

betareg — Beta regression[Description](#)[Quick start](#)[Menu](#)[Syntax](#)[Options](#)[Remarks and examples](#)[Stored results](#)[Methods and formulas](#)[Acknowledgments](#)[References](#)[Also see](#)

Description

`betareg` estimates the parameters of a beta regression model. This model accommodates dependent variables that are greater than 0 and less than 1, such as rates, proportions, and fractional data.

Quick start

Beta regression of y on x_1 and x_2

```
betareg y x1 x2
```

Add categorical variable `a` using [factor-variable](#) syntax

```
betareg y x1 x2 i.a
```

Add covariates for scale

```
betareg y x1 x2 i.a, scale(x1 z1)
```

Same as above, but use probit link for conditional mean and square-root link for conditional scale

```
betareg y x1 x2 i.a, scale(x1 z1) link(probit) slink(root)
```

Beta regression of y on x_1 and x_2 with robust standard errors

```
betareg y x1 x2, vce(robust)
```

Menu

Statistics > Fractional outcomes > Beta regression

Syntax

```
betareg depvar indepvars [if] [in] [weight] [, options]
```

<i>options</i>	Description
Model	
<code><u>noconstant</u></code>	suppress constant term
<code><u>scale</u>(<i>varlist</i> [, <u>noconstant</u>])</code>	specify independent variables for scale
<code><u>link</u>(<i>linkname</i>)</code>	specify link function for the conditional mean; default is <code>link(logit)</code>
<code><u>slink</u>(<i>slinkname</i>)</code>	specify link function for the conditional scale; default is <code>slink(log)</code>
<code><u>constraints</u>(<i>constraints</i>)</code>	apply specified linear constraints
SE/Robust	
<code><u>vce</u>(<i>vcetype</i>)</code>	<i>vcetype</i> may be <code>oim</code> , <code>robust</code> , <code>cluster <i>clustvar</i></code> , <code>bootstrap</code> , or <code>jackknife</code>
Reporting	
<code><u>level</u>(#)</code>	set confidence level; default is <code>level(95)</code>
<code><u>nocnsreport</u></code>	do not display constraints
<code><u>display_options</u></code>	control columns and column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling
Maximization	
<code><u>maximize_options</u></code>	control the maximization process; seldom used
<code><u>coeflegend</u></code>	display legend instead of statistics

<i>linkname</i>	Description
<code>logit</code>	logit
<code>probit</code>	probit
<code>cloglog</code>	complementary log–log
<code>loglog</code>	log–log

<i>slinkname</i>	Description
<code>log</code>	log
<code>root</code>	square root
<code>identity</code>	identity

indepvars and *varlist* specified in `scale()` may contain factor variables; see [U] 11.4.3 **Factor variables**.

`bayes`, `bootstrap`, `by`, `collect`, `fmm`, `fp`, `jackknife`, `nestreg`, `rolling`, `statsby`, `stepwise`, and `svy` are allowed; see [U] 11.1.10 **Prefix commands**. For more details, see [BAYES] `bayes: betareg` and [FMM] `fmm: betareg`.

Weights are not allowed with the `bootstrap` prefix; see [R] **bootstrap**.

`vce()` and weights are not allowed with the `svy` prefix; see [SVY] **svy**.

`fweights`, `iweights`, and `pweights` are allowed; see [U] 11.1.6 **weight**.

`coeflegend` does not appear in the dialog box.

See [U] 20 **Estimation and postestimation commands** for more capabilities of estimation commands.

Options

Model

`noconstant`; see [R] [Estimation options](#).

`scale(varlist [, noconstant])` specifies the independent variables used to model the scale.

`noconstant` suppresses the constant term in the scale model. A constant term is included by default.

`link(linkname)` specifies the link function used for the conditional mean. *linkname* may be `logit`, `probit`, `cloglog`, or `loglog`. The default is `link(logit)`.

`slink(slinkname)` specifies the link function used for the conditional scale. *slinkname* may be `log`, `root`, or `identity`. The default is `slink(log)`.

