(h,k,\rho)$ of bivariate normal with correlation ρ
cauchy (a,b,x)	the cumulative Cauchy distribution with location parameter \boldsymbol{a} and scale parameter \boldsymbol{b}
cauchyden(a,b,x)	the probability density of the Cauchy distribution with location parameter \boldsymbol{a} and scale parameter \boldsymbol{b}
cauchytail(a,b,x)	the reverse cumulative (upper tail or survivor) Cauchy distribution with location parameter \boldsymbol{a} and scale parameter \boldsymbol{b}
chi2(df,x)	the cumulative χ^2 distribution with $d\!f$ degrees of freedom; 0 if $x<0$
$\operatorname{chi2den}(df,x)$	the probability density of the χ^2 distribution with $d\!f$ degrees of freedom; 0 if $x<0$
$\mathtt{chi2tail}(df,x)$	the reverse cumulative (upper tail or survivor) χ^2 distribution with df degrees of freedom; 1 if $x<0$
dgammapda(a,x)	$rac{\partial P(a,x)}{\partial a},$ where $P(a,x)=$ gammap(a,x); 0 if $x<0$
dgammapdada(a,x)	$rac{\partial^2 P(a,x)}{\partial a^2},$ where $P(a,x)=$ gammap(a,x); 0 if $x<0$
dgammapdadx(a,x)	$rac{\partial^2 P(a,x)}{\partial a \partial x}$, where $P(a,x) = \mathrm{gammap}(a,x)$; 0 if $x < 0$
$\operatorname{dgammapdx}(a,x)$	$rac{\partial P(a,x)}{\partial x},$ where $P(a,x)=$ gammap(a,x); 0 if $x<0$
dgammapdxdx(a,x)	$\frac{\partial^2 P(a,x)}{\partial x^2}$, where $P(a,x)=$ gammap(a,x); 0 if $x<0$
dunnettprob(k, df, x)	the cumulative multiple range distribution that is used in Dunnett's multiple-comparison method with k ranges and df degrees of freedom; 0 if $x<0$
exponential(b,x)	the cumulative exponential distribution with scale b
exponentialden(b,x)	the probability density function of the exponential distribution with scale \boldsymbol{b}
exponentialtail(b,x)	the reverse cumulative exponential distribution with scale b

$F(df_1, df_2, f)$	the cumulative F distribution with df_1 numerator and df_2 denominator degrees of freedom: $\mathbf{F}(df_1, df_2, f) = \int_0^f \mathbf{Fden}(df_1, df_2, t) dt$; 0 if $f < 0$
$\texttt{Fden}(df_1, df_2, f)$	the probability density function of the F distribution with df_1 numerator and df_2 denominator degrees of freedom; 0 if $f<0$
$\texttt{Ftail}(df_1, df_2, f)$	the reverse cumulative (upper tail or survivor) F distribution with df_1 numerator and df_2 denominator degrees of freedom; 1 if $f<0$
gammaden(a,b,g,x)	the probability density function of the gamma distribution; 0 if $x < g \label{eq:control}$
gammap(a,x)	the cumulative gamma distribution with shape parameter $a; \ 0$ if $x < 0$
gammaptail(a,x)	the reverse cumulative (upper tail or survivor) gamma distribution with shape parameter $a;1$ if $x<0$
${\tt hypergeometric}(N,K,n,k)$	the cumulative probability of the hypergeometric distribution
$\label{eq:hypergeometricp} \texttt{hypergeometricp}(N,K,n,k)$) the hypergeometric probability of k successes out of a sample of size n , from a population of size N containing K elements that have the attribute of interest
ibeta(a,b,x)	the cumulative beta distribution with shape parameters a and b ; 0 if $x<0$; or 1 if $x>1$
ibetatail(a,b,x)	the reverse cumulative (upper tail or survivor) beta distribution with shape parameters a and b ; 1 if $x<0$; or 0 if $x>1$
igaussian(m,a,x)	the cumulative inverse Gaussian distribution with mean m and shape parameter $a;\ {\bf 0}$ if $x\leq 0$
igaussianden(m,a,x)	the probability density of the inverse Gaussian distribution with mean m and shape parameter $a;$ 0 if $x \leq 0$
igaussiantail(m,a,x)	the reverse cumulative (upper tail or survivor) inverse Gaussian distribution with mean m and shape parameter $a;$ 1 if $x \leq 0$
invbinomial(n,k,p)	the inverse of the cumulative binomial; that is, θ (θ = probability of success on one trial) such that the probability of observing floor(k) or fewer successes in floor(n) trials is p
invbinomialtail(n,k,p)	the inverse of the right cumulative binomial; that is, θ (θ = probability of success on one trial) such that the probability of observing floor(k) or more successes in floor(n) trials is p
invcauchy(a,b,p)	the inverse of cauchy(): if cauchy(a,b,x) = p , then invcauchy(a,b,p) = x
invcauchytail(a,b,p)	the inverse of cauchytail(): if cauchytail(a,b,x) = p , then invcauchytail(a,b,p) = x
invchi2(df,p)	the inverse of chi2(): if chi2(df , x) = p , then invchi2(df , p) = x
invchi2tail(df,p)	the inverse of chi2tail(): if chi2tail($d\!f$, x) = p , then invchi2tail($d\!f$, p) = x
invdunnettprob(k, df, p)	the inverse cumulative multiple range distribution that is used in Dunnett's multiple-comparison method with k ranges and df degrees of freedom
invexponential(b,p)	the inverse cumulative exponential distribution with scale b : if exponential(b , x) = p , then invexponential(b , p) = x

```
the inverse reverse cumulative exponential distribution with scale b:
invexponential tail(b, p)
                                  if exponentialtail(b, x) = p, then
                                  invexponentialtail(b, p) = x
                               the inverse cumulative F distribution: if F(df_1, df_2, f) = p, then
invF(df_1, df_2, p)
                                  invF(df_1, df_2, p) = f
                               the inverse reverse cumulative (upper tail or survivor) F distribution:
invFtail(df_1, df_2, p)
                                  if Ftail(df_1, df_2, f) = p, then invFtail(df_1, df_2, p) = f
                               the inverse cumulative gamma distribution: if gammap(a, x) = p,
invgammap(a,p)
                                  then invgammap(a, p) = x
                               the inverse reverse cumulative (upper tail or survivor) gamma distri-
invgammaptail(a, p)
                                  bution: if gammaptail(a, x) = p, then invgammaptail(a, p)
                               the inverse cumulative beta distribution: if ibeta(a,b,x) = p,
invibeta(a,b,p)
                                  then invibeta(a,b,p)=x
invibetatail (a,b,p)
                               the inverse reverse cumulative (upper tail or survivor) beta distribu-
                                  tion: if ibetatail(a,b,x) = p, then invibetatail(a,b,p)
                               the inverse of igaussian(): if
invigaussian(m,a,p)
                                  igaussian(m,a,x) = p, then invigaussian(m,a,p) = x
invigaussiantail(m, a, p)
                               the inverse of igaussiantail(): if
                                  igaussiantail(m,a,x) = p, then
                                  invigaussiantail(m,a,p) = x
                               the inverse of laplace(): if laplace(m, b, x) = p, then
invlaplace(m,b,p)
                                  invlaplace(m,b,p) = x
invlaplacetail(m,b,p)
                               the inverse of laplacetail(): if laplacetail(m,b,x) = p,
                                  then invlaplacetail (m, b, p) = x
invlogistic(p)
                               the inverse cumulative logistic distribution: if logistic(x) = p,
                                  then invlogistic(p) = x
                               the inverse cumulative logistic distribution: if logistic(s, x) = p,
invlogistic(s,p)
                                  then invlogistic(s,p) = x
                               the inverse cumulative logistic distribution: if logistic(m, s, x)
invlogistic(m,s,p)
                                  = p, then invlogistic(m, s, p) = x
invlogistictail(p)
                               the inverse reverse cumulative logistic distribution: if
                                  logistictail(x) = p, then invlogistictail(p) = x
                               the inverse reverse cumulative logistic distribution: if
invlogistictail(s,p)
                                  logistictail(s,x) = p, then invlogistictail(s,p) = x
invlogistictail(m,s,p)
                               the inverse reverse cumulative logistic distribution: if
                                  logistictail(m,s,x) = p, then
                                  invlogistictail(m,s,p) = x
                               the value of the negative binomial parameter, p, such that q =
invnbinomial (n, k, q)
                                  nbinomial(n,k,p)
                               the value of the negative binomial parameter, p, such that
invnbinomialtail(n, k, q)
                                  q = nbinomialtail(n, k, p)
                               the inverse cumulative noncentral \chi^2 distribution: if
invnchi2(df, np, p)
                                  nchi2(df, np, x) = p, then invnchi2(df, np, p) = x
                               the inverse reverse cumulative (upper tail or survivor) non-
invnchi2tail(df, np, p)
                                  central \chi^2 distribution: if nchi2tail(df, np, x) = p, then
                                  invnchi2tail(df, np, p) = x
```

```
invnF(df_1, df_2, np, p)
                               the inverse cumulative noncentral F distribution: if
                                  nF(df_1, df_2, np, f) = p, then invnF(df_1, df_2, np, p) = f
invnFtail(df_1, df_2, np, p)
                               the inverse reverse cumulative (upper tail or survivor) noncen-
                                  tral F distribution: if nFtail(df_1, df_2, np, f) = p, then
                                  invnFtail(df_1, df_2, np, p) = f
                               the inverse cumulative noncentral beta distribution: if
invnibeta(a,b,np,p)
                                  nibeta(a,b,np,x) = p, then invibeta(a,b,np,p) = x
                               the inverse cumulative standard normal distribution: if normal(z)
invnormal(p)
                                  = p, then invnormal(p) = z
invnt(df, np, p)
                               the inverse cumulative noncentral Student's t distribution: if
                                  nt(df, np, t) = p, then invnt(df, np, p) = t
                               the inverse reverse cumulative (upper tail or survivor) noncen-
invnttail(df, np, p)
                                  tral Student's t distribution: if nttail(df, np, t) = p, then
                                  invnttail(df, np, p) = t
                               the Poisson mean such that the cumulative Poisson distribution eval-
invpoisson(k,p)
                                  uated at k is p: if poisson(m,k) = p, then invpoisson(k,p)
                               the Poisson mean such that the reverse cumulative Poisson distri-
invpoissontail(k,q)
                                  bution evaluated at k is q: if poissontail(m,k) = q, then
                                  invpoissontail(k,q) = m
                               the inverse cumulative Student's t distribution: if t(df,t) = p,
invt(df, p)
                                  then invt(df, p) = t
invttail(df, p)
                               the inverse reverse cumulative (upper tail or survivor) Student's
                                  t distribution: if ttail(df, t) = p, then invttail(df, p) = t
                               the inverse cumulative Tukey's Studentized range distribution with
invtukeyprob(k, df, p)
                                  k ranges and df degrees of freedom
                               the inverse cumulative Weibull distribution with shape a and scale
invweibull(a,b,p)
                                  b: if weibull(a,b,x) = p, then invweibull(a,b,p) = x
invweibull(a,b,g,p)
                               the inverse cumulative Weibull distribution with shape a, scale b,
                                  and location g: if weibull(a,b,g,x) = p, then
                                  invweibull(a,b,g,p) = x
                               the inverse cumulative Weibull (proportional hazards) distribution
invweibullph(a,b,p)
                                  with shape a and scale b: if weibullph(a,b,x) = p, then
                                  invweibullph(a,b,p) = x
                               the inverse cumulative Weibull (proportional hazards) distribution
invweibullph(a,b,g,p)
                                  with shape a, scale b, and location g: if weibullph(a,b,g,x) =
                                  p, then invweibullph(a,b,g,p) = x
                               the inverse reverse cumulative Weibull (proportional hazards) distri-
invweibullphtail(a,b,p)
                                  bution with shape a and scale b: if weibullphtail(a, b, x) = p,
                                  then invweibullphtail(a,b,p) = x
                               the inverse reverse cumulative Weibull (proportional hazards)
invweibullphtail(a,b,g,p)
                                  distribution with shape a, scale b, and location g: if
                                  weibullphtail(a,b,g,x) = p, then
                                  invweibullphtail(a,b,g,p) = x
invweibulltail(a, b, p)
                               the inverse reverse cumulative Weibull distribution with shape a and
                                  scale b: if weibulltail(a,b,x) = p, then
                                  invweibulltail(a,b,p) = x
                               the inverse reverse cumulative Weibull distribution with shape a,
invweibulltail(a, b, q, p)
                                  scale b, and location g: if weibulltail(a,b,g,x) = p, then
```

invweibulltail(a,b,g,p) = x

laplace(m,b,x)

```
laplaceden(m,b,x)
                                 the probability density of the Laplace distribution with mean m and
                                    scale parameter b
                                 the reverse cumulative (upper tail or survivor) Laplace distribution
laplacetail(m,b,x)
                                    with mean m and scale parameter b
lncauchyden(a,b,x)
                                 the natural logarithm of the density of the Cauchy distribution with
                                    location parameter a and scale parameter b
lnigammaden(a,b,x)
                                 the natural logarithm of the inverse gamma density, where a is the
                                    shape parameter and b is the scale parameter
                                 the natural logarithm of the inverse Gaussian density with mean m
lnigaussianden(m,a,x)
                                    and shape parameter a
lniwishartden(df, V, X)
                                 the natural logarithm of the density of the inverse Wishart distribu-
                                    tion; missing if df \leq n-1
                                 the natural logarithm of the density of the Laplace distribution with
lnlaplaceden(m,b,x)
                                    mean m and scale parameter b
lnmvnormalden(M, V, X)
                                 the natural logarithm of the multivariate normal density
                                 the natural logarithm of the cumulative standard normal distribution
lnnormal(z)
lnnormalden(z)
                                 the natural logarithm of the standard normal density, N(0,1)
lnnormalden(x,\sigma)
                                 the natural logarithm of the normal density with mean 0 and standard
                                    deviation \sigma
                                 the natural logarithm of the normal density with mean \mu and standard
lnnormalden(x, \mu, \sigma)
                                    deviation \sigma, N(\mu, \sigma^2)
lnwishartden(df, V, X)
                                 the natural logarithm of the density of the Wishart distribution;
                                    missing if df \leq n-1
                                 the cumulative logistic distribution with mean 0 and standard devi-
logistic(x)
                                    ation \pi/\sqrt{3}
                                 the cumulative logistic distribution with mean 0, scale s, and standard
logistic(s,x)
                                    deviation s\pi/\sqrt{3}
logistic(m,s,x)
                                 the cumulative logistic distribution with mean m, scale s, and
                                    standard deviation s\pi/\sqrt{3}
                                 the density of the logistic distribution with mean 0 and standard
logisticden(x)
                                    deviation \pi/\sqrt{3}
                                 the density of the logistic distribution with mean 0, scale s, and
logisticden(s,x)
                                    standard deviation s\pi/\sqrt{3}
                                 the density of the logistic distribution with mean m, scale s, and
logisticden(m,s,x)
                                    standard deviation s\pi/\sqrt{3}
logistictail(x)
                                 the reverse cumulative logistic distribution with mean 0 and standard
                                    deviation \pi/\sqrt{3}
                                 the reverse cumulative logistic distribution with mean 0, scale s,
logistictail(s,x)
                                    and standard deviation s\pi/\sqrt{3}
                                 the reverse cumulative logistic distribution with mean m, scale s,
logistictail(m,s,x)
                                    and standard deviation s\pi/\sqrt{3}
                                 the probability density function of the noncentral beta distribution;
nbetaden(a,b,np,x)
                                    0 if x < 0 or x > 1
nbinomial(n,k,p)
                                 the cumulative probability of the negative binomial distribution
```

the cumulative Laplace distribution with mean m and scale param-

```
nbinomialtail(n, k, p)
                                 the reverse cumulative probability of the negative binomial distri-
                                 the cumulative noncentral \chi^2 distribution; 0 if x < 0
nchi2(df, np, x)
                                 the probability density of the noncentral \chi^2 distribution; 0 if x < 0
nchi2den(df, np, x)
                                 the reverse cumulative (upper tail or survivor) noncentral \chi^2 distri-
nchi2tail(df, np, x)
                                    bution: 1 if x < 0
nF(df_1, df_2, np, f)
                                 the cumulative noncentral F distribution with df_1 numerator and
                                     df_2 denominator degrees of freedom and noncentrality parameter
                                    np; 0 if f < 0
nFden(df_1, df_2, np, f)
                                 the probability density function of the noncentral F distribution
                                     with df_1 numerator and df_2 denominator degrees of freedom and
                                     noncentrality parameter np; 0 if f < 0
nFtail(df_1, df_2, np, f)
                                 the reverse cumulative (upper tail or survivor) noncentral F dis-
                                    tribution with df_1 numerator and df_2 denominator degrees of
                                    freedom and noncentrality parameter np; 1 if f < 0
nibeta(a,b,np,x)
                                 the cumulative noncentral beta distribution; 0 if x < 0; or 1 if
                                    x > 1
normal(z)
                                 the cumulative standard normal distribution
normalden(z)
                                 the standard normal density, N(0,1)
normalden(x, \sigma)
                                 the normal density with mean 0 and standard deviation \sigma
normalden(x, \mu, \sigma)
                                 the normal density with mean \mu and standard deviation \sigma, N(\mu, \sigma^2)
                                 the noncentrality parameter, np, for noncentral \chi^2: if
npnchi2(df,x,p)
                                    nchi2(df, np, x) = p, then npnchi2(df, x, p) = np
npnF(df_1, df_2, f, p)
                                 the noncentrality parameter, np, for the noncentral F: if
                                    nF(df_1, df_2, np, f) = p, then npnF(df_1, df_2, f, p) = np
                                 the noncentrality parameter, np, for the noncentral Student's
npnt(df,t,p)
                                     t distribution: if nt(df, np, t) = p, then npnt(df, t, p) = np
nt(df, np, t)
                                 the cumulative noncentral Student's t distribution with df degrees
                                    of freedom and noncentrality parameter np
ntden(df, np, t)
                                 the probability density function of the noncentral Student's
                                     t distribution with df degrees of freedom and noncentrality pa-
                                    rameter np
nttail(df, np, t)
                                 the reverse cumulative (upper tail or survivor) noncentral Student's
                                     t distribution with df degrees of freedom and noncentrality pa-
                                    rameter np
poisson(m,k)
                                 the probability of observing floor(k) or fewer outcomes that are
                                    distributed as Poisson with mean m
                                 the probability of observing floor(k) outcomes that are distributed
poissonp(m,k)
                                     as Poisson with mean m
                                 the probability of observing floor(k) or more outcomes that are
poissontail(m,k)
                                     distributed as Poisson with mean m
t(df,t)
                                 the cumulative Student's t distribution with df degrees of freedom
tden(df,t)
                                 the probability density function of Student's t distribution
ttail(df,t)
                                 the reverse cumulative (upper tail or survivor) Student's t distribution;
                                    the probability T > t
                                 the cumulative Tukey's Studentized range distribution with k ranges
tukeyprob(k, df, x)
                                     and df degrees of freedom; 0 if x < 0
```

the negative binomial probability

nbinomialp(n,k,p)

weibull(a,b,x)
weibull (a,b,g,x)
weibullden(a,b,x)
weibullden(a,b,g,x)
weibullph(a,b,x)
weibullph(a,b,g,x)
$\verb weibullphden (a,b,x) $
weibullphden(a,b,g,x)
${\tt weibullphtail}(a,b,x)$
weibullphtail(a,b,g,x)
weibulltail(a,b,x)

weibulltail(a,b,q,x)

```
the cumulative Weibull distribution with shape a and scale b
```

the cumulative Weibull distribution with shape a, scale b, and location q

the probability density function of the Weibull distribution with shape a and scale b

the probability density function of the Weibull distribution with shape a, scale b, and location q

the cumulative Weibull (proportional hazards) distribution with shape \boldsymbol{a} and scale \boldsymbol{b}

the cumulative Weibull (proportional hazards) distribution with shape a, scale b, and location g

the probability density function of the Weibull (proportional hazards) distribution with shape a and scale b

the probability density function of the Weibull (proportional hazards) distribution with shape a, scale b, and location g

the reverse cumulative Weibull (proportional hazards) distribution with shape a and scale b

the reverse cumulative Weibull (proportional hazards) distribution with shape a, scale b, and location g

the reverse cumulative Weibull distribution with shape \boldsymbol{a} and scale \boldsymbol{b}

the reverse cumulative Weibull distribution with shape a, scale b, and location g