`constraints(constraints)`; see [R] [Estimation options](#).

SE/Robust

`vce(vcetype)` specifies the type of standard error reported, which includes types that are derived from asymptotic theory (`oim`), that are robust to some kinds of misspecification (`robust`), that allow for intragroup correlation (`cluster clustvar`), and that use bootstrap or jackknife methods (`bootstrap`, `jackknife`); see [R] [vce_option](#).

Reporting

`level(#)`, `nocnsreport`; see [R] [Estimation options](#).

`display_options`: `nocl`, `nopvalues`, `noomitted`, `vsquish`, `noemptycells`, `baselevels`, `allbaselevels`, `nofvlabel`, `fvwrap(#)`, `fvwrapon(style)`, `cformat(%fmt)`, `pformat(%fmt)`, `sformat(%fmt)`, and `nolstretch`; see [R] [Estimation options](#).

Maximization

`maximize_options`: `difficult`, `technique(algorithm_spec)`, `iterate(#)`, `[no]log`, `trace`, `gradient`, `showstep`, `hessian`, `showtolerance`, `tolerance(#)`, `ltolerance(#)`, `nrtolerance(#)`, `nonrntolerance`, and `from(init_specs)`; see [R] [Maximize](#). These options are seldom used.

The following option is available with `betareg` but is not shown in the dialog box:

`coeflegend`; see [R] [Estimation options](#).

Remarks and examples

[stata.com](http://www.stata.com)

Dependent variables such as rates, proportions, and fractional data are frequently greater than 0 and less than 1. There are a variety of methods to model such variables, including beta regression and fractional logistic regression.

Beta regression is widely used because of its flexibility for modeling variables between 0 and 1 and because its predictions are confined to the same range. However, beta regression models are not appropriate for dependent variables with some observations exactly equal to 0 or 1. See [R] [fracreg](#) for models when the dependent variable can equal 0 or 1 that also make predictions over the same range. The predictions from linear regression models are not constrained to the 0 to 1 interval; thus, they are not widely used for these variables.

These models have applications in a variety of disciplines, such as economics, the social sciences, and health science. For example, [Castellani, Pattitoni, and Scorcu \(2012\)](#) use beta regression to estimate Gini index values for the prices of art by famous and nonfamous artists. In political science, [Paolino \(2001\)](#) explores the advantages of beta regression and reviews its applicability for a variety of research topics such as the proportion of minority applicants deemed eligible for the Rural Housing Loans program and the proportion of a state's gay and lesbian population that is covered by antidiscrimination laws. In psychology, [Smithson, Deady, and Gracik \(2007\)](#) analyzed the relationship between how jurors judged the probability of a defendant's guilt and the verdict in a trial. Finally, beta regression has been used to model quality-adjusted life years in health-economics outcome studies ([Hubben et al. \[2008\]](#); [Basu and Manca \[2012\]](#)).

[Ferrari and Cribari-Neto \(2004\)](#) and [Smithson and Verkuilen \(2006\)](#) derived the beta regression estimators implemented in `betareg`. [Basu and Manca \(2012\)](#) also discuss quasimaximum likelihood inference for these estimators. These estimators augment the inherent flexibility of the beta distribution with functional form choices, known as links.

Beta regression is a model of the mean of the dependent variable y conditional on covariates \mathbf{x} , which we denote by $\mu_{\mathbf{x}}$. Because y is in $(0, 1)$, we must ensure that $\mu_{\mathbf{x}}$ is also in $(0, 1)$. We do this by using the link function for the conditional mean, denoted $g(\cdot)$. This is necessary because linear combinations of the covariates are not otherwise restricted to $(0, 1)$.