Functions

Statistical functions are listed alphabetically under the following headings:

Beta and noncentral beta distributions

Binomial distribution

Cauchy distribution

 χ^2 and noncentral χ^2 distributions

Dunnett's multiple range distribution

Exponential distribution

F and noncentral F distributions

Gamma distribution

Hypergeometric distribution

Inverse Gaussian distribution

Laplace distribution

Logistic distribution

Negative binomial distribution

Normal (Gaussian), binormal, and multivariate normal distributions

Poisson distribution

Student's t and noncentral Student's t distributions

Tukey's Studentized range distribution

Weibull distribution

Weibull (proportional hazards) distribution

Wishart distribution

Beta and noncentral beta distributions

betaden(a,b,x)

Description: the probability density of the beta distribution, where a and b are the shape parameters;

0 if x < 0 or x > 1

The probability density of the beta distribution is

$$\mathtt{betaden}(a,b,x) = \frac{x^{a-1}(1-x)^{b-1}}{\int_0^\infty t^{a-1}(1-t)^{b-1}dt} = \frac{\Gamma(a+b)}{\Gamma(a)\Gamma(b)}x^{a-1}(1-x)^{b-1}$$

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307

Domain x: -8e+307 to 8e+307; interesting domain is $0 \le x \le 1$

Range: 0 to 8e+307

ibeta(a,b,x)

Description: the cumulative beta distribution with shape parameters a and b; 0 if x < 0; or 1 if x > 1The cumulative beta distribution with shape parameters a and b is defined by

$$I_x(a,b) = \frac{\Gamma(a+b)}{\Gamma(a)\Gamma(b)} \int_0^x t^{a-1} (1-t)^{b-1} dt$$

ibeta() returns the regularized incomplete beta function, also known as the incomplete beta function ratio. The incomplete beta function without regularization is given by (gamma(a)*gamma(b)/gamma(a+b))*ibeta(a,b,x) or, better when a or b might be large, exp(lngamma(a)+lngamma(b)-lngamma(a+b))*ibeta(a,b,x).

Here is an example of the use of the regularized incomplete beta function. Although Stata has a cumulative binomial function (see binomial()), the probability that an event occurs k or fewer times in n trials, when the probability of one event is p, can be evaluated as cond(k==n,1,1-ibeta(k+1,n-k,p)). The reverse cumulative binomial (the probability that an event occurs k or more times) can be evaluated as cond(k==0,1,ibeta(k,n-k+1,p)). See Press et al. (2007, 270-273) for a more complete description and for suggested uses for this function.

Domain a: 1e-10 to 1e+17Domain b: 1e-10 to 1e+17

Domain x: -8e+307 to 8e+307; interesting domain is $0 \le x \le 1$

Range: 0 to 1

ibetatail(a,b,x)

Description: the reverse cumulative (upper tail or survivor) beta distribution with shape parameters a and b; 1 if x < 0; or 0 if x > 1

> The reverse cumulative (upper tail or survivor) beta distribution with shape parameters a and b is defined by

$$ibetatail(a,b,x) = 1 - ibeta(a,b,x) = \int_{x}^{1} betaden(a,b,t) dt$$

ibetatail() is also known as the complement to the incomplete beta function (ratio).

Domain a: 1e-10 to 1e+17 Domain b: 1e-10 to 1e+17

-8e+307 to 8e+307; interesting domain is $0 \le x \le 1$ Domain x:

Range: 0 to 1

invibeta(a,b,p)

Description: the inverse cumulative beta distribution: if ibeta(a,b,x) = p,

then invibeta(a,b,p) = x

Domain a: 1e-10 to 1e+17 Domain b: 1e-10 to 1e+17

Domain p: 0 to 1 Range: 0 to 1

invibetatail(a,b,p)

Description: the inverse reverse cumulative (upper tail or survivor) beta distribution: if

ibetatail(a,b,x) = p, then invibetatail(a,b,p) = x

Domain a: 1e-10 to 1e+17 Domain b: 1e-10 to 1e+17

Domain p: 0 to 1 Range: 0 to 1

nbetaden(a,b,np,x)

Description: the probability density function of the noncentral beta distribution; 0 if x < 0 or x > 1

The probability density function of the noncentral beta distribution is defined as

$$\sum_{i=0}^{\infty} \frac{e^{-np/2} (np/2)^{j}}{\Gamma(j+1)} \left\{ \frac{\Gamma(a+b+j)}{\Gamma(a+j)\Gamma(b)} x^{a+j-1} (1-x)^{b-1} \right\}$$

where a and b are shape parameters, np is the noncentrality parameter, and x is the value of a beta random variable.

nbetaden(a,b,0,x) = betaden(a,b,x), but betaden() is the preferred function to use for the central beta distribution. nbetaden() is computed using an algorithm described in Johnson, Kotz, and Balakrishnan (1995).

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307

Domain np: 0 to 1,000

Domain x: -8e+307 to 8e+307; interesting domain is $0 \le x \le 1$

Range: 0 to 8e+307

nibeta(a,b,np,x)

Description: the cumulative noncentral beta distribution; 0 if x < 0; or 1 if x > 1

The cumulative noncentral beta distribution is defined as

$$I_x(a, b, np) = \sum_{j=0}^{\infty} \frac{e^{-np/2}(np/2)^j}{\Gamma(j+1)} I_x(a+j, b)$$

where a and b are shape parameters, np is the noncentrality parameter, x is the value of a beta random variable, and $I_x(a,b)$ is the cumulative beta distribution, ibeta().

 $\mathtt{nibeta}(a,b,0,x) = \mathtt{ibeta}(a,b,x)$, but $\mathtt{ibeta}()$ is the preferred function to use for the central beta distribution. $\mathtt{nibeta}()$ is computed using an algorithm described in Johnson, Kotz, and Balakrishnan (1995).

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307

Domain np: 0 to 10,000

Domain x: -8e+307 to 8e+307; interesting domain is $0 \le x \le 1$

invnibeta(a,b,np,p)

Description: the inverse cumulative noncentral beta distribution: if

nibeta(a,b,np,x) = p, then invibeta(a,b,np,p) = x

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307

Domain np: 0 to 1,000 Domain p: 0 to 1

Range: 0 to 1

Binomial distribution

binomialp(n,k,p)

Description: the probability of observing floor(k) successes in floor(n) trials when the

probability of a success on one trial is p

Domain n: 1 to 1e+6 Domain k: 0 to n Domain p: 0 to 1 Range: 0 to 1

binomial (n, k, θ)

Description: the probability of observing floor(k) or fewer successes in floor(n) trials when

the probability of a success on one trial is θ ; 0 if k < 0; or 1 if k > n

Domain n: 0 to 1e+17

Domain k: -8e+307 to 8e+307; interesting domain is $0 \le k < n$

Domain θ : 0 to 1 Range: 0 to 1

binomialtail (n, k, θ)

Description: the probability of observing floor(k) or more successes in floor(n) trials when

the probability of a success on one trial is θ ; 1 if k < 0; or 0 if k > n

Domain n: 0 to 1e+17

Domain k: -8e+307 to 8e+307; interesting domain is $0 \le k \le n$

Domain θ : 0 to 1 Range: 0 to 1

invbinomial(n, k, p)

Description: the inverse of the cumulative binomial; that is, θ (θ = probability of success on

one trial) such that the probability of observing floor(k) or fewer successes in

floor(n) trials is p

Domain n: 1 to 1e+17 Domain k: 0 to n-1

Domain p: 0 to 1 (exclusive)

invbinomialtail (n, k, p)

Description: the inverse of the right cumulative binomial; that is, θ (θ = probability of success

on one trial) such that the probability of observing floor(k) or more successes in

floor(n) trials is p

Domain n: 1 to 1e+17 Domain k: 1 to n

Domain p: 0 to 1 (exclusive)

Range: 0 to 1

Cauchy distribution

cauchyden(a,b,x)

Description: the probability density of the Cauchy distribution with location parameter a and scale

parameter b

Domain *a*: -1e+300 to 1e+300 Domain *b*: 1e-100 to 1e+300 Domain *x*: -8e+307 to 8e+307 Range: 0 to 8e+307

cauchy (a,b,x)

Description: the cumulative Cauchy distribution with location parameter a and scale parameter b

Domain a: -1e+300 to 1e+300Domain b: 1e-100 to 1e+300Domain x: -8e+307 to 8e+307

Range: 0 to 1

cauchytail(a,b,x)

Description: the reverse cumulative (upper tail or survivor) Cauchy distribution with location

parameter a and scale parameter b

cauchytail(a,b,x) = 1 - cauchy(a,b,x)

Domain a: -1e+300 to 1e+300Domain b: 1e-100 to 1e+300Domain x: -8e+307 to 8e+307

Range: 0 to 1

invcauchy(a,b,p)

Description: the inverse of cauchy(): if cauchy(a,b,x) = p, then

invcauchy(a,b,p) = x

Domain a: -1e+300 to 1e+300
Domain b: 1e-100 to 1e+300
Domain p: 0 to 1 (exclusive)
Range: -8e+307 to 8e+307

invcauchytail(a,b,p)

Description: the inverse of cauchytail(): if cauchytail(a,b,x) = p, then

invcauchytail(a,b,p) = x

Domain *a*: -1e+300 to 1e+300 Domain *b*: 1e-100 to 1e+300 Domain *p*: 0 to 1 (exclusive) Range: -8e+307 to 8e+307

lncauchyden(a,b,x)

Description: the natural logarithm of the density of the Cauchy distribution with location parameter

a and scale parameter b

Domain *a*: -1e+300 to 1e+300 Domain *b*: 1e-100 to 1e+300 Domain *x*: -8e+307 to 8e+307 Range: -1650 to 230

Augustin-Louis Cauchy (1789–1857) was born in Paris, France. He obtained a degree in engineering with honors from École Polytechnique, where he would later teach mathematics. While working as a military engineer, he published two papers on polyhedra, one of which was a solution to a problem presented to him by Joseph-Louis Lagrange. In 1816, he won the Grand Prix for his work on wave propagation.

Cauchy's contributions were numerous and far reaching, as evident by the many concepts and theorems named after him. Some examples include the Cauchy criterion for convergence, Cauchy's theorem for finite groups, the Cauchy distribution, and the Cauchy stress tensor. His contributions were so vast that once all of his work was collected, it comprised 27 volumes. His name is engraved on the Eiffel Tower, along with 71 other scientists and mathematicians.

χ^2 and noncentral χ^2 distributions

chi2den(df,x)

Description: the probability density of the χ^2 distribution with df degrees of freedom; 0 if x < 0

 $\mathtt{chi2den}(df,x) = \mathtt{gammaden}(df/2,2,0,x)$

Domain df: 2e-10 to 2e+17 (may be nonintegral)

Domain x: -8e+307 to 8e+307

Range: 0 to 8e+307

 ${\tt chi2}(df,x)$

Description: the cumulative χ^2 distribution with df degrees of freedom; 0 if x < 0

chi2(df,x) = gammap(df/2,x/2)

Domain df: 2e-10 to 2e+17 (may be nonintegral)

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge 0$

chi2tail(df,x)

Description: the reverse cumulative (upper tail or survivor) χ^2 distribution with df degrees of

freedom; 1 if x < 0

chi2tail(df,x) = 1 - chi2(df,x)Domain df: 2e–10 to 2e+17 (may be nonintegral)

Domain x: -8e+307 to 8e+307; interesting domain is x > 0

Range: 0 to 1

invchi2(df,p)

Description: the inverse of chi2(): if chi2(df,x) = p, then invchi2(df,p) = x

Domain df: 2e-10 to 2e+17 (may be nonintegral)

Domain p: 0 to 1

0 to 8e+307 Range:

invchi2tail(df, p)

Description: the inverse of chi2tail(): if chi2tail(df,x) = p, then invchi2tail(df,p) =

Domain df: $\overset{\sim}{2}e-10$ to 2e+17 (may be nonintegral)

Domain p: 0 to 1

0 to 8e + 307Range:

nchi2den(df, np, x)

Description: the probability density of the noncentral χ^2 distribution; 0 if x < 0

df denotes the degrees of freedom, np is the noncentrality parameter, and x is the value of χ^2 .

nchi2den(df,0,x) = chi2den(df,x), but chi2den() is the preferred function to use for the central χ^2 distribution.

Domain df: 2e–10 to 1e+6 (may be nonintegral)

Domain np: 0 to 10,000

Domain x: -8e+307 to 8e+307

0 to 8e+307 Range:

nchi2(df, np, x)

Description: the cumulative noncentral χ^2 distribution; 0 if x < 0

The cumulative noncentral χ^2 distribution is defined as

$$\int_0^x \frac{e^{-t/2} \, e^{-np/2}}{2^{d\!f/2}} \, \sum_{j=0}^\infty \frac{t^{d\!f/2+j-1} \, np^j}{\Gamma(d\!f/2+j) \, 2^{2j} \, j!} \, dt$$

where df denotes the degrees of freedom, np is the noncentrality parameter, and xis the value of χ^2 .

nchi2(df,0,x) = chi2(df,x), but chi2() is the preferred function to use for the

central χ^2 distribution. Domain df: 2e-10 to 1e+6 (may be nonintegral)

Domain np: 0 to 10,000

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge 0$

nchi2tail(df, np, x)

Description: the reverse cumulative (upper tail or survivor) noncentral χ^2 distribution; 1 if x < 0

df denotes the degrees of freedom, np is the noncentrality parameter, and x is the

value of χ^2 .

Domain df: 2e–10 to 1e+6 (may be nonintegral)

Domain np: 0 to 10,000

Domain x: -8e+307 to 8e+307

Range: 0 to 1

invnchi2(df, np, p)

Description: the inverse cumulative noncentral χ^2 distribution: if

nchi2(df, np, x) = p, then invnchi2(df, np, p) = x

Domain df: 2e–10 to 1e+6 (may be nonintegral)

Domain np: 0 to 10,000 Domain p: 0 to 1 Range: 0 to 8e+307

Range. 0 to 60 1307

invnchi2tail(df, np, p)

Description: the inverse reverse cumulative (upper tail or survivor) noncentral χ^2 distribution: if

nchi2tail(df, np, x) = p, then invnchi2tail(df, np, p) = x

Domain df: 2e–10 to 1e+6 (may be nonintegral)

Domain np: 0 to 10,000 Domain p: 0 to 1 Range: 0 to 8e+307

npnchi2(df,x,p)

Description: the noncentrality parameter, np, for noncentral χ^2 : if

nchi2(df, np, x) = p, then npnchi2(df, x, p) = np

Domain df: 2e–10 to 1e+6 (may be nonintegral)

Domain *x*: 0 to 8e+307 Domain *p*: 0 to 1 Range: 0 to 10,000

Dunnett's multiple range distribution

dunnettprob(k, df, x)

Description: the cumulative multiple range distribution that is used in Dunnett's multiple-comparison

method with k ranges and df degrees of freedom; 0 if x < 0

dunnettprob() is computed using an algorithm described in Miller (1981).

Domain k: 2 to 1e+6 Domain df: 2 to 1e+6

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge 0$

invdunnettprob(k, df, p)

Description: the inverse cumulative multiple range distribution that is used in Dunnett's multiple-

comparison method with k ranges and df degrees of freedom

If dunnettprob(k, df, x) = p, then involunnettprob(k, df, p) = x.

invdunnettprob() is computed using an algorithm described in Miller (1981).

Domain k: 2 to 1e+6 Domain df: 2 to 1e+6

Domain p: 0 to 1 (right exclusive)

Range: 0 to 8e+307

Charles William Dunnett (1921–2007) was a Canadian statistician best known for his work on multiple-comparison procedures. He was born in Windsor, Ontario, and graduated in mathematics and physics from McMaster University. After naval service in World War II, Dunnett's career included further graduate work, teaching, and research at Toronto, Columbia, the New York State Maritime College, the Department of National Health and Welfare in Ottawa, Cornell, Lederle Laboratories, and Aberdeen before he became Professor of Clinical Epidemiology and Biostatistics at McMaster University in 1974. He was President and Gold Medalist of the Statistical Society of Canada. Throughout his career, Dunnett took a keen interest in computing. According to Google Scholar, his 1955 paper on comparing treatments with a control has been cited over 4,000 times.

Exponential distribution

exponentialden(b,x)

Description: the probability density function of the exponential distribution with scale b

The probability density function of the exponential distribution is

$$\frac{1}{b}\exp(-x/b)$$

where b is the scale and x is the value of an exponential variate.

Domain *b*: 1e–323 to 8e+307

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge 0$

Range: 1e-323 to 8e+307

exponential(b,x)

Description: the cumulative exponential distribution with scale b

The cumulative distribution function of the exponential distribution is

$$1 - \exp(-x/b)$$

for $x \ge 0$ and 0 for x < 0, where b is the scale and x is the value of an exponential variate

The mean of the exponential distribution is b and its variance is b^2 .

Domain *b*: 1e-323 to 8e+307

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge 0$

exponential tail(b,x)

Description: the reverse cumulative exponential distribution with scale b

The reverse cumulative distribution function of the exponential distribution is

$$\exp(-x/b)$$

where b is the scale and x is the value of an exponential variate.

Domain *b*: 1e–323 to 8e+307

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge 0$

Range: 0 to 1

invexponential(b, p)

Description: the inverse cumulative exponential distribution with scale b: if

exponential (b,x) = p, then invexponential (b,p) = x

Domain *b*: 1e–323 to 8e+307

Domain p: 0 to 1

Range: 1e-323 to 8e+307

invexponentialtail(b, p)

Description: the inverse reverse cumulative exponential distribution with scale b:

if exponentialtail(b,x) = p, then invexponentialtail(b,p) = x

Domain *b*: $1e-32\frac{1}{3}$ to 8e+307

Domain p: 0 to 1

Range: 1e-323 to 8e+307

F and noncentral F distributions

Fden (df_1, df_2, f)

Description: the probability density function of the F distribution with df_1 numerator and df_2 denominator degrees of freedom; 0 if f < 0

The probability density function of the F distribution with df_1 numerator and df_2 denominator degrees of freedom is defined as

$$\mathtt{Fden}(\mathit{d}f_1,\mathit{d}f_2,f) = \frac{\Gamma(\frac{\mathit{d}f_1+\mathit{d}f_2}{2})}{\Gamma(\frac{\mathit{d}f_1}{2})\Gamma(\frac{\mathit{d}f_2}{2})} \bigg(\frac{\mathit{d}f_1}{\mathit{d}f_2}\bigg)^{\frac{\mathit{d}f_1}{2}} \cdot f^{\frac{\mathit{d}f_1}{2}-1} \bigg(1 + \frac{\mathit{d}f_1}{\mathit{d}f_2}f\bigg)^{-\frac{1}{2}(\mathit{d}f_1+\mathit{d}f_2)}$$

Domain df_1 : 1e–323 to 8e+307 (may be nonintegral) Domain df_2 : 1e–323 to 8e+307 (may be nonintegral)

Domain f: -8e+307 to 8e+307; interesting domain is $f \ge 0$

Range: 0 to 8e+307

$F(df_1, df_2, f)$

Description: the cumulative F distribution with df_1 numerator and df_2 denominator degrees of

freedom: F(df_1 , df_2 ,f) = \int_0^f Fden(df_1 , df_2 ,t) dt; 0 if f<0 Domain df_1 : 2e-10 to 2e+17 (may be nonintegral)

Domain df_2 : 2e–10 to 2e+17 (may be nonintegral)

Domain f: -8e+307 to 8e+307; interesting domain is $f \ge 0$

Range: 0 to 1

Ftail(df_1, df_2, f)

Description: the reverse cumulative (upper tail or survivor) F distribution with df_1 numerator and df_2 denominator degrees of freedom; 1 if f < 0

Ftail(df_1, df_2, f) = 1 - F(df_1, df_2, f).

Domain df_1 : 2e–10 to 2e+17 (may be nonintegral) Domain df_2 : 2e–10 to 2e+17 (may be nonintegral)

Domain f: -8e+307 to 8e+307; interesting domain is $f \ge 0$

Range: 0 to 1

$invF(df_1, df_2, p)$

Description: the inverse cumulative F distribution: if $F(df_1, df_2, f) = p$, then

 $invF(df_1, df_2, p) = f$

Domain df_1 : 2e–10 to 2e+17 (may be nonintegral) Domain df_2 : 2e–10 to 2e+17 (may be nonintegral)

Domain p: 0 to 1

0 to 8e+307 Range:

invFtail(df_1, df_2, p)

Description: the inverse reverse cumulative (upper tail or survivor) F distribution:

if Ftail(df_1, df_2, f) = p, then invFtail(df_1, df_2, p) = f

Domain df_1 : 2e–10 to 2e+17 (may be nonintegral) Domain df_2 : 2e–10 to 2e+17 (may be nonintegral)

Domain p: 0 to 1

0 to 8e+307 Range:

 $nFden(df_1, df_2, np, f)$

Description: the probability density function of the noncentral F distribution with df_1 numerator and df_2 denominator degrees of freedom and noncentrality parameter np; 0 if f < 0

nFden $(df_1, df_2, 0, f)$ = Fden (df_1, df_2, f) , but Fden() is the preferred function to use for the central F distribution.

Also, if F follows the noncentral F distribution with df_1 and df_2 degrees of freedom and noncentrality parameter np, then

$$\frac{df_1F}{df_2 + df_1F}$$

follows a noncentral beta distribution with shape parameters $a=df_1/2$, $b=df_2/2$, and noncentrality parameter np, as given in nbetaden(). nFden() is computed based on this relationship.

Domain df_1 : 1e–323 to 8e+307 (may be nonintegral) Domain df_2 : 1e–323 to 8e+307 (may be nonintegral)

Domain np: 0 to 1,000

Domain f: -8e+307 to 8e+307; interesting domain is $f \ge 0$

Range: 0 to 8e+307

 $nF(df_1, df_2, np, f)$

Description: the cumulative noncentral F distribution with df_1 numerator and df_2 denominator degrees of freedom and noncentrality parameter np; 0 if f < 0

$$\mathtt{nF}(\mathit{df}_1,\mathit{df}_2,\mathtt{0},f) = \mathtt{F}(\mathit{df}_1,\mathit{df}_2,f)$$

nF() is computed using nibeta() based on the relationship between the noncentral beta and noncentral F distributions: nF(df_1 , df_2 , np, f) = nibeta($df_1/2$, $df_2/2$, np, $df_1 \times f/\{(df_1 \times f) + df_2\}$).

Domain df_1 : 2e–10 to 1e+8 Domain df_2 : 2e–10 to 1e+8 Domain np: 0 to 10,000

Domain f: -8e+307 to 8e+307

Range: 0 to 1

 $nFtail(df_1, df_2, np, f)$

Description: the reverse cumulative (upper tail or survivor) noncentral F distribution with df_1 numerator and df_2 denominator degrees of freedom and noncentrality parameter np; 1 if f < 0

nFtail() is computed using nibeta() based on the relationship between the noncentral beta and F distributions. See Johnson, Kotz, and Balakrishnan (1995) for more details

more details. Domain df_1 : 1e-323 to 8e+307 (may be nonintegral) Domain df_2 : 1e-323 to 8e+307 (may be nonintegral)

Domain np: 0 to 1,000

Domain f: -8e+307 to 8e+307; interesting domain is $f \ge 0$

 $invnF(df_1, df_2, np, p)$

Description: the inverse cumulative noncentral F distribution: if

 $\operatorname{nF}(df_1, df_2, np, f) = p$, then $\operatorname{invnF}(df_1, df_2, np, p) = f$

Domain df_1 : 1e–6 to 1e+6 (may be nonintegral) Domain df_2 : 1e–6 to 1e+6 (may be nonintegral)

Domain np: 0 to 10,000 Domain p: 0 to 1 Range: 0 to 8e+307

 $invnFtail(df_1, df_2, np, p)$

Description: the inverse reverse cumulative (upper tail or survivor) noncentral F distribution: if

 $nFtail(df_1, df_2, np, f) = p$, then $invnFtail(df_1, df_2, np, p) = f$

Domain df_1 : 1e–323 to 8e+307 (may be nonintegral) Domain df_2 : 1e–323 to 8e+307 (may be nonintegral)

Domain np: 0 to 1,000 Domain p: 0 to 1 Range: 0 to 8e+307

 $npnF(df_1, df_2, f, p)$

Description: the noncentrality parameter, np, for the noncentral F: if

 $\operatorname{nF}(df_1, df_2, np, f) = p$, then $\operatorname{npnF}(df_1, df_2, f, p) = np$

Domain df_1 : 2e–10 to 1e+6 (may be nonintegral) Domain df_2 : 2e–10 to 1e+6 (may be nonintegral)

Domain f: 0 to 8e+307 Domain p: 0 to 1 Range: 0 to 1,000

Gamma distribution

gammaden(a,b,g,x)

Description: the probability density function of the gamma distribution; 0 if x < g

The probability density function of the gamma distribution is defined by

$$\frac{1}{\Gamma(a)b^{a}}(x-g)^{a-1}e^{-(x-g)/b}$$

where a is the shape parameter, b is the scale parameter, and g is the location parameter.

Domain a: 1e–323 to 8e+307

Domain *b*: 1e–323 to 8e+307 Domain *a*: –8e+307 to 8e+307

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge g$

Range: 0 to 8e+307

gammap(a,x)

Description: the cumulative gamma distribution with shape parameter a; 0 if x < 0

The cumulative gamma distribution with shape parameter a is defined by

$$\frac{1}{\Gamma(a)} \int_0^x e^{-t} t^{a-1} dt$$

The cumulative Poisson (the probability of observing k or fewer events if the expected is x) can be evaluated as 1-gammap(k+1,x). The reverse cumulative (the probability of observing k or more events) can be evaluated as gammap(k,x). See Press et al. (2007, 259–266) for a more complete description and for suggested uses for this function.

gammap() is also known as the incomplete gamma function (ratio).

Probabilities for the three-parameter gamma distribution (see gammaden()) can be calculated by shifting and scaling x; that is, gammap(a,(x-q)/b).

Domain a: 1e–10 to 1e+17

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge 0$

Range: 0 to 1

gammaptail(a,x)

Description: the reverse cumulative (upper tail or survivor) gamma distribution with shape parameter a: 1 if x < 0

The reverse cumulative (upper tail or survivor) gamma distribution with shape parameter a is defined by

$$\mathtt{gammaptail}(a,x) = 1 - \mathtt{gammap}(a,x) = \int_x^\infty \mathtt{gammaden}(a,t) \ dt$$

gammaptail() is also known as the complement to the incomplete gamma function (ratio).

Domain a: 1e-10 to 1e+17

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge 0$

Range: 0 to 1

invgammap(a,p)

Description: the inverse cumulative gamma distribution: if gammap (a, x) = p,

then invgammap(a, p) = x

Domain a: 1e–10 to 1e+17

Domain p: 0 to 1

Range: 0 to 8e+307

invgammaptail(a,p)

Description: the inverse reverse cumulative (upper tail or survivor) gamma distribution: if

gammaptail(a,x) = p, then invgammaptail(a,p) = x

Domain *a*: 1e-10 to 1e+17

Domain p: 0 to 1

Range: 0 to 8e+307

dgammapda(a,x)

Description: $\frac{\partial P(a,x)}{\partial a}$, where $P(a,x)=\mathrm{gammap}(a,x)$; 0 if x<0

Domain a: 1e-7 to 1e+17

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge 0$

Range: -16 to 0

dgammapdada(a,x)

Description: $\frac{\partial^2 P(a,x)}{\partial a^2}$, where $P(a,x)=\mathrm{gammap}(a,x)$; 0 if x<0

Domain a: 1e-7 to 1e+17

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge 0$

Range: -0.02 to 4.77e+5

dgammapdadx(a,x)

Description: $\frac{\partial^2 P(a,x)}{\partial a \partial x}$, where P(a,x) = gammap(a,x); 0 if x < 0

Domain a: 1e-7 to 1e+17

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge 0$

Range: -0.04 to 8e+307

dgammapdx(a,x)

Description: $\frac{\partial P(a,x)}{\partial x}$, where P(a,x) = gammap(a,x); 0 if x < 0

Domain a: 1e–10 to 1e+17

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge 0$

Range: 0 to 8e+307

dgammapdxdx(a,x)

Description: $\frac{\partial^2 P(a,x)}{\partial x^2}$, where P(a,x) = gammap(a,x); 0 if x < 0

Domain a: 1e–10 to 1e+17

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge 0$

Range: 0 to 1e+40

lnigammaden(a,b,x)

Description: the natural logarithm of the inverse gamma density, where a is the shape parameter

and b is the scale parameter

Domain *a*: 1e–300 to 1e+300
Domain *b*: 1e–300 to 1e+300
Domain *x*: 1e–300 to 8e+307
Range: -8e+307 to 8e+307

hypergeometricp(N, K, n, k)

Description: the hypergeometric probability of k successes out of a sample of size n, from a

population of size N containing K elements that have the attribute of interest

Success is obtaining an element with the attribute of interest.

Domain N: 2 to 1e+5 Domain K: 1 to N-1Domain n: 1 to N-1

Domain k: $\max(0, n - N + K)$ to $\min(K, n)$

Range: 0 to 1 (right exclusive)

hypergeometric (N, K, n, k)

Description: the cumulative probability of the hypergeometric distribution

N is the population size, K is the number of elements in the population that have the attribute of interest, and n is the sample size. Returned is the probability of observing k or fewer elements from a sample of size n that have the attribute of interest.

Domain N: 2 to 1e+5 Domain K: 1 to N-1Domain n: 1 to N-1

Domain k: $\max(0, n - N + K)$ to $\min(K, n)$

Range: 0 to 1

Inverse Gaussian distribution

igaussianden(m,a,x)

Description: the probability density of the inverse Gaussian distribution with mean m and shape

parameter a; 0 if x < 0

Domain m: 1e-323 to 8e+307 Domain a: 1e-323 to 8e+307 Domain x: -8e+307 to 8e+307

Range: 0 to 8e+307

igaussian(m,a,x)

Description: the cumulative inverse Gaussian distribution with mean m and shape parameter a; 0

if $x \leq 0$

Domain m: $1e-3\overline{2}3$ to 8e+307Domain a: 1e-323 to 8e+307Domain x: -8e+307 to 8e+307

Range: 0 to 1

igaussiantail(m,a,x)

Description: the reverse cumulative (upper tail or survivor) inverse Gaussian distribution with

mean m and shape parameter a; 1 if $x \le 0$

igaussiantail(m,a,x) = 1 - igaussian(m,a,x)

Domain *m*: 1e–323 to 8e+307 Domain *a*: 1e–323 to 8e+307 Domain *x*: -8e+307 to 8e+307

invigaussian(m,a,p)

Description: the inverse of igaussian(): if

igaussian(m,a,x)=p, then invigaussian(m,a,p)=x

Domain *m*: 1e–323 to 8e+307 Domain *a*: 1e–323 to 1e+8 Domain *p*: 0 to 1 (exclusive) Range: 0 to 8e+307

invigaussiantail(m, a, p)

Description: the inverse of igaussiantail(): if

igaussiantail(m,a,x) = p, then invigaussiantail(m,a,p) = x

Domain m: 1e–323 to 8e+307 Domain a: 1e–323 to 1e+8 Domain p: 0 to 1 (exclusive) Range: 0 to 8e+307

lnigaussianden(m,a,x)

Description: the natural logarithm of the inverse Gaussian density with mean m and shape

parameter a

Domain *m*: 1e–323 to 8e+307 Domain *a*: 1e–323 to 8e+307 Domain *x*: 1e–323 to 8e+307 Range: –8e+307 to 8e+307

Laplace distribution

laplaceden(m,b,x)

Description: the probability density of the Laplace distribution with mean m and scale parameter b

Domain *m*: -8e+307 to 8e+307 Domain *b*: 1e-307 to 8e+307 Domain *x*: -8e+307 to 8e+307 Range: 0 to 8e+307

laplace(m,b,x)

Description: the cumulative Laplace distribution with mean m and scale parameter b

Domain *m*: -8e+307 to 8e+307 Domain *b*: 1e-307 to 8e+307 Domain *x*: -8e+307 to 8e+307

Range: 0 to 1

laplacetail(m,b,x)

Description: the reverse cumulative (upper tail or survivor) Laplace distribution with mean m and

scale parameter b

laplacetail(m,b,x) = 1 - laplace(m,b,x)

Domain m: -8e+307 to 8e+307Domain b: 1e-307 to 8e+307Domain x: -8e+307 to 8e+307

invlaplace(m,b,p)

Description: the inverse of laplace(): if laplace(m, b, x) = p, then

 $\mathtt{invlaplace}(m,b,p)=x$

Domain m: -8e+307 to 8e+307Domain b: 1e-307 to 8e+307Domain p: 0 to 1 (exclusive) Range: -8e+307 to 8e+307

invlaplacetail(m,b,p)

Description: the inverse of laplacetail(): if laplacetail(m, b, x) = p,

then invlaplacetail(m, b, p) = x

Domain m: -8e+307 to 8e+307Domain b: 1e-307 to 8e+307Domain p: 0 to 1 (exclusive) Range: -8e+307 to 8e+307

lnlaplaceden(m,b,x)

Description: the natural logarithm of the density of the Laplace distribution with mean m and scale parameter b

Domain m: -8e+307 to 8e+307Domain b: 1e-307 to 8e+307Domain x: -8e+307 to 8e+307Range: -8e+307 to 707

Logistic distribution

logisticden(x)

Description: the density of the logistic distribution with mean 0 and standard deviation $\pi/\sqrt{3}$

logisticden(x) = logisticden(1,x) = logisticden(0,1,x), where x is

the value of a logistic random variable.

Domain x: -8e+307 to 8e+307

Range: 0 to 0.25

logisticden(s,x)

Description: the density of the logistic distribution with mean 0, scale s, and standard deviation

 $s\pi/\sqrt{3}$

logisticden(s,x) = logisticden(0,s,x), where s is the scale and x is the value of a logistic random variable.

Domain *s*: 1e–323 to 8e+307 Domain *x*: -8e+307 to 8e+307

Range: 0 to 8e+307

logisticden(m,s,x)

Description: the density of the logistic distribution with mean m, scale s, and standard deviation

 $s\pi/\sqrt{3}$

The density of the logistic distribution is defined as

$$\frac{\exp\{-(x-m)/s\}}{s[1+\exp\{-(x-m)/s\}]^2}$$

where m is the mean, s is the scale, and x is the value of a logistic random variable.

Domain m: -8e+307 to 8e+307Domain s: 1e-323 to 8e+307Domain x: -8e+307 to 8e+307Range: 0 to 8e+307

logistic(x)

Description: the cumulative logistic distribution with mean 0 and standard deviation $\pi/\sqrt{3}$

logistic(x) = logistic(1,x) = logistic(0,1,x), where x is the value of a logistic random variable.

Domain x: -8e+307 to 8e+307

Range: 0 to 1

logistic(s,x)

Description: the cumulative logistic distribution with mean 0, scale s, and standard deviation

 $s\pi/\sqrt{3}$

logistic(s, x) = logistic(0, s, x), where s is the scale and x is the value of a logistic random variable.