Algebraically,

$$g(\mu_{\mathbf{x}}) = \mathbf{x}\beta$$

or, equivalently,

$$\mu_{\mathbf{x}} = g^{-1}(\mathbf{x}\beta)$$

where $g^{-1}(\cdot)$ is the inverse function of $g(\cdot)$. For example, the default logit link implies that

$$\ln\{\mu_{\mathbf{x}}/(1 - \mu_{\mathbf{x}})\} = \mathbf{x}\beta$$

and that

$$\mu_{\mathbf{x}} = \exp(\mathbf{x}\beta) / \{1 + \exp(\mathbf{x}\beta)\}$$

Using a link function to keep the conditional-mean model inside an interval is common in the statistical literature; see [\[R\] glm](#) for additional applications of link functions.

The conditional variance of the beta distribution is

$$\text{Var}(y|\mathbf{x}) = \{\mu_{\mathbf{x}}(1 - \mu_{\mathbf{x}})\} / (1 + \psi)$$

The parameter ψ is known as the scale factor because it rescales the conditional variance. We use the scale link to ensure that $\psi > 0$.

► Example 1: Beta regression model of a rate

Suppose we wish to know whether offering a summer instruction program increases a school's pass rate for a mandatory state exam administered to students. The school-wide pass rate must be between 0 and 1. It is unlikely that any school will have either no students pass or all students pass, so we consider estimating the effect of the summer instruction program using beta regression.

The dataset `sprogram` contains fictional data on the pass rate of 1,000 schools (`prate`). We begin by reading in the data and verifying that `prate` contains no 0s or 1s.

```
. use https://www.stata-press.com/data/r18/sprogram
(Fictional summer program data)
. summarize prate
```

Variable	Obs	Mean	Std. dev.	Min	Max
prate	1,000	.8150803	.1233684	.2986041	.9973584

prate ranges from 0.299 to 0.997, so we proceed with our choice of a beta regression model.

We model prate as a function of a binary indicator for whether the school offered voluntary, half-day instruction to students during the past two summers (`summer`). The summer program should raise the scores of disadvantaged children who otherwise would not have access to programs that maintain their skills through the summer, thereby increasing the total proportion of students who pass the exam the next year.

We include the fraction of students receiving free or reduced-price meals (`freemeals`) and the sum of parents' monetary donations to the school two years earlier (`pdonations`) as additional covariates that measure affluence of the students' parents. We estimate the parameters of this model using the default logit link for the conditional mean and log link for the conditional scale.

```
. betareg prate i.summer freemeals pdonations
Initial:      Log likelihood = 781.55846
Rescale:      Log likelihood = 781.55846
Rescale eq:   Log likelihood = 781.55846
(setting technique to bhxx)
Iteration 0:  Log likelihood = 781.55846
Iteration 1:  Log likelihood = 891.57913
Iteration 2:  Log likelihood = 892.99578
Iteration 3:  Log likelihood = 893.02725
Iteration 4:  Log likelihood = 893.0279
Iteration 5:  Log likelihood = 893.02792
```

```
Beta regression          Number of obs   =      1,000
                        LR chi2(3)             =      164.61
                        Prob > chi2            =      0.0000

Link function   :  g(u) = log(u/(1-u))      [Logit]
Slink function  :  g(u) = log(u)           [Log]
Log likelihood = 893.02792
```

prate	Coefficient	Std. err.	z	P> z	[95% conf. interval]	
prate						
summer						
Yes	.5560171	.0480307	11.58	0.000	.4618787	.6501555
freemeals	-.4564181	.0834885	-5.47	0.000	-.6200525	-.2927836
pdonations	.0449706	.0097781	4.60	0.000	.025806	.0641353
_cons	1.175013	.0642797	18.28	0.000	1.049027	1.300999
scale						
_cons	2.375433	.0443005	53.62	0.000	2.288606	2.462261

The output table reports the estimated coefficients of the covariates and an estimated scale parameter. The coefficient of the factor variable for `summer==1`, shown as `yes` under `summer`, is significant and positive. Thus we conclude that the summer program was effective at increasing a school's pass rate.

However, we cannot determine the magnitude of the effect from these results. In general, when you use `betareg`, the best way to obtain interpretable effect sizes for the covariates is by using margins. See [example 1](#) in [\[R\] betareg postestimation](#) for more information.