Domain s: 1e–323 to 8e+307 Domain x: -8e+307 to 8e+307

Range: 0 to 1

logistic(m,s,x)

Description: the cumulative logistic distribution with mean m, scale s, and standard deviation $s\pi/\sqrt{3}$

The cumulative logistic distribution is defined as

$$[1 + \exp{-(x-m)/s}]^{-1}$$

where m is the mean, s is the scale, and x is the value of a logistic random variable.

Domain m: -8e+307 to 8e+307Domain s: 1e-323 to 8e+307Domain x: -8e+307 to 8e+307

logistictail(x)

Description: the reverse cumulative logistic distribution with mean 0 and standard deviation $\pi/\sqrt{3}$

logistictail(x) = logistictail(1,x) = logistictail(0,1,x), where xis the value of a logistic random variable.

Domain x: -8e+307 to 8e+307

0 to 1 Range:

logistictail(s,x)

Description: the reverse cumulative logistic distribution with mean 0, scale s, and standard deviation

$$s\pi/\sqrt{3}$$

logistictail(s,x) = logistictail(0,s,x), where s is the scale and x is the value of a logistic random variable.

1e-323 to 8e+307 Domain s: Domain x: -8e+307 to 8e+307

0 to 1 Range:

logistictail(m,s,x)

Description: the reverse cumulative logistic distribution with mean m, scale s, and standard deviation $s\pi/\sqrt{3}$

The reverse cumulative logistic distribution is defined as

$$[1 + \exp\{(x - m)/s\}]^{-1}$$

where m is the mean, s is the scale, and x is the value of a logistic random variable.

Domain m: -8e+307 to 8e+307Domain s: 1e-323 to 8e+307 Domain x: -8e+307 to 8e+307

Range: 0 to 1

invlogistic(p)

Description: the inverse cumulative logistic distribution: if logistic(x) = p,

then invlogistic(p) = x

Domain p: 0 to 1

-8e+307 to 8e+307Range:

invlogistic(s,p)

Description: the inverse cumulative logistic distribution: if logistic(s,x) = p, then

invlogistic(s,p) = x

Domain s: 1e-323 to 8e+307

Domain p: 0 to 1

-8e+307 to 8e+307Range:

```
invlogistic (m, s, p)
Description: the inv
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Description: the inverse cumulative logistic distribution: if logistic(m,s,x) = p, then

invlogistic(m,s,p) = x

Domain m: -8e+307 to 8e+307Domain s: 1e-323 to 8e+307

Domain p: 0 to 1

Range: -8e+307 to 8e+307

invlogistictail(p)

Description: the inverse reverse cumulative logistic distribution: if

logistictail(x) = p, then invlogistictail(p) = x

Domain p: 0 to 1

Range: -8e+307 to 8e+307

invlogistictail(s, p)

Description: the inverse reverse cumulative logistic distribution: if

logistictail(s,x) = p, then invlogistictail(s,p) = x

Domain s: 1e–323 to 8e+307

Domain p: 0 to 1

Range: -8e+307 to 8e+307

invlogistictail(m,s,p)

Description: the inverse reverse cumulative logistic distribution: if

logistictail(m,s,x) = p, then invlogistictail(m,s,p) = x

Domain m: -8e+307 to 8e+307Domain s: 1e-323 to 8e+307

Domain p: 0 to 1

Range: -8e+307 to 8e+307

Negative binomial distribution

nbinomialp(n, k, p)

Description: the negative binomial probability

When n is an integer, nbinomialp() returns the probability of observing exactly floor(k) failures before the nth success when the probability of a success on one

trial is p.

Domain n: 1e–10 to 1e+6 (can be nonintegral)

Domain k: 0 to 1e+10

Domain p: 0 to 1 (left exclusive)

nbinomial(n,k,p)

Description: the cumulative probability of the negative binomial distribution

n can be nonintegral. When n is an integer, nbinomial() returns the probability of observing k or fewer failures before the nth success, when the probability of a success on one trial is p.

The negative binomial distribution function is evaluated using ibeta().

Domain n: 1e–10 to 1e+17 (can be nonintegral)

Domain k: 0 to $2^{53} - 1$

Domain p: 0 to 1 (left exclusive)

Range: 0 to 1

nbinomialtail(n, k, p)

Description: the reverse cumulative probability of the negative binomial distribution

When n is an integer, nbinomialtail() returns the probability of observing k or more failures before the nth success, when the probability of a success on one trial is p.

The reverse negative binomial distribution function is evaluated using ibetatail().

Domain n: 1e–10 to 1e+17 (can be nonintegral)

Domain k: 0 to $2^{53} - 1$

Domain p: 0 to 1 (left exclusive)

Range: 0 to 1

invnbinomial (n, k, q)

Description: the value of the negative binomial parameter, p, such that q = nbinomial(n, k, p)

invnbinomial() is evaluated using invibeta().

Domain n: 1e-10 to 1e+17 (can be nonintegral)

Domain k: 0 to $2^{53} - 1$

Domain q: 0 to 1 (exclusive)

Range: 0 to 1

invnbinomialtail(n, k, q)

Description: the value of the negative binomial parameter, p, such that

q = nbinomialtail(n, k, p)

invnbinomialtail() is evaluated using invibetatail().

Domain n: 1e–10 to 1e+17 (can be nonintegral)

Domain k: 1 to $2^{53} - 1$ Domain q: 0 to 1 (exclusive)

Range: 0 to 1 (exclusive)

Normal (Gaussian), binormal, and multivariate normal distributions

normalden(z)

Description: the standard normal density, N(0,1)

Domain: -8e+307 to 8e+307 Range: 0 to 0.39894 ...

$normalden(x, \sigma)$

Description: the normal density with mean 0 and standard deviation σ

normalden(x,1) = normalden(x) and $normalden(x, \sigma) = normalden(x/\sigma)/\sigma$.

Domain x: -8e+307 to 8e+307Domain σ : 1e–308 to 8e+307 Range: 0 to 8e+307

$normalden(x, \mu, \sigma)$

Description: the normal density with mean μ and standard deviation σ , $N(\mu, \sigma^2)$

normalden(x,0,s) = normalden(x,s) and normalden (x, μ, σ) = normalden $((x - \mu)/\sigma)/\sigma$. In general,

$$\texttt{normalden}(z,\!\mu,\!\sigma) = \frac{1}{\sigma\sqrt{2\pi}}e^{-\frac{1}{2}\left\{\frac{(z-\mu)}{\sigma}\right\}^2}$$

Domain x: -8e+307 to 8e+307Domain μ : -8e+307 to 8e+307 Domain σ : 1e–308 to 8e+307 Range: 0 to 8e+307

normal(z)

Description: the cumulative standard normal distribution

normal(z) = $\int_{-\infty}^{z} \frac{1}{\sqrt{2\pi}} e^{-x^2/2} dx$ -8e+307 to 8e+307

Domain:

Range: 0 to 1

invnormal(p)

Description: the inverse cumulative standard normal distribution: if normal(z) = p, then

invnormal(p) = z

1e-323 to $1-2^{-53}$ Domain:

-38.449394 to 8.2095362 Range:

lnnormalden(z)

Description: the natural logarithm of the standard normal density, N(0,1)

Domain: -1e+154 to 1e+154

-5e+307 to -0.91893853 = lnnormalden(0)Range:

lnnormalden (x,σ)

Description: the natural logarithm of the normal density with mean 0 and standard deviation σ

lnnormalden(x, 1) = lnnormalden(x) and

 $lnnormalden(x,\sigma) = lnnormalden(x/\sigma) - ln(\sigma).$

Domain x: -8e+307 to 8e+307Domain σ : 1e–323 to 8e+307 -5e+307 to 742.82799Range:

lnnormalden(x, μ, σ)

Description: the natural logarithm of the normal density with mean μ and standard deviation σ , $N(\mu, \sigma^2)$

Innormalden(x,0,s) = Innormalden(x,s) and Innormalden(x, μ , σ) = Innormalden($(x - \mu)/\sigma$) - $\ln(\sigma)$. In general,

$${\tt lnnormalden}(z,\mu,\sigma) = \ln\left[\frac{1}{\sigma\sqrt{2\pi}}e^{-\frac{1}{2}\left\{\frac{(z-\mu)}{\sigma}\right\}^2}\right]$$

Domain x: -8e+307 to 8e+307Domain μ : -8e+307 to 8e+307Domain σ : 1e-323 to 8e+307Range: 1e-323 to 8e+307

lnnormal(z)

Description: the natural logarithm of the cumulative standard normal distribution

$$\operatorname{lnnormal}(z) = \ln \left(\int_{-\infty}^{z} \frac{1}{\sqrt{2\pi}} e^{-x^2/2} dx \right)$$

Domain: -1e+99 to 8e+307Range: -5e+197 to 0

$binormal(h, k, \rho)$

Description: the joint cumulative distribution $\Phi(h,k,\rho)$ of bivariate normal with correlation ρ

Cumulative over $(-\infty, h] \times (-\infty, k]$:

$$\Phi(h,k,\rho) = \frac{1}{2\pi\sqrt{1-\rho^2}} \int_{-\infty}^{h} \int_{-\infty}^{k} \exp\left\{-\frac{1}{2(1-\rho^2)} \left(x_1^2 - 2\rho x_1 x_2 + x_2^2\right)\right\} dx_1 dx_2$$

Domain h: -8e+307 to 8e+307Domain k: -8e+307 to 8e+307

Domain ρ : -1 to 1 Range: 0 to 1

lnmvnormalden(M, V, X)

Description: the natural logarithm of the multivariate normal density

M is the mean vector, V is the covariance matrix, and X is the random vector.

Domain M: $1 \times n$ and $n \times 1$ vectors

Domain $V: n \times n$, positive-definite, symmetric matrices

Domain X: $1 \times n$ and $n \times 1$ vectors Range: -8e+307 to 8e+307

Poisson distribution

```
poissonp(m,k)
```

Description: the probability of observing floor (k) outcomes that are distributed as Poisson with

mean m

The Poisson probability function is evaluated using gammaden().

Domain m: 1e-10 to 1e+8 Domain k: 0 to 1e+9 Range: 0 to 1

poisson(m,k)

Description: the probability of observing floor(k) or fewer outcomes that are distributed as

Poisson with mean m

The Poisson distribution function is evaluated using gammaptail().

Domain m: 1e-10 to $2^{53} - 1$ Domain k: 0 to $2^{53} - 1$ Range: 0 to 1

poissontail(m,k)

Description: the probability of observing floor(k) or more outcomes that are distributed as

Poisson with mean m

The reverse cumulative Poisson distribution function is evaluated using gammap().

Domain m: 1e-10 to $2^{53} - 1$ Domain k: 0 to $2^{53} - 1$ Range: 0 to 1

invpoisson(k,p)

Description: the Poisson mean such that the cumulative Poisson distribution evaluated at k is p:

if poisson(m,k) = p, then invpoisson(k,p) = m

The inverse Poisson distribution function is evaluated using invgammaptail().

Domain k: 0 to $2^{53} - 1$ Domain p: 0 to 1 (exclusive) Range: 1.110e–16 to 2^{53}

invpoissontail(k,q)

Description: the Poisson mean such that the reverse cumulative Poisson distribution evaluated at

k is q: if poissontail(m,k) = q, then invpoissontail(k,q) = m

The inverse of the reverse cumulative Poisson distribution function is evaluated using invgammap().

Domain k: 0 to $2^{53} - 1$ Domain q: 0 to 1 (exclusive) Range: 0 to 2^{53} (left exclusive)

Student's t and noncentral Student's t distributions

tden(df,t)

Description: the probability density function of Student's t distribution

$$\mathtt{tden}(\mathit{df}\,,t) = \frac{\Gamma\{(\mathit{df}+1)/2\}}{\sqrt{\pi \mathit{df}}\Gamma(\mathit{df}/2)} \cdot \left(1 + t^2/\mathit{df}\right)^{-(\mathit{df}+1)/2}$$

Domain df: 1e–323 to 8e+307 (may be nonintegral)

Domain t: -8e+307 to 8e+307 Range: 0 to 0.39894 ...

t(df,t)

Description: the cumulative Student's t distribution with df degrees of freedom

Domain df: 2e–10 to 2e+17 (may be nonintegral)

Domain t; -8e+307 to 8e+307

Range: 0 to 1

ttail(df,t)

Description: the reverse cumulative (upper tail or survivor) Student's t distribution; the probability T > t

$$\mathtt{ttail}(df,t) = \int_{t}^{\infty} \frac{\Gamma\{(df+1)/2\}}{\sqrt{\pi df} \Gamma(df/2)} \cdot (1 + x^2/df)^{-(df+1)/2} \ dx$$

Domain df: 2e–10 to 2e+17 (may be nonintegral)

Domain t: -8e+307 to 8e+307

Range: 0 to 1

invt(df,p)

Description: the inverse cumulative Student's t distribution: if t(df,t) = p, then invt(df,p) = t

Domain df: 2e–10 to 2e+17 (may be nonintegral)

Domain p: 0 to 1

Range: -8e+307 to 8e+307

invttail(df,p)

Description: the inverse reverse cumulative (upper tail or survivor) Student's t distribution: if

ttail(df,t) = p, then invttail(df,p) = t

Domain df: 2e–10 to 2e+17 (may be nonintegral)

Domain p: 0 to 1

Range: -8e+307 to 8e+307

invnt(df, np, p)

Description: the inverse cumulative noncentral Student's t distribution: if nt(df, np, t) = p, then

invnt(df, np, p) = t

Domain df: 1 to 1e+6 (may be nonintegral)

Domain np: -1,000 to 1,000

Domain p: 0 to 1

Range: -8e+307 to 8e+307

invnttail(df, np, p)

Description: the inverse reverse cumulative (upper tail or survivor) noncentral Student's

t distribution: if nttail(df, np, t) = p, then invnttail(df, np, p) = t

Domain df: 1 to 1e+6 (may be nonintegral)

Domain np: -1,000 to 1,000

Domain p: 0 to 1

Range: -8e+10 to 8e+10

ntden(df, np, t)

Description: the probability density function of the noncentral Student's

t distribution with df degrees of freedom and noncentrality parameter np

Domain df: 1e–100 to 1e+10 (may be nonintegral)

Domain np: -1,000 to 1,000Domain t: -8e+307 to 8e+307Range: 0 to 0.39894 ...

nt(df, np, t)

Description: the cumulative noncentral Student's t distribution with $d\!f$ degrees of freedom and

noncentrality parameter np

$$nt(df,0,t) = t(df,t).$$

Domain df: 1e–100 to 1e+10 (may be nonintegral)

Domain np: -1,000 to 1,000Domain t: -8e+307 to 8e+307

Range: 0 to 1

nttail(df, np, t)

Description: the reverse cumulative (upper tail or survivor) noncentral Student's t distribution with

df degrees of freedom and noncentrality parameter np

Domain df: 1e-100 to 1e+10 (may be nonintegral)

Domain np: -1,000 to 1,000Domain t: -8e+307 to 8e+307

Range: 0 to 1

$\mathtt{npnt}(df,t,p)$

Description: the noncentrality parameter, np, for the noncentral Student's

t distribution: if nt(df, np, t) = p, then npnt(df, t, p) = np

Domain df: 1e–100 to 1e+8 (may be nonintegral)

Domain t: -8e+307 to 8e+307

Domain p: 0 to 1

Range: -1,000 to 1,000

Tukey's Studentized range distribution

tukeyprob(k, df, x)

Description: the cumulative Tukey's Studentized range distribution with k ranges and df degrees

of freedom; 0 if x < 0

If df is a missing value, then the normal distribution is used instead of Student's t.

tukeyprob() is computed using an algorithm described in Miller (1981).

Domain k: 2 to 1e+6 Domain df: 2 to 1e+6

Domain x: -8e+307 to 8e+307

Range: 0 to 1

invtukeyprob(k, df, p)

Description: the inverse cumulative Tukey's Studentized range distribution with k ranges and df

degrees of freedom

If df is a missing value, then the normal distribution is used instead of Student's t.

If tukeyprob(k, df, x) = p, then invtukeyprob(k, df, p) = x.

invtukeyprob() is computed using an algorithm described in Miller (1981).

Domain k: 2 to 1e+6 Domain df: 2 to 1e+6 Domain p: 0 to 1 Range: 0 to 8e+307

Weibull distribution

weibullden(a,b,x)

Description: the probability density function of the Weibull distribution with shape a and scale b

weibullden(a,b,x) = weibullden(a,b,0,x), where a is the shape, b is the

scale, and x is the value of Weibull random variable.

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307 Domain *x*: 1e–323 to 8e+307 Range: 0 to 8e+307

weibullden(a,b,g,x)

Description: the probability density function of the Weibull distribution with shape a, scale b, and location a

The probability density function of the generalized Weibull distribution is defined as

$$\frac{a}{b} \left(\frac{x-g}{b} \right)^{a-1} \exp \left\{ -\left(\frac{x-g}{b} \right)^a \right\}$$

for $x \ge g$ and 0 for x < g, where a is the shape, b is the scale, g is the location parameter, and x is the value of a generalized Weibull random variable.

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307 Domain *g*: –8e+307 to 8e+307

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge g$

Range: 0 to 8e+307

weibull(a,b,x)

Description: the cumulative Weibull distribution with shape a and scale b

weibull(a, b, x) = weibull(a, b, 0, x), where a is the shape, b is the scale, and x is the value of Weibull random variable.

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307 Domain *x*: 1e–323 to 8e+307

Range: 0 to 1

weibull(a,b,g,x)

Description: the cumulative Weibull distribution with shape a, scale b, and location g

The cumulative Weibull distribution is defined as

$$1 - \exp\left[-\left(\frac{x-g}{b}\right)^a\right]$$

for $x \ge g$ and 0 for x < g, where a is the shape, b is the scale, g is the location parameter, and x is the value of a Weibull random variable.

The mean of the Weibull distribution is $g + b\Gamma\{(a+1)/a\}$ and its variance is $b^2\left(\Gamma\{(a+2)/a\} - [\Gamma\{(a+1)/a\}]^2\right)$ where $\Gamma()$ is the gamma function described in lngamma().

Domain a: 1e–323 to 8e+307 Domain b: 1e–323 to 8e+307 Domain g: -8e+307 to 8e+307

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge g$

Range: 0 to 1

weibulltail(a,b,x)

Description: the reverse cumulative Weibull distribution with shape a and scale b

weibulltail(a,b,x) = weibulltail(a,b,0,x), where a is the shape, b is the scale, and x is the value of a Weibull random variable.

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307 Domain *x*: 1e–323 to 8e+307

Range: 0 to 1

weibulltail(a,b,g,x)

Description: the reverse cumulative Weibull distribution with shape a, scale b, and location g

The reverse cumulative Weibull distribution is defined as

$$\exp\left\{-\left(\frac{x-g}{b}\right)^a\right\}$$

for $x \ge g$ and 0 if x < g, where a is the shape, b is the scale, g is the location parameter, and x is the value of a generalized Weibull random variable.

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307 Domain *q*: –8e+307 to 8e+307

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge g$

Range: 0 to 1

invweibull(a,b,p)

Description: the inverse cumulative Weibull distribution with shape a and scale b: if

weibull(a,b,x) = p, then invweibull(a,b,p) = x

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307

Domain p: 0 to 1

Range: 1e-323 to 8e+307

invweibull(a,b,g,p)

Description: the inverse cumulative Weibull distribution with shape a, scale b, and location g: if

weibull(a,b,g,x) = p, then invweibull(a,b,g,p) = x

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307 Domain *g*: –8e+307 to 8e+307

Domain p: 0 to 1

Range: q + c(epsdouble) to 8e+307

invweibulltail(a,b,p)

Description: the inverse reverse cumulative Weibull distribution with shape a and scale b: if

weibulltail(a,b,x) = p, then invweibulltail(a,b,p) = x

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307

Domain p: 0 to 1

Range: 1e-323 to 8e+307

invweibulltail(a,b,g,p)

Description: the inverse reverse cumulative Weibull distribution with shape a, scale b, and location

g: if weibulltail(a,b,g,x) = p, then

invweibulltail(a,b,g,p) = x

Domain a: 1e–323 to 8e+307 Domain b: 1e–323 to 8e+307 Domain g: -8e+307 to 8e+307

Domain p: 0 to 1

Range: q + c(epsdouble) to 8e+307

Weibull (proportional hazards) distribution

weibullphden(a,b,x)

Description: the probability density function of the Weibull (proportional hazards) distribution

with shape a and scale b

weibullphden(a,b,x) = weibullphden(a,b,0,x), where a is the shape, b is the scale, and x is the value of Weibull (proportional hazards) random variable.

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307 Domain *x*: 1e–323 to 8e+307 Range: 0 to 8e+307

weibullphden(a,b,g,x)

Description: the probability density function of the Weibull (proportional hazards) distribution with shape a, scale b, and location g

The probability density function of the Weibull (proportional hazards) distribution is defined as

$$ba(x-g)^{a-1}\exp\left\{-b(x-g)^a\right\}$$

for $x \ge g$ and 0 for x < g, where a is the shape, b is the scale, g is the location parameter, and x is the value of a Weibull (proportional hazards) random variable.

Domain a: 1e–323 to 8e+307 Domain b: 1e–323 to 8e+307 Domain g: -8e+307 to 8e+307

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge g$

Range: 0 to 8e+307

weibullph(a,b,x)

Description: the cumulative Weibull (proportional hazards) distribution with shape a and scale b

weibullph(a,b,x) = weibullph(a,b,0,x), where a is the shape, b is the scale, and x is the value of Weibull random variable.

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307 Domain *x*: 1e–323 to 8e+307

Range: 0 to 1

weibullph(a,b,g,x)

Description: the cumulative Weibull (proportional hazards) distribution with shape a, scale b, and location q

The cumulative Weibull (proportional hazards) distribution is defined as

$$1 - \exp\left\{-b(x-g)^a\right\}$$

for $x \ge g$ and 0 if x < g, where a is the shape, b is the scale, g is the location parameter, and x is the value of a Weibull (proportional hazards) random variable. The mean of the Weibull (proportional hazards) distribution is

$$g + b^{-\frac{1}{a}} \Gamma\{(a+1)/a)\}$$

and its variance is

$$b^{-\frac{2}{a}} \left(\Gamma\{(a+2)/a\} - [\Gamma\{(a+1)/a\}]^2 \right)$$

where $\Gamma()$ is the gamma function described in $\operatorname{Ingamma}(x)$.

Domain a: 1e–323 to 8e+307 Domain b: 1e–323 to 8e+307 Domain g: -8e+307 to 8e+307

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge g$

Range: 0 to 1

weibullphtail(a,b,x)

Description: the reverse cumulative Weibull (proportional hazards) distribution with shape a and scale b

weibullphtail(a,b,x) = weibullphtail(a,b,0,x), where a is the shape, b is the scale, and x is the value of a Weibull (proportional hazards) random variable.

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307 Domain *x*: 1e–323 to 8e+307

Range: 0 to 1

weibullphtail(a,b,g,x)

Description: the reverse cumulative Weibull (proportional hazards) distribution with shape a, scale

b, and location g

The reverse cumulative Weibull (proportional hazards) distribution is defined as

$$\exp\left\{-b(x-g)^a\right\}$$

for $x \ge g$ and 0 of x < g, where a is the shape, b is the scale, g is the location parameter, and x is the value of a Weibull (proportional hazards) random variable.

Domain a: 1e–323 to 8e+307 Domain b: 1e–323 to 8e+307 Domain g: -8e+307 to 8e+307

Domain x: -8e+307 to 8e+307; interesting domain is $x \ge g$

Range: 0 to 1

invweibullph(a,b,p)

Description: the inverse cumulative Weibull (proportional hazards) distribution with shape a and

scale b: if weibullph(a,b,x) = p, then invweibullph(a,b,p) = x

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307

Domain p: 0 to 1

Range: 1e-323 to 8e+307

invweibullph(a,b,g,p)

Description: the inverse cumulative Weibull (proportional hazards) distribution with shape a, scale b,

and location g: if weibullph(a, b, g, x) = p, then invweibullph(a, b, g, p) = x

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307 Domain *g*: –8e+307 to 8e+307

Domain p: 0 to 1

Range: q + c(epsdouble) to 8e+307

invweibullphtail(a,b,p)

Description: the inverse reverse cumulative Weibull (proportional hazards) distribution with shape a

and scale b: if weibullphtail(a,b,x) = p, then invweibullphtail(a,b,p) = x

Domain *a*: 1e–323 to 8e+307 Domain *b*: 1e–323 to 8e+307

Domain p: 0 to 1

Range: 1e-323 to 8e+307

invweibullphtail(a,b,g,p)

Description: the inverse reverse cumulative Weibull (proportional hazards) distribution with shape

a, scale b, and location g: if weibullphtail(a, b, q, x) = p, then

invweibullphtail(a,b,q,p) = x

Domain a: 1e–323 to 8e+307 Domain b: 1e–323 to 8e+307 Domain g: -8e+307 to 8e+307

Domain p: 0 to 1

Range: q + c(epsdouble) to 8e+307

Wishart distribution

lnwishartden(df, V, X)

Description: the natural logarithm of the density of the Wishart distribution; missing if $df \leq n-1$

 $d\!f$ denotes the degrees of freedom, V is the scale matrix, and X is the Wishart random matrix.

Domain df: 1 to 1e+100 (may be nonintegral)

Domain V: $n \times n$, positive-definite, symmetric matrices Domain X: $n \times n$, positive-definite, symmetric matrices

Range: -8e+307 to 8e+307

lniwishartden(df, V, X)

Description: the natural logarithm of the density of the inverse Wishart distribution; missing if

 $df \leq n-1$

 df denotes the degrees of freedom, V is the scale matrix, and X is the inverse

Wishart random matrix.

Domain df: 1 to 1e+100 (may be nonintegral)

Domain V: $n \times n$, positive-definite, symmetric matrices Domain X: $n \times n$, positive-definite, symmetric matrices

Range: -8e+307 to 8e+307

John Wishart (1898–1956) was born in Montrose, Scotland. He obtained a degree in mathematics and physics from the University of Edinburgh. He learned mathematics from E. T. Whittaker, upon whose recommendation he became Karl Pearson's research assistant. During his apprenticeship, he worked on approximations to the incomplete beta function and published multiple papers on this topic. He is best known for deriving the generalized product moment distribution, which was consequently named the Wishart distribution. This distribution is a critical component in the calculation of covariance matrices and Bayesian statistics.

Wishart served in both world wars, fighting with the Black Watch regiment in the first and working for the Intelligence Corps in the second. Upon his return from World War II, he resumed his involvement with the Royal Statistical Society, becoming chairman of the Research Section in 1945. A few years later, he also served as Associate Editor for the journal *Biometrika*.

He taught courses in statistics and agriculture at Cambridge and became the Head of the Statistical Laboratory. He published multiple papers applying statistical methods to agricultural research and was involved with the United Nations Food and Agriculture Organization. He was in Mexico to establish an agricultural research center on behalf of this organization when he died.

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Also see

- [FN] Functions by category
- [D] **egen** Extensions to generate
- [D] generate Create or change contents of variable
- [M-4] **Statistical** Statistical functions
- [U] 13.3 Functions

String functions

Contents Functions References Also see

Contents