□ Technical note

The results displayed in [example 1](#) can be written concisely in algebraic form. Because we used the default logit link, the estimated conditional mean is

$$\hat{\mu}_{\mathbf{x}} = \exp(\mathbf{x}\hat{\beta}) / \{1 + \exp(\mathbf{x}\hat{\beta})\}$$

where the estimated $\mathbf{x}\hat{\beta}$ is

$$\mathbf{x}\hat{\beta} = -0.456 \times \text{freemeals} + 0.045 \times \text{pdonations} + 0.556 \times (\text{summer}==1) + 1.18$$

The estimated ψ with the default log link for the scale is $\hat{\psi} = \exp(2.38) = 10.80$, which is simply substituted into the formula given [above](#) to express the conditional variance.

See [Methods and formulas](#) for the functional forms of the other links implemented in **betareg** for the conditional mean and scale. □

▷ Example 2: Modeling conditional variance

Some processes require that we model the scale parameter as a function of covariates. For example, we might believe that the proportion of students with free or reduced meals influences the variance of the estimated mean.

We augment [example 1](#) by modeling the scale parameter as a function of `freemeals`.

```
. betareg prate i.summer freemeals pdonations, scale(freemeals)
(output omitted)
Beta regression                               Number of obs   =       1,000
                                                LR chi2(4)      =       169.38
                                                Prob > chi2     =       0.0000

Link function   :  g(u) = log(u/(1-u))         [Logit]
Slink function  :  g(u) = log(u)              [Log]
Log likelihood = 895.41544
```

prate	Coefficient	Std. err.	z	P> z	[95% conf. interval]	
prate						
summer						
Yes	.5571133	.0480378	11.60	0.000	.4629609	.6512658
freemeals	-.5291892	.0896511	-5.90	0.000	-.7049021	-.3534762
pdonations	.0454228	.0097809	4.64	0.000	.0262527	.0645929
_cons	1.209179	.0649585	18.61	0.000	1.081863	1.336495
scale						
freemeals	-.3598137	.1644214	-2.19	0.029	-.6820737	-.0375536
_cons	2.547047	.0882327	28.87	0.000	2.374114	2.71998

Again, we conclude that having a summer program increases the pass rate. The effect of an increase in the proportion of students receiving free meals on the conditional variance is ambiguous because it is in both equations. We can use `margins` to estimate the effect of the program on the conditional mean or the conditional variance. ◀

The estimators in `betareg` are consistent and efficient when the model is correctly specified. [Smithson and Verkuilen \(2006\)](#) discuss model selection for beta regression and note that selecting the model that minimizes the Bayesian information criterion (BIC) will select the correct model in large samples. Selecting the model that minimizes the BIC is a general approach to model selection; see [Cameron and Trivedi \(2005\)](#) for more details.

► Example 3: Model selection

We fit the models `quietly` and use `estimates store` to store the results under the names `model1`, `model2`, `model3`, and `model4`.

```
. quietly betareg prate i.summer freemeals pdonations, scale(freemeals)
. estimates store model1
. quietly betareg prate i.summer freemeals pdonations, scale(freemeals)
> link(cloglog)
. estimates store model2
. quietly betareg prate i.summer freemeals pdonations, scale(freemeals)
> slink(root)
. estimates store model3
. quietly betareg prate i.summer freemeals pdonations, scale(freemeals)
> link(cloglog) slink(root)
. estimates store model4
```

Next, we use `estimates table` to display the coefficients, standard errors, and the BIC for each model.

```
. estimates table model1 model2 model3 model4, stats(bic) se
```