```
abbrev(s,n)
                                 name s, abbreviated to a length of n
char(n)
                                 the character corresponding to ASCII or extended ASCII code n; ""
                                    if n is not in the domain
collatorlocale(loc, type)
                                 the most closely related locale supported by ICU from loc if type
                                    is 1; the actual locale where the collation data comes from if
                                    type is 2
collatorversion(loc)
                                 the version string of a collator based on locale loc
                                 the position in ASCII string s_1 of the first character of s_1 not found
indexnot(s_1, s_2)
                                    in ASCII string s_2, or 0 if all characters of s_1 are found in s_2
plural(n,s)
                                 the plural of s if n \neq \pm 1
plural(n,s_1,s_2)
                                 the plural of s_1, as modified by or replaced with s_2, if n \neq \pm 1
real(s)
                                 s converted to numeric or missing
regexcapture(n)
                                 subexpression n from a previous regexm() or regexmatch()
                                    match
regexcapturenamed(grp)
                                 subexpression corresponding to matching group named grp in reg-
                                    ular expression from a previous regexm() or regexmatch()
                                    match
regexm(s, re)
                                 a match of a regular expression, which evaluates to 1 if regular
                                    expression re is satisfied by the ASCII string s; otherwise, 0
regexmatch(s,re[,noc[,std[,nlalt]]])
                                 a match of a regular expression, which evaluates to 1 if regular
                                    expression re is satisfied by the ASCII string s; otherwise, 0
                                 replaces the first substring within ASCII string s_1 that matches re
regexr(s_1, re, s_2)
                                    with ASCII string s_2 and returns the resulting string
regexreplace (s_1, re, s_2 |, noc |, fmt |, std |, nlalt | | | |)
                                 replaces the first substring within ASCII string s_1 that matches re
                                    with ASCII string s_2 and returns the resulting string
regexreplaceall(s_1, re, s_2 |, noc |, fmt |, std |, nlalt | | | |)
                                 replaces all substrings within ASCII string s_1 that match re with
                                    ASCII string s_2 and returns the resulting string
regexs(n)
                                 subexpression n from a previous regexm() or regexmatch()
                                    match, where 0 \le n < 10
soundex(s)
                                 the soundex code for a string, s
soundex_nara(s)
                                 the U.S. Census soundex code for a string, s
strcat(s_1, s_2)
                                 there is no strcat() function; instead the addition operator is used
                                    to concatenate strings
strdup(s_1, n)
                                 there is no strdup() function; instead the multiplication operator
                                    is used to create multiple copies of strings
string(n)
                                 a synonym for strofreal(n)
```

```
string(n,s)
                                 a synonym for strofreal(n,s)
stritrim(s)
                                 s with multiple, consecutive internal blanks (ASCII space character
                                    char(32)) collapsed to one blank
strlen(s)
                                 the number of characters in ASCII s or length in bytes
strlower(s)
                                 lowercase ASCII characters in string s
strltrim(s)
                                 s without leading blanks (ASCII space character char (32))
strmatch(s_1, s_2)
                                 1 if s_1 matches the pattern s_2; otherwise, 0
strofreal(n)
                                 n converted to a string
strofreal(n,s)
                                 n converted to a string using the specified display format
                                 the position in s_1 at which s_2 is first found, 0 if s_2 does not occur,
strpos(s_1, s_2)
                                    and 1 if s_2 is empty
strproper(s)
                                 a string with the first ASCII letter and any other letters immediately
                                    following characters that are not letters capitalized; all other
                                    ASCII letters converted to lowercase
strreverse(s)
                                 the reverse of ASCII string s
strrpos(s_1, s_2)
                                 the position in s_1 at which s_2 is last found, 0 if s_2 does not occur,
                                    and 1 if s_2 is empty
strrtrim(s)
                                 s without trailing blanks (ASCII space character char (32))
strtoname(s[,p])
                                 s translated into a Stata 13 compatible name
strtrim(s)
                                 s without leading and trailing blanks (ASCII space character
                                    char(32)); equivalent to strltrim(strrtrim(s))
strupper(s)
                                 uppercase ASCII characters in string s
subinstr(s_1, s_2, s_3, n)
                                 s_1, where the first n occurrences in s_1 of s_2 have been replaced
subinword(s_1, s_2, s_3, n)
                                 s_1, where the first n occurrences in s_1 of s_2 as a word have been
                                    replaced with s_3
substr(s, n_1, n_2)
                                 the substring of s, starting at n_1, for a length of n_2
tobytes(s[,n])
                                 escaped decimal or hex digit strings of up to 200 bytes of s
uchar(n)
                                 the Unicode character corresponding to Unicode code point n or
                                    an empty string if n is beyond the Unicode code-point range
                                 the number of display columns needed to display the Unicode string
udstrlen(s)
                                    s in the Stata Results window
udsubstr(s, n_1, n_2)
                                 the Unicode substring of s, starting at character n_1, for n_2 display
                                    columns
uisdigit(s)
                                 1 if the first Unicode character in s is a Unicode decimal digit;
                                    otherwise, 0
uisletter(s)
                                 1 if the first Unicode character in s is a Unicode letter; otherwise.
ustrcompare (s_1, s_2 \lceil, loc \rceil)
                                 compares two Unicode strings
ustrcompareex(s_1, s_2, loc, st, case, cslv, norm, num, alt, fr)
                                 compares two Unicode strings
ustrfix(s[,rep])
                                 replaces each invalid UTF-8 sequence with a Unicode character
ustrfrom(s,enc,mode)
                                 converts the string s in encoding enc to a UTF-8 encoded Unicode
ustrinvalidcnt(s)
                                 the number of invalid UTF-8 sequences in s
ustrleft(s,n)
                                 the first n Unicode characters of the Unicode string s
```

```
ustrlen(s)
                                the number of characters in the Unicode string s
ustrlower(s[,loc])
                                lowercase all characters of Unicode string s under the given locale
ustrltrim(s)
                                removes the leading Unicode whitespace characters and blanks from
                                   the Unicode string s
ustrnormalize(s, norm)
                                normalizes Unicode string s to one of the five normalization forms
                                    specified by norm
ustrpos(s_1, s_2[, n])
                                the position in s_1 at which s_2 is first found; otherwise, 0
ustrregexm(s, re[, noc])
                                performs a match of a regular expression and evaluates to 1 if regular
                                   expression re is satisfied by the Unicode string s; otherwise, 0
ustrregexra(s_1, re, s_2[, noc]) replaces all substrings within the Unicode string s_1 that match re
                                    with s_2 and returns the resulting string
ustrregexrf (s_1, re, s_2 \mid , noc \mid) replaces the first substring within the Unicode string s_1 that matches
                                    re with s_2 and returns the resulting string
ustrregexs(n)
                                subexpression n from a previous ustrregexm() match
ustrreverse(s)
                                the reverse of Unicode string s
ustrright(s,n)
                                the last n Unicode characters of the Unicode string s
ustrrpos(s_1, s_2[, n])
                                the position in s_1 at which s_2 is last found; otherwise, 0
ustrrtrim(s)
                                remove trailing Unicode whitespace characters and blanks from the
                                    Unicode string s
ustrsortkey(s[,loc])
                                generates a null-terminated byte array that can be used by the sort
                                   command to produce the same order as ustrcompare()
ustrsortkeyex(s, loc, st, case, cslv, norm, num, alt, fr)
                                generates a null-terminated byte array that can be used by the sort
                                   command to produce the same order as ustrcompare()
ustrtitle(s[,loc])
                                a string with the first characters of Unicode words titlecased and
                                    other characters lowercased
                                converts the Unicode string s in UTF-8 encoding to a string in
ustrto(s,enc,mode)
                                   encoding enc
ustrtohex(s[,n])
                                escaped hex digit string of s up to 200 Unicode characters
ustrtoname(s|,p|)
                                string s translated into a Stata name
ustrtrim(s)
                                removes leading and trailing Unicode whitespace characters and
                                   blanks from the Unicode string s
ustrunescape(s)
                                the Unicode string corresponding to the escaped sequences of s
ustrupper(s[,loc])
                                uppercase all characters in string s under the given locale loc
ustrword(s, n[, loc])
                                the nth Unicode word in the Unicode string s
ustrwordcount(s[,loc])
                                the number of nonempty Unicode words in the Unicode string s
usubinstr(s_1, s_2, s_3, n)
                                replaces the first n occurrences of the Unicode string s_2 with the
                                    Unicode string s_3 in s_1
usubstr(s, n_1, n_2)
                                the Unicode substring of s, starting at n_1, for a length of n_2
word(s,n)
                                the nth word in s; missing ("") if n is missing
```

wordbreaklocale (loc, type)

the most closely related locale supported by ICU from loc if type is 1, the actual locale where the word-boundary analysis data come from if type is 2; or an empty string is returned for any

other type

wordcount(s)

the number of words in s

Functions

In the display below, s indicates a string subexpression (a string literal, a string variable, or another string expression) and n indicates a numeric subexpression (a number, a numeric variable, or another numeric expression).

If your strings contain Unicode characters or you are writing programs that will be used by others who might use Unicode strings, read [U] 12.4.2 Handling Unicode strings.

abbrev(s,n)

Description:

name s, abbreviated to a length of n

Length is measured in the number of display columns, not in the number of characters. For most users, the number of display columns equals the number of characters. For a detailed discussion of display columns, see [U] 12.4.2.2 Displaying Unicode characters.

If any of the characters of s are a period, ".", and n < 8, then the value of ndefaults to a value of 8. Otherwise, if n < 5, then n defaults to a value of 5. If n is missing, abbrev() will return the entire string s. abbrev() is typically used with variable names and variable names with factor-variable or time-series operators (the period case).

abbrev("displacement",8) is displa~t.

Domain s:

strings

Domain n:

integers 5 to 32

strings Range:

char(n)

Description:

the character corresponding to ASCII or extended ASCII code n; "" if n is not in the domain

Note: ASCII codes are from 0 to 127; extended ASCII codes are from 128 to 255. Prior to Stata 14, the display of extended ASCII characters was encoding dependent. For example, char (128) on Microsoft Windows using Windows-1252 encoding displayed the Euro symbol, but on Linux using ISO-Latin-1 encoding, char (128) displayed an invalid character symbol. Beginning with Stata 14, Stata's display encoding is UTF-8 on all platforms. The char(128) function is an invalid UTF-8 sequence and thus will display a question mark. There are two Unicode functions corresponding to char(): uchar() and ustrunescape(). You can use uchar(8364) or ustrunescape("\u20AC") to display a Euro sign on all

platforms. Domain n: integers 0 to 255

Range:

ASCII characters

uchar(n)

Description: the Unicode character corresponding to Unicode code point n or an empty string

if n is beyond the Unicode code-point range

Note that uchar() takes the decimal value of the Unicode code point. ustrunescape() takes an escaped hex digit string of the Unicode code point. For example, both uchar(8364) and ustrunescape("\u20ac") produce the Euro

sign.

Domain n: integers ≥ 0

Range: Unicode characters

collatorlocale(loc, type)

Description: the most closely related locale supported by ICU from loc if type is 1; the actual

locale where the collation data comes from if type is 2

For any other type, loc is returned in a canonicalized form.

collatorlocale("en_us_texas", 0) = en_US_TEXAS

collatorlocale("en_us_texas", 1) = en_US
collatorlocale("en_us_texas", 2) = root

Domain *loc*: strings of locale name

Domain *type*: integers Range: strings

collatorversion(loc)

Description: the version string of a collator based on locale *loc*

The Unicode standard is constantly adding more characters and the sort key format may change as well. This can cause ustrsortkey() and ustrsortkeyex() to produce incompatible sort keys between different versions of International Components for Unicode. The version string can be used for versioning the sort

keys to indicate when saved sort keys must be regenerated.

Range: strings

 $indexnot(s_1, s_2)$

Description: the position in ASCII string s_1 of the first character of s_1 not found in ASCII string

 s_2 , or 0 if all characters of s_1 are found in s_2

indexnot() is intended for use only with plain ASCII strings. For Unicode characters beyond the plain ASCII range, the position and character are given in

bytes, not characters.

Domain s_1 : ASCII strings (to be searched) Domain s_2 : ASCII strings (to search for)

Range: integers ≥ 0

plural(n,s)

Description: the plural of s if $n \neq \pm 1$

The plural is formed by adding "s" to s.

plural(1, "horse") = "horse"
plural(2, "horse") = "horses"

Domain n: real numbers
Domain s: strings
Range: strings

$plural(n,s_1,s_2)$

Description: the plural of s_1 , as modified by or replaced with s_2 , if $n \neq \pm 1$

If s_2 begins with the character "+", the plural is formed by adding the remainder of s_2 to s_1 . If s_2 begins with the character "-", the plural is formed by subtracting the remainder of s_2 from s_1 . If s_2 begins with neither "+" nor "-", then the plural is formed by returning s_2 .

plural(2, "glass", "+es") = "glasses"
plural(1, "mouse", "mice") = "mouse"
plural(2, "mouse", "mice") = "mice"
plural(2, "abcdefg", "-efg") = "abcd"

Domain n:real numbersDomain s_1 :stringsDomain s_2 :stringsRange:strings

real(s)

Description: s converted to numeric or missing

Also see strofreal(). real("5.2")+1 = 6.2 real("hello") = .

Domain s: strings

Range: -8e+307 to 8e+307 or missing

regexcapture(n)

Description: subexpression n from a previous regexm() or regexmatch() match

regexcapture(0) returns the entire string that satisfied the regular expression.

Domain n: integers

Range: ASCII strings or missing

regexcapturenamed(grp)

Description: subexpression corresponding to matching group named grp in regular expression

from a previous regexm() or regexmatch() match

Domain grp: ASCII strings

Range: ASCII strings or missing

regexm(s, re)

Description: a match of a regular expression, which evaluates to 1 if regular expression re is

satisfied by the ASCII string s; otherwise, 0

Regular expression syntax is based on Henry Spencer's NFA algorithm, and this is nearly identical to the POSIX.2 standard. s and re may not contain binary 0 (\setminus 0).

regexm() is intended for use only with plain ASCII characters. For Unicode characters beyond the plain ASCII range, the match is based on bytes. For a character-based match, see ustrregexm().

For more advanced regular expression matching, see regexmatch().

Domain s: ASCII strings

Domain re: regular expressions Range: 0, 1, or *missing*

regexmatch(s, re[, noc[, std[, nlalt]]])

Description: a match of a regular expression, which evaluates to 1 if regular expression re is satisfied by the ASCII string s; otherwise, 0

regermatch() is intended for use only with plain ASCII characters. For Unicode characters beyond the plain ASCII range, the match is based on bytes. For a character-based match, see ustrregerm().

If *noc* is specified and is not 0, a case-insensitive match is performed; otherwise, a case-sensitive match is performed.

std specifies the regular expression standard: 1 for POSIX Extended Regular, 2 for POSIX Basic Regular, 3 for Emacs, 4 for AWK, 5 for grep, 6 for egrep, or any other number for Perl, the default.

If nlalt is specified and is 0, the newline character, char(10), is not treated like alternation operator |; otherwise, newline has the same effect as |.

s and re may not contain binary $0 (\0)$.

Domain s: ASCII strings Domain re: regular expression

Domain *noc*: integers Domain *std*: integers Domain *nlalt*: integers

Range: 0, 1, or missing

 $regexr(s_1, re, s_2)$

Description:

replaces the first substring within ASCII string s_1 that matches re with ASCII string s_2 and returns the resulting string

If s_1 contains no substring that matches re, the unaltered s_1 is returned. s_1 and the result of regexr() may be at most 1,100,000 characters long. s_1 , re, and s_2 may not contain binary 0 (\0).

regexr() is intended for use only with plain ASCII characters. For Unicode characters beyond the plain ASCII range, the match is based on bytes, and the result is restricted to 1,100,000 bytes. For a character-based match, see ustrregexrf() or ustrregexra().

For more advanced regular expression replacement, see regexreplace() and regexreplaceall().

Domain s_1 : ASCII strings

Domain re: regular expressions Domain s_2 : ASCII strings Range: ASCII strings

regexreplace(s_1 , re, s_2 [, noc[, fmt[, std[, nlalt]]])

Description: replaces the first substring within ASCII string s_1 that matches re with ASCII string s_2 and returns the resulting string

If *noc* is specified and is not 0, a case-insensitive match is performed; otherwise, a case-sensitive match is performed.

fmt specifies the format string syntax supported in s_2 : 1 for literal, where s_2 is treated as a string literal (no special character substitution), 2 for sed, or any other number for Perl, the default.

std specifies the regular expression standard: 1 for POSIX Extended Regular, 2 for POSIX Basic Regular, 3 for Emacs, 4 for AWK, 5 for grep, 6 for egrep, or any other number for Perl, the default.

If nlalt is specified and is 0, the newline character, char(10), is not treated like alternation operator |; otherwise, newline has the same effect as |.

If s_1 contains no substring that matches re, the unaltered s_1 is returned. s_1 , s_2 , and re may not contain binary 0 (\0).

Domain *nlalt*: integers
Range: ASCII strings

regexreplaceall(s_1 , re, s_2 [, noc[, fmt[, std[, nlalt]]])

Description: replaces all substrings within ASCII string s_1 that match re with ASCII string s_2

and returns the resulting string

If noc is specified and is not 0, a case-insensitive match is performed; otherwise, a case-sensitive match is performed.

fmt specifies the format string syntax supported in s_2 : 1 for literal, where s_2 is treated as a string literal (no special character substitution), 2 for sed, or any other number for Perl, the default.

std specifies the regular expression standard: 1 for POSIX Extended Regular, 2 for POSIX Basic Regular, 3 for Emacs, 4 for AWK, 5 for grep, 6 for egrep, or any other number for Perl, the default.

If nlalt is specified and is 0, the newline character, char(10), is not treated like alternation operator |; otherwise, newline has the same effect as |.

If s_1 contains no substring that matches re, the unaltered s_1 is returned. s_1 , s_2 , and re may not contain binary 0 (\setminus 0).

Domain s_1 : ASCII strings Domain re: regular expression Domain s_2 : ASCII strings

Domain s_2 :ASCII stringsDomain noc:integersDomain fmt:integersDomain std:integersDomain nlalt:integersRange:ASCII strings

regexs(n)

Description: subexpression n from a previous regexm() or regexmatch() match, where

 $0 \le n < 10$

Subexpression 0 is reserved for the entire string that satisfied the regular expression. The returned subexpression may be at most 1,100,000 characters (bytes) long.

For more options to return matching substrings, see regexcapture() and regexcapturenamed().

Domain n: 0 to 9

Range: ASCII strings

ustrregexm(s, re[, noc])

Description: performs a match of a regular expression and evaluates to 1 if regular expression

re is satisfied by the Unicode string s; otherwise, 0

If *noc* is specified and not 0, a case-insensitive match is performed. The function may return a negative integer if an error occurs.

 $\begin{array}{l} {\rm ustrregexm("12345",\ "([0-9])\{5\}")=1} \\ {\rm ustrregexm("de\ TR\grave{E}S\ pr\grave{e}s",\ "r\grave{e}s")=1} \\ {\rm ustrregexm("de\ TR\grave{E}S\ pr\grave{e}s",\ "R\grave{e}s")=0} \\ {\rm ustrregexm("de\ TR\grave{E}S\ pr\grave{e}s",\ "R\grave{e}s",\ 1)=1} \\ \end{array}$

Domain s: Unicode strings

Domain re: Unicode regular expressions

Domain *noc*: integers Range: integers

ustrregexrf(s_1 , re, s_2 [, noc])

Description: replaces the first substring within the Unicode string s_1 that matches re with s_2

and returns the resulting string

If noc is specified and not 0, a case-insensitive match is performed. The function

may return an empty string if an error occurs.

ustrregexrf("très près", "rès", "X") = "tX près" ustrregexrf("TRÈS près", "Rès", "X") = "TRÈS près" ustrregexrf("TRÈS près", "Rès", "X", 1) = "TX près"

Domain s_1 : Unicode strings

Domain re: Unicode regular expressions

Domain s_2 : Unicode strings

Domain noc: integers

Range: Unicode strings

ustrregexra(s_1 , re, s_2 [, noc])

Description: replaces all substrings within the Unicode string s_1 that match re with s_2 and

returns the resulting string

If noc is specified and not 0, a case-insensitive match is performed. The function

may return an empty string if an error occurs.

ustrregexra("très près", "rès", "X") = "tX pX" ustrregexra("TRÈS près", "Rès", "X") = "TRÈS près" ustrregexra("TRÈS près", "Rès", "X", 1) = "TX pX"

Domain s_1 : Unicode strings

Domain re: Unicode regular expressions

Domain s_2 : Unicode strings

Domain noc: integers

Range: Unicode strings

ustrregexs(n)

Description: subexpression n from a previous ustrregexm() match

Subexpression 0 is reserved for the entire string that satisfied the regular expression. The function may return an empty string if n is larger than the maximum count

of subexpressions from the previous match or if an error occurs.

Domain n: integers ≥ 0

Range: strings

soundex(s)

Description: the soundex code for a string, s

The soundex code consists of a letter followed by three numbers: the letter is the first ASCII letter of the name and the numbers encode the remaining consonants. Similar sounding consonants are encoded by the same number. Unicode characters

beyond the plain ASCII range are ignored.

soundex("Ashcraft") = "A226"
soundex("Robert") = "R163"
soundex("Rupert") = "R163"

Domain s: strings Range: strings

soundex_nara(s)

Description: the U.S. Census soundex code for a string, s

The soundex code consists of a letter followed by three numbers: the letter is the first ASCII letter of the name and the numbers encode the remaining consonants. Similar sounding consonants are encoded by the same number. Unicode characters

beyond the plain ASCII range are ignored.

soundex_nara("Ashcraft") = "A261"

Domain s: strings Range: strings

 $strcat(s_1, s_2)$

Description: there is no strcat() function; instead the addition operator is used to concatenate

sumgs

"hello " + "world" = "hello world"

"a" + "b" = "ab"

"Café " + "de Flore" = "Café de Flore"

Domain s_1 : strings Domain s_2 : strings Range: strings

 $strdup(s_1,n)$

Description: there is no strdup() function; instead the multiplication operator is used to create

multiple copies of strings

"hello" * 3 = "hellohellohello"
3 * "hello" = "hellohellohello"

0 * "hello" = ""

"hello" * 1 = "hello"

"Здравствуйте" * 2 = "Здравствуйте Здравствуйте"

Domain s_1 : strings

Domain n: nonnegative integers $0, 1, 2, \ldots$

Range: strings

string(n)

Description: a synonym for strofreal(n)

string(n,s)

Description: a synonym for strofreal(n,s)

stritrim(s)

Description: s with multiple, consecutive internal blanks (ASCII space character char(32))

collapsed to one blank

stritrim("hello there") = "hello there"

Domain s: strings

Range: strings with no multiple, consecutive internal blanks

strlen(s)

Description: the number of characters in ASCII s or length in bytes

strlen() is intended for use only with plain ASCII characters and for use by programmers who want to obtain the byte-length of a string. Note that any Unicode character beyond ASCII range (code point greater than 127) takes more than 1 byte

in the UTF-8 encoding; for example, é takes 2 bytes.

For the number of characters in a Unicode string, see ustrlen().

strlen("ab") = 2strlen("é") = 2

Domain s: strings

Range: integers > 0

ustrlen(s)

Description: the number of characters in the Unicode string s

An invalid UTF-8 sequence is counted as one Unicode character. An invalid UTF-8 sequence may contain one byte or multiple bytes. Note that any Unicode character beyond the plain ASCII range (code point greater than 127) takes more than 1 byte

in the UTF-8 encoding; for example, é takes 2 bytes.

ustrlen("médiane") = 7 strlen("médiane") = 8

Domain s: Unicode strings Range: integers > 0

udstrlen(s)

Description: the number of display columns needed to display the Unicode string s in the Stata

Results window

A Unicode character in the CJK (Chinese, Japanese, and Korean) encoding usually requires two display columns; a Latin character usually requires one column. Any

invalid UTF-8 sequence requires one column.

udstrlen("中值") = 4 ustrlen("中值") = 2 strlen("中值") = 6

Domain s: Unicode strings Range: integers ≥ 0

strlower(s)

Description: lowercase ASCII characters in string s

Unicode characters beyond the plain ASCII range are ignored.

strlower("THIS") = "this"
strlower("CAFÉ") = "cafÉ"

Domain s: strings

Range: strings with lowercased characters

ustrlower(s[,loc])

Description: lowercase all characters of Unicode string s under the given locale loc

If loc is not specified, the default locale is used. The same s but different loc may produce different results; for example, the lowercase letter of "I" is "i" in English but a dotless "i" in Turkish. The same Unicode character can be mapped to different Unicode characters based on its surrounding characters; for example, Greek capital letter sigma Σ has two lowercases: ς , if it is the final character of a word, or σ . The result can be longer or shorter than the input Unicode string in bytes.

ustrlower("MÉDIANE","fr") = "médiane"
ustrlower("ISTANBUL","tr") = "istanbul"

ustrlower("ΟΔΥΣΣΕΥΣ") = "ὀδυσσεύς"

Domain s: Unicode strings
Domain loc: locale name
Range: Unicode strings

strltrim(s)

Description: s without leading blanks (ASCII space character char (32))

strltrim(" this") = "this"

Domain s: strings

Range: strings without leading blanks

ustrltrim(x)

Description: removes the leading Unicode whitespace characters and blanks from the Unicode

string s

Note that, in addition to char(32), ASCII characters char(9), char(10), char(11), char(12), and char(13) are whitespace characters in Unicode stan-

ustrltrim(" this") = "this"

ustrltrim(char(9)+"this") = "this"

ustrltrim(ustrunescape("\u1680")+" this") = "this"

Domain s: Unicode strings Range: Unicode strings

$strmatch(s_1, s_2)$

Description: 1 if s_1 matches the pattern s_2 ; otherwise, 0

strmatch("17.4", "1??4") returns 1. In s_2 , "?" means that one character goes here, and "*" means that zero or more bytes go here. Note that a Unicode character may contain multiple bytes; thus, using "*" with Unicode characters can infrequently result in matches that do not occur at a character boundary.

Also see regexm(), regexr(), and regexs().

strmatch("café", "caf?") = 1

Domain s_1 : strings Domain s_2 : strings

Range: integers 0 or 1

strofreal(n)

Description: n converted to a string

Also see real().

strofreal(4)+"F" = "4F"

strofreal(1234567) = "1234567"strofreal(12345678) = "1.23e+07"

strofreal(.) = "."

Domain n: -8e+307 to 8e+307 or missing

Range: strings