Variable	model1	model2	model3	model4
prate				
summer				
Yes	.55711332	.27762093	.55719742	.27765283
	.04803785	.02460121	.04803698	.02459953
freemeals	-.52918917	-.25685191	-.5300549	-.25729221
	.08965112	.04308385	.08978883	.04314336
pdonations	.04542281	.02162612	.04542462	.02163225
	.00978086	.00444813	.00978099	.00444817
_cons	1.2091789	.37961457	1.2094991	.37977162
	.06495845	.03212448	.06496946	.03212509
scale				
freemeals	-.35981368	-.36808486	-.59912234	-.61295521
	.16442142	.16448631	.27259725	.27273851
_cons	2.5470469	2.5516626	3.5692049	3.5771444
	.0882327	.08821157	.15204032	.15218042
Statistics				
bic	-1749.3843	-1749.9903	-1749.444	-1750.0511

Legend: b/se

We select `model4`, the model with the complementary log–log link for the conditional mean and the square-root link for the conditional variance, because it has the lowest BIC.

Stored results

`betareg` stores the following in `e()`:

Scalars

<code>e(N)</code>	number of observations
<code>e(k)</code>	number of parameters
<code>e(k_eq)</code>	number of equations in <code>e(b)</code>
<code>e(k_eq_model)</code>	number of equations in overall model test
<code>e(k_dv)</code>	number of dependent variables
<code>e(df_m)</code>	model degrees of freedom
<code>e(ll)</code>	log likelihood
<code>e(ll_0)</code>	log likelihood, constant-only model
<code>e(N_clust)</code>	number of clusters
<code>e(chi2)</code>	χ^2
<code>e(p)</code>	<i>p</i> -value for model test
<code>e(rank)</code>	rank of <code>e(V)</code>
<code>e(ic)</code>	number of iterations
<code>e(rc)</code>	return code
<code>e(converged)</code>	1 if converged, 0 otherwise

Macros

<code>e(cmd)</code>	<code>betareg</code>
<code>e(cmdline)</code>	command as typed
<code>e(depvar)</code>	name of dependent variable
<code>e(wtype)</code>	weight type
<code>e(wexp)</code>	weight expression
<code>e(title)</code>	title in estimation output
<code>e(linkt)</code>	link title in the conditional mean equation
<code>e(linkf)</code>	link function in the conditional mean equation
<code>e(slinkt)</code>	link title in the conditional scale equation
<code>e(slinkf)</code>	link function in the conditional scale equation
<code>e(clustvar)</code>	name of cluster variable
<code>e(chi2type)</code>	Wald or LR; type of model χ^2 test
<code>e(vce)</code>	<i>vce</i> type specified in <code>vce()</code>
<code>e(vcetype)</code>	title used to label Std. err.
<code>e(opt)</code>	type of optimization
<code>e(which)</code>	max or min; whether optimizer is to perform maximization or minimization
<code>e(ml_method)</code>	type of ml method
<code>e(user)</code>	name of likelihood-evaluator program
<code>e(technique)</code>	maximization technique
<code>e(properties)</code>	<code>b V</code>
<code>e(predict)</code>	program used to implement <code>predict</code>
<code>e(marginsok)</code>	predictions allowed by <code>margins</code>
<code>e(marginsnotok)</code>	predictions disallowed by <code>margins</code>
<code>e(asbalanced)</code>	factor variables <code>fvset</code> as <code>asbalanced</code>
<code>e(asobserved)</code>	factor variables <code>fvset</code> as <code>asobserved</code>

Matrices

<code>e(b)</code>	coefficient vector
<code>e(Cns)</code>	constraints matrix
<code>e(ilog)</code>	iteration log (up to 20 iterations)
<code>e(gradient)</code>	gradient vector
<code>e(V)</code>	variance-covariance matrix of the estimators
<code>e(V_modelbased)</code>	model-based variance

Functions

<code>e(sample)</code>	marks estimation sample
------------------------	-------------------------

In addition to the above, the following is stored in `r()`:

Matrices

<code>r(table)</code>	matrix containing the coefficients with their standard errors, test statistics, <i>p</i> -values, and confidence intervals
-----------------------	--

Note that results stored in `r()` are updated when the command is replayed and will be replaced when any `r-class` command is run after the estimation command.

Methods and formulas

Beta regression models were proposed by [Ferrari and Cribari-Neto \(2004\)](#) and extended by [Smithson and Verkuilen \(2006\)](#) to allow the scale parameter to depend on covariates.

Beta regression is appropriate only for a dependent variable that is strictly greater than 0 and strictly less than 1 because the beta distribution has support only on the interval $(0, 1)$. The density of a beta-distributed dependent variable y conditional on covariates \mathbf{x} can be written as

$$f(y; \mu_{\mathbf{x}}, \psi_{\mathbf{x}}) = \frac{\Gamma(\psi_{\mathbf{x}})}{\Gamma(\mu_{\mathbf{x}}\psi_{\mathbf{x}})\Gamma\{(1 - \mu_{\mathbf{x}})\psi_{\mathbf{x}}\}} y^{\mu_{\mathbf{x}}\psi_{\mathbf{x}}-1} (1 - y)^{(1 - \mu_{\mathbf{x}})\psi_{\mathbf{x}}-1}$$

where $\mu_{\mathbf{x}} = \mathbf{E}(y|\mathbf{x})$, $\mu_{\mathbf{x}}$ is linked to the covariates by the link function $g(\mu_{\mathbf{x}}) = \mathbf{x}\beta$, $\psi_{\mathbf{x}}$ scales the conditional variance according to

$$\text{Var}(y|\mathbf{x}) = \mu_{\mathbf{x}}(1 - \mu_{\mathbf{x}})/(1 + \psi_{\mathbf{x}})$$

and $\psi_{\mathbf{x}}$ is linked to the covariates by link function $h(\psi_{\mathbf{x}}) = \mathbf{x}\gamma$.

This parameterization yields a log-likelihood function of

$$\sum_{i=1}^N \omega_i \left(\ln \{ \Gamma(\psi_{\mathbf{x},i}) \} - \ln \{ \Gamma(\mu_{\mathbf{x},i}\psi_{\mathbf{x},i}) \} - \ln [\Gamma \{ (1 - \mu_{\mathbf{x},i})\psi_{\mathbf{x},i} \}] \right. \\ \left. + (\mu_{\mathbf{x},i}\psi_{\mathbf{x},i} - 1) \ln(y_i) + \{ (1 - \mu_{\mathbf{x},i})\psi_{\mathbf{x},i} - 1 \} \ln(1 - y_i) \right)$$

The definitions of the link functions are

Name	Function
<code>logit</code>	$g(\mu_{\mathbf{x}}) = \ln\{\mu_{\mathbf{x}}/(1 - \mu_{\mathbf{x}})\}$
<code>probit</code>	$g(\mu_{\mathbf{x}}) = \Phi^{-1}(\mu_{\mathbf{x}})$
<code>cloglog</code>	$g(\mu_{\mathbf{x}}) = \ln\{-\ln(1 - \mu_{\mathbf{x}})\}$
<code>loglog</code>	$g(\mu_{\mathbf{x}}) = -\ln\{-\ln(\mu_{\mathbf{x}})\}$

The definitions of the scale-link functions are

Name	Function
<code>log</code>	$h(\psi_{\mathbf{x}}) = \ln(\psi_{\mathbf{x}})$
<code>root</code>	$h(\psi_{\mathbf{x}}) = \sqrt{\psi_{\mathbf{x}}}$
<code>identity</code>	$h(\psi_{\mathbf{x}}) = \psi_{\mathbf{x}}$

This command supports the Huber/White/sandwich estimator of the variance and its clustered version using `vce(robust)` and `vce(cluster clustvar)`, respectively. See [\[P\] `_robust`](#), particularly [Maximum likelihood estimators](#) and [Methods and formulas](#).

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Also see

- [R] **betareg postestimation** — Postestimation tools for `betareg`
- [R] **fracreg** — Fractional response regression
- [R] **glm** — Generalized linear models
- [BAYES] **bayes: betareg** — Bayesian beta regression
- [FMM] **fmm: betareg** — Finite mixtures of beta regression models
- [SVY] **svy estimation** — Estimation commands for survey data
- [U] **20 Estimation and postestimation commands**

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