```
strofreal(n,s)
```

Description: n converted to a string using the specified display format

Also see real().

strofreal(4,"%9.2f") = "4.00" strofreal(123456789,"%11.0g") = "123456789"

strofreal(123456789, "%13.0gc") = "123,456,789"

strofreal(0,"%td") = "01jan1960" strofreal(225,"%tq") = "2016q2" strofreal(225,"not a format") = ""

Domain n: -8e+307 to 8e+307 or missing

Domain s: strings containing %fmt numeric display format

Range: strings

$strpos(s_1, s_2)$

Description: the position in s_1 at which s_2 is first found, 0 if s_2 does not occur, and 1 if s_2 is empty

strpos() is intended for use only with plain ASCII characters and for use by programmers who want to obtain the byte-position of s_2 . Note that any Unicode character beyond ASCII range (code point greater than 127) takes more than 1 byte in the UTF-8 encoding; for example, \acute{e} takes 2 bytes.

To find the character position of s_2 in a Unicode string, see ustrpos().

strpos("this","is") = 3
strpos("this","it") = 0
strpos("this","") = 1

Domain s_1 : strings (to be searched) Domain s_2 : strings (to search for)

Range: integers ≥ 0

$ustrpos(s_1, s_2[, n])$

Description: the position in s_1 at which s_2 is first found; otherwise, 0

If n is specified and is greater than 0, the search starts at the nth Unicode character of s_1 . An invalid UTF-8 sequence in either s_1 or s_2 is replaced with a Unicode replacement character \ufffd before the search is performed.

ustrpos("médiane", "édi") = 2 ustrpos("médiane", "édi", 3) = 0 ustrpos("médiane", "éci") = 0

Domain s_1 : Unicode strings (to be searched)
Domain s_2 : Unicode strings (to search for)

 $\begin{array}{ll} \text{Domain } n\text{:} & \text{integers} \\ \text{Range:} & \text{integers} \end{array}$

strproper(s)

Description:

a string with the first ASCII letter and any other letters immediately following characters that are not letters capitalized; all other ASCII letters converted to lowercase

strproper() implements a form of titlecasing and is intended for use only with plain ASCII strings. Unicode characters beyond ASCII are treated as characters that are not letters. To titlecase strings with Unicode characters beyond the plain ASCII range or to implement language-sensitive rules for titlecasing, see ustrtitle().

strproper("mR. joHn a. sMitH") = "Mr. John A. Smith"
strproper("jack o'reilly") = "Jack O'Reilly"
strproper("2-cent's worth") = "2-Cent'S Worth"
strproper("vous êtes") = "Vous êTes"

Domain s: strings Range: strings

ustrtitle(s[,loc])

Description:

a string with the first characters of Unicode words titlecased and other characters lowercased

If *loc* is not specified, the default locale is used. Note that a Unicode word is different from a Stata word produced by function word(). The Stata word is a space-separated token. A Unicode word is a language unit based on either a set of word-boundary rules or dictionaries for some languages (Chinese, Japanese, and Thai). The titlecase is also locale dependent and context sensitive; for example, lowercase "ij" is considered a digraph in Dutch. Its titlecase is "IJ".

ustrtitle("vous êtes", "fr") = "Vous Êtes"
ustrtitle("mR. joHn a. sMitH") = "Mr. John A. Smith"
ustrtitle("ijmuiden", "en") = "Ijmuiden"
ustrtitle("ijmuiden", "nl") = "IJmuiden"

Domain s: Unicode strings
Domain loc: Unicode strings
Range: Unicode strings

strreverse(s)

Description:

the reverse of ASCII string s

strreverse() is intended for use only with plain ASCII characters. For Unicode characters beyond ASCII range (code point greater than 127), the encoded bytes are reversed.

To reverse the characters of Unicode string, see ustrreverse().

strreverse("hello") = "olleh"

Domain s: ASCII strings

Range: ASCII reversed strings

ustrreverse(s)

Description: the reverse of Unicode string s

The function does not take Unicode character equivalence into consideration. Hence, a Unicode character in a decomposed form will not be reversed as one unit. An invalid UTF-8 sequence is replaced with a Unicode replacement character

\ufffd.

ustrreverse("médiane") = "enaidém"

Domain s: Unicode strings

Range: reversed Unicode strings

strrpos (s_1, s_2) Description:

the position in s_1 at which s_2 is last found, 0 if s_2 does not occur, and 1 if s_2 is

empty

strrpos() is intended for use only with plain ASCII characters and for use by programmers who want to obtain the last byte-position of s_2 . Note that any Unicode character beyond ASCII range (code point greater than 127) takes more than 1 byte in the UTF-8 encoding; for example, \acute{e} takes 2 bytes.

To find the last character position of s_2 in a Unicode string, see ustrrpos().

$$\begin{split} & \text{strrpos("this","is")} = 3 \\ & \text{strrpos("this is","is")} = 6 \\ & \text{strrpos("this is","it")} = 0 \\ & \text{strrpos("this is","")} = 1 \end{split}$$

Domain s_1 : strings (to be searched) Domain s_2 : strings (to search for)

Range: integers ≥ 0

 $ustrrpos(s_1, s_2[, n])$

Description: the position in s_1 at which s_2 is last found; otherwise, 0

If n is specified and is greater than 0, only the part between the first Unicode character and the nth Unicode character of s_1 is searched. An invalid UTF-8 sequence in either s_1 or s_2 is replaced with a Unicode replacement character

\ufffd before the search is performed.

ustrrpos("enchanté", "n") = 6
ustrrpos("enchanté", "n", 5) = 2
ustrrpos("enchanté", "n", 6) = 6
ustrrpos("enchanté", "ne") = 0

Domain s_1 : Unicode strings (to be searched) Domain s_2 : Unicode strings (to search for)

Domain n: integers Range: integers

strrtrim(s)

Description: s without trailing blanks (ASCII space character char (32))

strrtrim("this ") = "this"

Domain s: strings

Range: strings without trailing blanks

ustrrtrim(s)

Description: remove trailing Unicode whitespace characters and blanks from the Unicode string

S

Note that, in addition to char(32), ASCII characters char(9), char(10), char(11), char(12), and char(13) are considered whitespace characters in the Unicode standard.

ustrrtrim("this ") = "this"
ustrltrim("this"+char(10)) = "this"
ustrrtrim("this "+ustrunescape("\u2000")) = "this"

Domain s: Unicode strings Range: Unicode strings

strtoname(s[,p])

Description: s translated into a Stata 13 compatible name

strtoname() results in a name that is truncated to 32 bytes. Each character in s that is not allowed in a Stata name is converted to an underscore character, $_$. If the first character in s is a numeric character and p is not 0, then the result is prefixed with an underscore. Stata 14 names may be 32 characters; see [U] 11.3 Naming conventions.

strtoname("name") = "name"
strtoname("a name") = "a_name"
strtoname("5",1) = "_5"
strtoname("5:30",1) = "_5_30"
strtoname("5",0) = "5"
strtoname("5:30",0) = "5_30"

Domain s: strings
Domain p: integers 0 or 1
Range: strings

ustrtoname(s[,p])

Description: string s translated into a Stata name

ustrtoname() results in a name that is truncated to 32 characters. Each character in s that is not allowed in a Stata name is converted to an underscore character, _. If the first character in s is a numeric character and p is not 0, then the result is prefixed with an underscore.

ustrtoname("name",1) = "name"
ustrtoname("the médiane") = "the_médiane"
ustrtoname("Omédiane") = "_Omédiane"
ustrtoname("Omédiane", 1) = "_Omédiane"
ustrtoname("Omédiane", 0) = "Omédiane"

Domain s: Unicode strings
Domain p: integers 0 or 1
Range: Unicode strings

strtrim(s)

Description: s without leading and trailing blanks (ASCII space character char(32)); equivalent

to strltrim(strrtrim(s))

strtrim(" this ") = "this"

Domain s: strings

Range: strings without leading or trailing blanks

ustrtrim(s)

Description: removes leading and trailing Unicode whitespace characters and blanks from the

Unicode string s

Note that, in addition to char(32), ASCII characters char(9), char(10), char(11), char(12), and char(13) are considered whitespace characters in

the Unicode standard.

ustrtrim(" this ") = "this"

ustrtrim(char(11)+" this ")+char(13) = "this"

ustrtrim(" this "+ustrunescape("\u2000")) = "this"

Domain s: Unicode strings Range: Unicode strings

strupper(s)

Description: uppercase ASCII characters in string s

Unicode characters beyond the plain ASCII range are ignored.

strupper("this") = "THIS"
strupper("café") = "CAFé"

Domain s: strings

Range: strings with uppercased characters

ustrupper(s[,loc])

Description: uppercase all characters in string s under the given locale loc

If loc is not specified, the default locale is used. The same s but a different loc may produce different results; for example, the uppercase letter of "i" is "I" in English, but "I" with a dot in Turkish. The result can be longer or shorter than the input string in bytes; for example, the uppercase form of the German letter β (code point 0.00df) is two capital letters "SS".

ustrupper("médiane","fr") = "MÉDIANE"
ustrupper("Rußland", "de") = "RUSSLAND"
ustrupper("istanbul", "tr") = "İSTANBUL"

Domain s: Unicode strings
Domain loc: locale name
Range: Unicode strings

```
subinstr(s_1, s_2, s_3, n)
```

Description: s_1 , where the first n occurrences in s_1 of s_2 have been replaced with s_3

subinstr() is intended for use only with plain ASCII characters and for use by programmers who want to perform byte-based substitution. Note that any Unicode character beyond ASCII range (code point greater than 127) takes more than 1 byte in the UTF-8 encoding; for example, é takes 2 bytes.

To perform character-based replacement in Unicode strings, see usubinstr().

If n is missing, all occurrences are replaced.

Also see regexm(), regexr(), and regexs().

subinstr("this is the day","is","X",1) = "thX is the day"
subinstr("this is the hour","is","X",2) = "thX X the hour"
subinstr("this is this","is","X",.) = "thX X thX"

Domain s_1 : strings (to be substituted into)
Domain s_2 : strings (to be substituted from)
Domain s_3 : strings (to be substituted with)

Domain n: integers ≥ 0 or missing

Range: strings

usubinstr (s_1, s_2, s_3, n)

Description: replaces the first n occurrences of the Unicode string s_2 with the Unicode string

 s_3 in s_1

If n is *missing*, all occurrences are replaced. An invalid UTF-8 sequence in s_1 , s_2 , or s_3 is replaced with a Unicode replacement character \ufffd before replacement is performed.

usubinstr("de très près","ès","es",1) = "de tres près"
usubinstr("de très pr'es","ès","X",2) = "de trX prX"

Domain s_1 : Unicode strings (to be substituted into) Domain s_2 : Unicode strings (to be substituted from) Domain s_3 : Unicode strings (to be substituted with)

Domain n: integers ≥ 0 or missing

Range: Unicode strings

 $subinword(s_1, s_2, s_3, n)$

Description: s_1 , where the first n occurrences in s_1 of s_2 as a word have been replaced with

A word is defined as a space-separated token. A token at the beginning or end of s_1 is considered space-separated. This is different from a Unicode word, which is a language unit based on either a set of word-boundary rules or dictionaries for several languages (Chinese, Japanese, and Thai). If n is missing, all occurrences are replaced.

Also see regexm(), regexr(), and regexs().

subinword("this is the day","is","X",1) = "this X the day"
subinword("this is the hour","is","X",.) = "this X the hour"
subinword("this is this","th","X",.) = "this is this"

Domain s_1 : strings (to be substituted for) Domain s_2 : strings (to be substituted from) Domain s_3 : strings (to be substituted with) Domain n: integers ≥ 0 or missing

Range: strings

 $substr(s, n_1, n_2)$

Description: the substring of s, starting at n_1 , for a length of n_2

substr() is intended for use only with plain ASCII characters and for use by programmers who want to extract a subset of bytes from a string. For those with plain ASCII text, n_1 is the starting character, and n_2 is the length of the string in characters. For programmers, substr() is technically a byte-based function. For plain ASCII characters, the two are equivalent but you can operate on byte values beyond that range. Note that any Unicode character beyond ASCII range (code point greater than 127) takes more than 1 byte in the UTF-8 encoding; for example, \acute{e} takes 2 bytes.

To obtain substrings of Unicode strings, see usubstr().

If $n_1 < 0$, n_1 is interpreted as the distance from the end of the string; if $n_2 = .$ (missing), the remaining portion of the string is returned.

substr("abcdef",2,3) = "bcd"
substr("abcdef",-3,2) = "de"
substr("abcdef",2,.) = "bcdef"
substr("abcdef",-3,.) = "def"
substr("abcdef",2,0) = ""
substr("abcdef",15,2) = ""

Domain s: strings

Domain n_1 : integers ≥ 1 and ≤ -1

Domain n_2 : integers ≥ 1 Range: strings

usubstr(s, n_1, n_2)

Description: the Unicode substring of s, starting at n_1 , for a length of n_2

If $n_1 < 0$, n_1 is interpreted as the distance from the last character of the s; if $n_2 = .$ (missing), the remaining portion of the Unicode string is returned.

usubstr("médiane",2,3) = "édi"
usubstr("médiane",-3,2) = "an"
usubstr("médiane",2,.) = "édiane"

Domain s: Unicode strings

Domain n_1 : integers ≥ 1 and ≤ -1

Domain n_2 : integers ≥ 1 Range: Unicode strings

$udsubstr(s, n_1, n_2)$

Description: the Unicode substring of s, starting at character n_1 , for n_2 display columns

If $n_2 = .$ (missing), the remaining portion of the Unicode string is returned. If n_2 display columns from n_1 is in the middle of a Unicode character, the substring stops at the previous Unicode character.

udsubstr("médiane",2,3) = "édi"

udsubstr("中值",1,1) = "" udsubstr("中值",1,2) = "中"

Domain s:Unicode stringsDomain n_1 :integers ≥ 1 Domain n_2 :integers ≥ 1 Range:Unicode strings

tobytes(s[,n])

Description: escaped decimal or hex digit strings of up to 200 bytes of s

The escaped decimal digit string is in the form of \DDD . The escaped hex digit string is in the form of \xh . If n is not specified or is 0, the decimal form is produced. Otherwise, the hex form is produced.

tobytes("abc") = " $d097\\d098\\d099$ " tobytes("abc", 1) = " $x61\\x62\\x63$ "

 $tobytes("café") = "\d099\d097\d102\d195\d169"$

Domain s: Unicode strings

Domain *n*: integers Range: strings

uisdigit(s)

Description: 1 if the first Unicode character in s is a Unicode decimal digit; otherwise, 0

A Unicode decimal digit is a Unicode character with the character property Nd according to the Unicode standard. The function returns -1 if the string starts with

an invalid UTF-8 sequence.

Domain s: Unicode strings

Range: integers

uisletter(s)

Description: 1 if the first Unicode character in s is a Unicode letter; otherwise, 0

A Unicode letter is a Unicode character with the character property L according to the Unicode standard. The function returns -1 if the string starts with an invalid

UTF-8 sequence.

Domain s: Unicode strings

Range: integers

 $ustrcompare(s_1, s_2[, loc])$

Description: compares two Unicode strings

The function returns -1, 1, or 0 if s_1 is less than, greater than, or equal to s_2 . The function may return a negative number other than -1 if an error happens. The comparison is locale dependent. For example, $z < \ddot{o}$ in Swedish but $\ddot{o} < z$ in German. If loc is not specified, the default locale is used. The comparison is diacritic and case sensitive. If you need different behavior, for example, case-insensitive comparison, you should use the extended comparison function ustrcompareex(). Unicode string comparison compares Unicode strings in a language-sensitive manner. On the other hand, the sort command compares strings in code-point (binary) order. For example, uppercase "Z" (code-point value 90) comes before lowercase "a" (code-point value 97) in code-point order but comes after "a" in any English dictionary.

 $\begin{array}{l} {\rm ustrcompare("z", "\"o", "sv") = -1} \\ {\rm ustrcompare("z", "\"o", "de") = 1} \end{array}$

 $\begin{array}{lll} \text{Domain } s_1: & \text{Unicode strings} \\ \text{Domain } s_2: & \text{Unicode strings} \\ \text{Domain } loc: & \text{Unicode strings} \\ \end{array}$

Range: integers

 $ustrcompareex(s_1, s_2, loc, st, case, cslv, norm, num, alt, fr)$

Description: compares two Unicode strings

The function returns -1, 1, or 0 if s_1 is less than, greater than, or equal to s_2 . The function may return a negative number other than -1 if an error occurs. The comparison is locale dependent. For example, $z < \ddot{o}$ in Swedish but $\ddot{o} < z$ in German. If loc is not specified, the default locale is used.

st controls the strength of the comparison. Possible values are 1 (primary), 2 (secondary), 3 (tertiary), 4 (quaternary), or 5 (identical). –1 means to use the default value for the locale. Any other numbers are treated as tertiary. The primary difference represents base letter differences; for example, letter "a" and letter "b" have primary differences. The secondary difference represents diacritical differences on the same base letter; for example, letters "a" and "ä" have secondary differences. The tertiary difference represents case differences of the same base letter; for example, letters "a" and "A" have tertiary differences. Quaternary strength is useful to distinguish between Katakana and Hiragana for the JIS 4061 collation standard. Identical strength is essentially the code-point order of the string, hence, is rarely useful.

```
 ustrcompareex("café","cafe","fr", 1, -1, -1, -1, -1, -1, -1, -1) = 0 \\ ustrcompareex("café","cafe","fr", 2, -1, -1, -1, -1, -1, -1) = 1 \\ ustrcompareex("Café","café","fr", 3, -1, -1, -1, -1, -1, -1) = 1 \\ value ("Café","café","café","fr", 3, -1, -1, -1, -1, -1, -1, -1) = 1 \\ value ("Café","café","café","fr", 3, -1, -1, -1, -1, -1, -1, -1) = 1 \\ value ("Café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","café","c
```

case controls the uppercase and lowercase letter order. Possible values are 0 (use order specified in tertiary strength), 1 (uppercase first), or 2 (lowercase first). -1 means to use the default value for the locale. Any other values are treated as 0.

```
ustrcompareex("Café", "café", "fr", -1, 1, -1, -1, -1, -1, -1) = -1 ustrcompareex("Café", "café", "fr", -1, 2, -1, -1, -1, -1, -1) = 1
```

cslv controls whether an extra case level between the secondary level and the tertiary level is generated. Possible values are 0 (off) or 1 (on). -1 means to use the default value for the locale. Any other values are treated as 0. Combining this setting to be "on" and the strength setting to be primary can achieve the effect of ignoring the diacritical differences but preserving the case differences. If the setting is "on", the result is also affected by the case setting.

```
ustrcompareex("café", "Cafe", "fr", 1, -1, 1, -1, -1, -1, -1) = -1 ustrcompareex("café", "Cafe", "fr", 1, 1, 1, -1, -1, -1, -1) = 1
```

norm controls whether the normalization check and normalizations are performed. Possible values are 0 (off) or 1 (on). -1 means to use the default value for the locale. Any other values are treated as 0. Most languages do not require normalization for comparison. Normalization is needed in languages that use multiple combining characters such as Arabic, ancient Greek, or Hebrew.

num controls how contiguous digit substrings are sorted. Possible values are 0 (off) or 1 (on). -1 means to use the default value for the locale. Any other values are treated as 0. If the setting is "on", substrings consisting of digits are sorted based on the numeric value. For example, "100" is after value "20" instead of before it. Note that the digit substring is limited to 254 digits, and plus/minus signs, decimals, or exponents are not supported.

```
ustrcompareex("100", "20", "en", -1, -1, -1, -1, 0, -1, -1) = -1 ustrcompareex("100", "20", "en", -1, -1, -1, -1, 1, -1, -1) = 1
```

alt controls how spaces and punctuation characters are handled. Possible values are 0 (use primary strength) or 1 (alternative handling). Any other values are treated as 0. If the setting is 1 (alternative handling), "onsite", "on-site", and "on site" are considered equals.

fr controls the direction of the secondary strength. Possible values are 0 (off) or 1 (on). -1 means to use the default value for the locale. All other values are treated as "off". If the setting is "on", the diacritical letters are sorted backward. Note that the setting is "on" by default only for Canadian French (locale fr_CA).

```
 \begin{array}{lll} ustrcompareex("coté", "côte", "fr_CA", -1, -1, -1, -1, -1, -1, 0) = -1 \\ ustrcompareex("coté", "côte", "fr_CA", -1, -1, -1, -1, -1, -1, 1) = 1 \\ ustrcompareex("coté", "côte", "fr_CA", -1, -1, -1, -1, -1, -1, -1) = 1 \\ ustrcompareex("coté", "côte", "fr", -1, -1, -1, -1, -1, -1, -1) = 1 \\ \end{array}
```

Domain s_1 : Unicode strings Domain s_2 : Unicode strings Domain loc: Unicode strings

ustrfix(s[,rep])

Description: replaces each invalid UTF-8 sequence with a Unicode character

In the one-argument case, the Unicode replacement character $\$ is used. In the two-argument case, the first Unicode character of rep is used. If rep starts with an invalid UTF-8 sequence, then Unicode replacement character $\$ ufffd is used. Note that an invalid UTF-8 sequence can contain one byte or multiple bytes.

```
ustrfix(char(200)) = ustrunescape("\ufffd")
ustrfix("ab"+char(200)+"cdé", "") = "abcdé"
ustrfix("ab"+char(229)+char(174)+"cdé", "é") = "abécdé"
```

Domain s: Unicode strings
Domain rep: Unicode character
Range: Unicode strings

ustrfrom(s,enc,mode)

Description: converts the string s in encoding enc to a UTF-8 encoded Unicode string

mode controls how invalid byte sequences in s are handled. The possible values are 1, which substitutes an invalid byte sequence with a Unicode replacement character \ufffd; 2, which skips any invalid byte sequences; 3, which stops at the first invalid byte sequence and returns an empty string; or 4, which replaces any byte in an invalid sequence with an escaped hex digit sequence %Xhh. Any other values are treated as 1. A good use of value 4 is to check what invalid bytes a Unicode string ust contains by examining the result of ustrfrom(ust, "utf-8", 4).

Also see ustrto().

Domain s: strings in encoding enc

Domain *enc*: Unicode strings Domain *mode*: integers

Range: Unicode strings

ustrinvalidcnt(s)

Description: the number of invalid UTF-8 sequences in s

An invalid UTF-8 sequence may contain one byte or multiple bytes.

ustrinvalidcnt("médiane") = 0

ustrinvalidcnt("médiane"+char(229)) = 1

ustrinvalidcnt("médiane"+char(229)+char(174)) = 1
ustrinvalidcnt("médiane"+char(174)+char(158)) = 2

Domain s: Unicode strings

Range: integers

ustrleft(s,n)

Description: the first n Unicode characters of the Unicode string s

An invalid UTF-8 sequence is replaced with a Unicode replacement character

\ufffd.

ustrleft("Экспериментальные",3) = "Экс" ustrleft("Экспериментальные",5) = "Экспе"

Domain s: Unicode strings

Domain n: integers

Range: Unicode strings

ustrnormalize(s, norm)

Description: normalizes Unicode string s to one of the five normalization forms specified by norm

The normalization forms are nfc, nfd, nfkc, nfkd, or nfkcc. The function returns an empty string for any other value of *norm*. Unicode normalization removes the Unicode string differences caused by Unicode character equivalence. nfc specifies Normalization Form C, which normalizes decomposed Unicode code points to a composited form. nfd specifies Normalization Form D, which normalizes composited Unicode code points to a decomposed form. nfc and nfd produce canonical equivalent form. nfkc and nfkd are similar to nfc and nfd but produce compatibility equivalent forms. nfkcc specifies nfkc with casefolding. This normalization and casefolding implement the Unicode Character Database.

In the Unicode standard, both "i" (\u0069 followed by a diaeresis \u00308) and the composite character \u00ef represent "i" with 2 dots as in "naïve". Hence, the code-point sequence \u0069\u00308 and the code point \u00ef are considered Unicode equivalent. According to the Unicode standard, they should be treated as the same single character in Unicode string operations, such as in display, comparison, and selection. However, Stata does not support multiple code-point characters; each code point is considered a separate Unicode character. Hence, \u00e9\u00308 is displayed as two characters in the Results window. ustrnormalize() can be used with "nfc" to normalize \u0069\u00308 to the canonical equivalent composited code point \u00ef.

ustrnormalize(ustrunescape("\u0069\u0308"), "nfc") = "ï"

The decomposed form nfd can be used to removed diacritical marks from base letters. First, normalize the Unicode string to canonical decomposed form, and then call ustrto() with mode skip to skip all non-ASCII characters.

Also see ustrfrom().

ustrto(ustrnormalize("café", "nfd"), "ascii", 2) = "cafe"

Domain s: Unicode strings Domain norm: Unicode strings Range: Unicode strings

ustrright(s,n)

Description: the last n Unicode characters of the Unicode string s

An invalid UTF-8 sequence is replaced with a Unicode replacement character

\ufffd.

ustrright("Экспериментальные",3) = "ные" ustrright("Экспериментальные",5) = "льные"

Domain s: Unicode strings

Domain n: integers

Range: Unicode strings

ustrsortkey(s[,loc])

Description: generates a null-terminated byte array that can be used by the sort command to

produce the same order as ustrcompare()

The function may return an empty array if an error occurs. The result is locale dependent. If loc is not specified, the default locale is used. The result is also diacritic and case sensitive. If you need different behavior, for example, case-insensitive results, you should use the extended function ustrsortkeyex(). See [U] 12.4.2.5 Sorting strings containing Unicode characters for details and

examples.

Domain s: Unicode strings
Domain loc: Unicode strings

Range: null-terminated byte array

ustrsortkeyex(s, loc, case, cslv, norm, num, alt, fr)

Description: generates a null-terminated byte array that can be used by the sort command to produce the same order as ustrcompare()

The function may return an empty array if an error occurs. The result is locale dependent. If *loc* is not specified, the default locale is used. See [U] **12.4.2.5 Sorting strings containing Unicode characters** for details and examples.

st controls the strength of the comparison. Possible values are 1 (primary), 2 (secondary), 3 (tertiary), 4 (quaternary), or 5 (identical). -1 means to use the default value for the locale. Any other numbers are treated as tertiary. The primary difference represents base letter differences; for example, letter "a" and letter "b" have primary differences. The secondary difference represents diacritical differences on the same base letter; for example, letters "a" and "a" have secondary differences. The tertiary difference represents case differences of the same base letters; for example, letters "a" and "A" have tertiary differences. Quaternary strength is useful to distinguish between Katakana and Hiragana for the JIS 4061 collation standard. Identical strength is essentially the code-point order of the string and, hence, is rarely useful.

case controls the uppercase and lowercase letter order. Possible values are 0 (use order specified in tertiary strength), 1 (uppercase first), or 2 (lowercase first). -1 means to use the default value for the locale. Any other values are treated as 0.

cslv controls if an extra case level between the secondary level and the tertiary level is generated. Possible values are 0 (off) or 1 (on). -1 means to use the default value for the locale. Any other values are treated as 0. Combining this setting to be "on" and the strength setting to be primary can achieve the effect of ignoring the diacritical differences but preserving the case differences. If the setting is "on", the result is also affected by the case setting.

norm controls whether the normalization check and normalizations are performed. Possible values are 0 (off) or 1 (on). -1 means to use the default value for the locale. Any other values are treated as 0. Most languages do not require normalization for comparison. Normalization is needed in languages that use multiple combining characters such as Arabic, ancient Greek, or Hebrew.

num controls how contiguous digit substrings are sorted. Possible values are 0 (off) or 1 (on). -1 means to use the default value for the locale. Any other values are treated as 0. If the setting is "on", substrings consisting of digits are sorted based on the numeric value. For example, "100" is after "20" instead of before it. Note that the digit substring is limited to 254 digits, and plus/minus signs, decimals, or exponents are not supported.

alt controls how spaces and punctuation characters are handled. Possible values are 0 (use primary strength) or 1 (alternative handling). Any other values are treated as 0. If the setting is 1 (alternative handling), "onsite", "on-site", and "on site" are considered equals.

fr controls the direction of the secondary strength. Possible values are 0 (off) or 1 (on). -1 means to use the default value for the locale. All other values are treated as "off". If the setting is "on", the diacritical letters are sorted backward. Note that the setting is "on" by default only for Canadian French (locale fr_CA).

Domain s: Unicode strings Domain loc: Unicode strings

Domain st: integers Domain case: integers Domain cslv: integers Domain norm: integers Domain num: integers Domain alt: integers Domain fr: integers

Range: null-terminated byte array

ustrto(s, enc, mode)

Description: converts the Unicode string s in UTF-8 encoding to a string in encoding enc

See [D] unicode encoding for details on available encodings. Any invalid sequence in s is replaced with a Unicode replacement character \ufffd. mode controls how unsupported Unicode characters in the encoding enc are handled. The possible values are 1, which substitutes any unsupported characters with the enc's substitution strings (the substitution character for both ascii and latin1 is char(26)); 2, which skips any unsupported characters; 3, which stops at the first unsupported character and returns an empty string; or 4, which replaces any unsupported character with an escaped hex digit sequence \uhhhh or \Uhhhhhhhh. The hex digit sequence contains either 4 or 8 hex digits, depending if the Unicode character's code-point value is less than or greater than \uffff. Any other values are treated as 1.

```
ustrto("café", "ascii", 1) = "caf"+char(26)
ustrto("café", "ascii", 2) = "caf"
ustrto("café", "ascii", 3) = ""
ustrto("café", "ascii", 4) = "caf\u00E9"
```

ustrto() can be used to removed diacritical marks from base letters. First, normalize the Unicode string to NFD form using ustrnormalize(), and then call ustrto() with value 2 to skip all non-ASCII characters.

Also see ustrfrom().

```
ustrto(ustrnormalize("café", "nfd"), "ascii", 2) = "cafe"
```

Domain s: Unicode strings
Domain enc: Unicode strings

Domain mode: integers

Range: strings in encoding enc

ustrtohex(s[,n])

Description: escaped hex digit string of s up to 200 Unicode characters

The escaped hex digit string is in the form of \uhhhh for code points less than \uffff or \Uhhhhhhhhh for code points greater than \uffff. The function starts at the nth Unicode character of s if n is specified and larger than 0. Any invalid UTF-8 sequence is replaced with a Unicode replacement character \ufffd. Note that the null terminator char(0) is a valid Unicode character. Function ustrunescape() can be applied on the result to get back the original Unicode string s if s does not contain any invalid UTF-8 sequences.

Also see ustrunescape().

ustrtohex("нуπю") = "\u043d\u0443\u043b\u044e" ustrtohex("нуπю", 2) = "\u0443\u043b\u044e" ustrtohex("i"+char(200)+char(0)+"s") = "\u0069\ufffd\u0000\u0073"

Domain s: Unicode strings Domain n: integers ≥ 1 Range: strings

ustrunescape(s)

Description: the Unicode string corresponding to the escaped sequences of s

The following escape sequences are recognized: 4 hex digit form \uhhhh; 8 hex digit form \Uhhhhhhhh; 1-2 hex digit form \xhh; and 1-3 octal digit form \ooo, where h is [0-9A-Fa-f] and o is [0-7]. The standard ANSI C escapes \a, \b, \t, \n, \v, \f, \r, \e, \", \', \?, \\ are recognized as well. The function returns an empty string if an escape sequence is badly formed. Note that the 8 hex digit form \Uhhhhhhhhh begins with a capital letter "U".

Also see ustrtohex().

ustrunescape("\u043d\u0443\u043b\u044e") = "нулю"

Domain s: strings of escaped hex values

Range: Unicode strings

word(s,n)

Description: the nth word in s; missing ("") if n is missing

Positive numbers count words from the beginning of s, and negative numbers count words from the end of s. (1 is the first word in s, and -1 is the last word in s.) A word is a set of characters that start and terminate with spaces. This is different from a Unicode word, which is a language unit based on either a set of word-boundary rules or dictionaries for several languages (Chinese, Japanese, and Thai).

Domain s: strings
Domain n: integers
Range: strings

ustrword(s,n[,loc])

Description: the nth Unicode word in the Unicode string s

Positive n counts Unicode words from the beginning of s, and negative n counts Unicode words from the end of s. For examples, n equal to 1 returns the first word in s, and n equal to -1 returns the last word in s. If loc is not specified, the default locale is used. A Unicode word is different from a Stata word produced by the word() function. A Stata word is a space-separated token. A Unicode word is a language unit based on either a set of word-boundary rules or dictionaries for some languages (Chinese, Japanese, and Thai). The function returns missing ("") if n is greater than cnt or less than -cnt, where cnt is the number of words s contains. cnt can be obtained from ustrwordcount(). The function also returns missing ("") if an error occurs.

ustrword("Parlez-vous français", 1, "fr") = "Parlez"
ustrword("Parlez-vous français", 2, "fr") = "-"

ustrword("Parlez-vous français",-1, "fr") = "français" ustrword("Parlez-vous français",-2, "fr") = "vous"

Domain s: Unicode strings Domain loc: Unicode strings

Domain n: integers

Range: Unicode strings

wordbreaklocale(loc, type)

Description: the most closely related locale supported by ICU from loc if type is 1, the actual

locale where the word-boundary analysis data come from if type is 2; or an empty

string is returned for any other type

wordbreaklocale("en_us_texas", 1) = en_US
wordbreaklocale("en_us_texas", 2) = root

Domain *loc*: strings of locale name

Domain *type*: integers Range: strings

wordcount(s)

Description: the number of words in s

A word is a set of characters that starts and terminates with spaces, starts with the beginning of the string, or terminates with the end of the string. This is different from a Unicode word, which is a language unit based on either a set of word-boundary rules or dictionaries for several languages (Chinese, Japanese, and

Thai).

Domain s: strings

Range: nonnegative integers 0, 1, 2, ...

ustrwordcount(s[,loc])

Description: the number of nonempty Unicode words in the Unicode string s

An empty Unicode word is a Unicode word consisting of only Unicode whitespace characters. If *loc* is not specified, the default locale is used. A Unicode word is different from a Stata word produced by the word() function. A Stata word is a space-separated token. A Unicode word is a language unit based on either a set of word-boundary rules or dictionaries for some languages (Chinese, Japanese, and Thai). The function may return a negative number if an error occurs.

ustrwordcount("Parlez-vous français", "fr") = 4

Domain s: Unicode strings Domain loc: Unicode strings

Range: integers

References

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Jeanty, P. W. 2013. Dealing with identifier variables in data management and analysis. Stata Journal 13: 699-718.

Koplenig, A. 2018. Stata tip 129: Efficiently processing textual data with Stata's new Unicode features. Stata Journal 18: 287–289.

Schwarz, C. 2019. Isemantica: A command for text similarity based on latent semantic analysis. Stata Journal 19: 129–142.

Also see

- [FN] Functions by category
- [D] egen Extensions to generate
- [D] **generate** Create or change contents of variable
- [M-4] **String** String manipulation functions
- [U] 12.4.2 Handling Unicode strings
- [U] 13.2.2 String operators
- [U] 13.3 Functions

Title

Trigonometric functions

Contents	Functions	References	Also see
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Contents

 $a\cos(x)$

acosh(x)	the inverse hyperbolic cosine of x	
asin(x)	the radian value of the arcsine of x	
asinh(x)	the inverse hyperbolic sine of x	
atan(x)	the radian value of the arctangent of x	
atan2(y, x)	the radian value of the arctangent of y/x , where the signs of the parameters y and x are used to determine the quadrant of the answer	
atanh(x)	the inverse hyperbolic tangent of x	
cos(x)	the cosine of x , where x is in radians	
cosh(x)	the hyperbolic cosine of x	

the sine of x, where x is in radians

the radian value of the arccosine of x

sinh(x) the hyperbolic sine of x

tan(x) the tangent of x, where x is in radians

tanh(x) the hyperbolic tangent of x

Functions

sin(x)

acos(x)

Description: the radian value of the arccosine of x

Domain: -1 to 1 Range: 0 to π

acosh(x)

Description: the inverse hyperbolic cosine of x

 $a\cosh(x) = \ln(x + \sqrt{x^2 - 1})$

Domain: 1 to 8.9e+307 Range: 0 to 709.77

asin(x)

Description: the radian value of the arcsine of x

Domain: -1 to 1 Range: $-\pi/2$ to $\pi/2$

asinh(x)

Description: the inverse hyperbolic sine of x

 $asinh(x) = ln(x + \sqrt{x^2 + 1})$

Domain: -8.9e+307 to 8.9e+307 Range: -709.77 to 709.77

atan(x)

Description: the radian value of the arctangent of x

Domain: -8e+307 to 8e+307

Range: $-\pi/2$ to $\pi/2$

atan2(y, x)

Description: the radian value of the arctangent of y/x, where the signs of the parameters y and

x are used to determine the quadrant of the answer

Domain y: -8e+307 to 8e+307Domain x: -8e+307 to 8e+307

Range: $-\pi$ to π

atanh(x)

Description: the inverse hyperbolic tangent of x

 $atanh(x) = \frac{1}{2} \{ \ln(1+x) - \ln(1-x) \}$

Domain: -1 to 1

Range: -8e+307 to 8e+307

cos(x)

Description: the cosine of x, where x is in radians

Domain: -1e+18 to 1e+18

Range: -1 to 1

cosh(x)

Description: the hyperbolic cosine of x

 $\cosh(x) = \{\exp(x) + \exp(-x)\}/2$

Domain: -709 to 709 Range: 1 to 4.11e+307

sin(x)

Description: the sine of x, where x is in radians

Domain: -1e+18 to 1e+18

Range: -1 to 1

sinh(x)

Description: the hyperbolic sine of x

 $\sinh(x) = \{\exp(x) - \exp(-x)\}/2$

Domain: -709 to 709

Range: -4.11e+307 to 4.11e+307

tan(x)

Description: the tangent of x, where x is in radians

Domain: -1e+18 to 1e+18

Range: -1e+17 to 1e+17 or missing

tanh(x)

Description: the hyperbolic tangent of x

 $tanh(x) = \{\exp(x) - \exp(-x)\}/\{\exp(x) + \exp(-x)\}$

Domain: -8e+307 to 8e+307Range: -1 to 1 or missing

□ Technical note

The trigonometric functions are defined in terms of radians. There are 2π radians in a circle. If you prefer to think in terms of degrees, because there are also 360 degrees in a circle, you may convert degrees into radians by using the formula $r=d\pi/180$, where d represents degrees and r represents radians. Stata includes the built-in constant $_{-}$ pi, equal to π to machine precision. Thus, to calculate the sine of theta, where theta is measured in degrees, you could type

atan() similarly returns radians, not degrees. The arccotangent can be obtained as

$$acot(x) = pi/2 - atan(x)$$

References

Norton, E. C. 2022. The inverse hyperbolic sine transformation and retransformed marginal effects. *Stata Journal* 22: 702–712.

Oldham, K. B., J. C. Myland, and J. Spanier. 2009. An Atlas of Functions. 2nd ed. New York: Springer.

Also see

- [FN] Functions by category
- [D] **egen** Extensions to generate
- [D] generate Create or change contents of variable
- [M-5] **sin**() Trigonometric and hyperbolic functions
- [U] 13.3 Functions

Subject and author index

See the combined subject index and the combined author index in the Stata Index.